#### **ORIGINAL RESEARCH**



# Cat swarm optimization for solving the open shop scheduling problem

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#### Abstract

This paper aims to prove the efficiency of an adapted computationally intelligence-based behavior of cats called the cat swarm optimization algorithm, that solves the open shop scheduling problem, classified as NP-hard which its importance appears in several industrial and manufacturing applications. The cat swarm optimization algorithm was applied to solve some benchmark instances from the literature. The computational results, and the comparison of the relative percentage deviation of the proposed metaheuristic with other's existing in the literature, show that the cat swarm optimization algorithm yields good results in reasonable execution time.

Keywords Scheduling problem · Swarm optimization · Behavior of cats · Computationally intelligence · Discrete

# Introduction

To solve real optimization problems such as in industrial and manufacturing applications, the problem should be formulated as a theoretical problem. In 1974, Gonzalez and Sahni (1976) had introduced one of the most known complex combinatorial problem called the open shop scheduling problem (OSSP). There are several real-world applications of the OSSP, such as system-on-a-chip testing (Iyengar and Chakrabarty 2002), the area of satellite-switched time-division multiple access (Dell'Amico and Martello 1996), routing packets (Suel 1995), the scheduling and wavelength assignment problem in optical networks that are based on the wavelength-division-multiplexing technology (Bampis and Rouskas 2002), routing in optical transpose interconnect system (Lucas 2010), in routing in

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heterogeneous networks to model communications schedules (Bhat et al. 2000).

The OSSP problem is classified as NP-hard (Gonzalez and Sahni 1976), that is why some researchers had tried to solve it by introducing some methods, such as exact methods, polynomial time algorithm proposed by Gonzalez and Sahni (1976), and the branch and bound developed by Brucker et al. (1997). In general, the exact methods can attain some local solutions and rarely a global solution. The metaheuristic has proven its efficiency to reach the global solution of some problems such as the OSSP. Some metaheuristics are used to solve the OSSP problem, such as simulated annealing (Liaw 1999a) and Tabu search algorithm proposed by Liaw (1999b), genetic algorithm proposed by Prins (2000), extended genetic algorithm proposed by Rahmani Hosseinabadi et al. (2018), hybrid ant colony optimization proposed by Blum (2005), bee colony optimization proposed by Huang and Lin (2011), particle swarm optimization proposed by Sha and Hsu (2008).

This paper presents a new approach for solving the open shop scheduling problem, which is called the cat swarm optimization. In order to prove that the proposed method is efficient, the result obtained by its application to solve some benchmarks instances is compared with those existing in the literature. The rest of the paper is organized as follows; Section two is a description and formulation of the open shop scheduling problem, with an example. Section three presents the cat swarm optimization algorithm, its used parameters, and its process. Section four describes the proposed adaptation of cat swarm optimization to solve the open shop scheduling problem.

# **Open shop scheduling problem**

#### Presentation of the problem

The OSSP (Gonzalez and Sahni 1976) involves a collection of *m* machines  $M = \{M_1, ..., M_m\}$  and a collection of *n* jobsses  $\{J_1, ..., J_n\}$ . Each job J<sub>i</sub> ( $i \in [1, n]$ .) consists of *m* operations  $J_i = \{o_{i1}, o_{i2}, ..., o_{im}\}$ , and each operation  $o_{ij}$  from b Ji executed on a dedicated machine  $M_j (j \in [1, m])$  must be processed in a determined process time  $p_{ij}$ .

The OSSP consists of *n* jobs, *J*, should be processed at most *m* machines, *M*, each job *I* consists of  $n^*m$  operations  $O = \{o_{i1}, o_{i2}, \ldots, o_{im}\}$ , each operation  $o_{ij} = (m_{ij}, t_{ij})$  from job  $J_i$  should be executed in machine  $m_{ij} \in M$  in a determinate execution time  $t_{ij}$ . One performance measure which is considered to be minimized is the total execution time of all process called makespan.

Problematic assumptions

- All operations should be processed.
- Each machine can process at most one operation at a time in determining operation process time.
- The operations in the same job cannot process simultaneously.
- Two operations of the same job cannot be processed at the same time.

#### Formulation of the problem

Let's consider *n* jobs  $J = \{J_1, ..., J_n\}$  and *m* machines  $\{M_1, ..., M_m\}$ , and each job consists of  $n \times m$  operations  $O = \{o_{11}, o_{12}, ..., o_{nm}\}$ , each operation  $t_{ij}$  from the job *I* should be executed in machine *j* at a determinate execution time. The solution is a schedule presented by a sequence of  $n^*m$  operations, numbered from 1 to  $n \times m$ . To calculate the makespan, the data is presented with a matrix of information Minfo that has  $m^*n$  four columns and four rows. The *Minfo* matrix presenting the information of each operation is described in Fig. 1. Let's use:

 $O_i$ : The name (number) of operation *i* in schedule  $(i \in [1, (n * m)])$ .  $J_{o_i}$ : The job of selected operation  $o_i \cdot M_{o_i}$ : The machine name where the operation  $o_i$  should be processed.  $T_{o_i}$ : The processing time of operation  $o_i$ .

## Example

Let's consider the following: 3\*3 OSSP, where n = 3, m = 3,  $J = \{J_1, J_2, J_3\}$ ,  $M = \{1, 2, 3\}$ , and for every  $J_i$  in J,  $Ji = \{(m_{ik}, t_{ik})\}$  for  $k \in [1, 3]$ ,

$0_1$	$O_2$	$O_3$	$O_4$	$O_5$	06	$O_7$	08	$0_9$
$\int J_{o_1}$	$J_{o_2}$	$J_{o_3}$	$J_{o_4}$	$J_{o_5}$	$J_{o_6}$	$J_{o_7}$	$J_{o_8}$	$J_{o_9}$
$M_{o_1}$	$M_{o_2}$	$M_{o_3}$	$M_{o_4}$	$M_{o_5}$	$M_{o_6}$	$M_{o_7}$	$M_{o_8}$	$M_{o_9}$
$\setminus T_{o_1}$	$T_{o_2}$	$T_{o_3}$	$T_{o_4}$	$T_{o_5}$	$T_{o_6}$	$T_{o_7}$	$T_{o_8}$	$T_{o_{9}}/$

Fig. 1 Informations matrix

/1	2	3	4	5	6	7	8	9\
$\begin{pmatrix} 1\\1\\3\\2 \end{pmatrix}$	1	1	2	2	2	3	3	3
3	1	2	1	3	2	1	2	3
$\backslash 2$	3	5	5	7	1	4	5	1/

Fig. 2 The schedule information matrix

J1	=	{(3,	2),	(1,	3),	(2,	5)}
J2	=	{(1,	5),	(3,	7),	(2,	1)}
<i>J</i> 3	=	{(1,	4),	(2,	5),	(3,	1)}

Let's choose a random solution:  $x = \{7, 5, 3, 2, 9, 1, 6, 4, 8\}$ . The representation of information matrix is shown in Fig. 2:

To present the solution, the Gantt chart is used in Fig. 3 by respecting all OSSP problem assumptions and the total makespan of the solution x is:

Makespan (x) = 13.

## Cat swarm optimization algorithm

Cat swarm optimization (CSO) algorithm is a computational intelligent algorithm, inspired from the behavior of cats. The CSO algorithm was introduced by Chu and Tsai (2006). This algorithm is divided into two modes which are the seeking mode and the tracing mode. The seeking mode presents the rest mode in real life of a cat, where it spends the majority lifetime and the tracing mode, when the cat hunts a prey or any moving object. Every cat is characterized by its own position, its velocity, and the flag to identify whether the cat is in the seeking mode or the tracing mode.

The CSO algorithm proposed by Chu and Tsai (2006) was improved by some researchers to ameliorate its efficiency, as using average-inertia weight suggested by Orouskhani et al. (2011), introducing an adaptive parameter control by Wang et al. (2015), parallel cat swarm optimization by PW Tsai et al. (2008), solving combinatorial optimization problem by Bouzidi and Riffi (2013), solving the clustering problem improved by Razzaq et al. (2016), enhanced parallel cat swarm optimization based on the Taguchi method by Tsai et al. (2012). It was also extended to solve multi-objective problems in 2012 by Pradhan and Panda (2012). These improvements were applied to solve some difficult application problems, such as IIR system identification by Panda et al. (2011b), optimizing least-significant-bit





substitution by Wang et al.(2012), optimal placement of multiple UPFC's in voltage stability enhancement under contingency by Kumar and Kalavathi (2014), direct and inverse modeling of plants by Panda et al. (2011a), single bitmap block truncation coding of color images by Cui et al. (2013), linear antenna array synthesis by Pappula and Ghosh (2014), improved metaheuristic techniques for simultaneous capacitor and DG allocation in radial distribution networks by Kawtar et al. (2015).

This paper aims to give an improved CSO algorithm to solve the OSSP problem, and to prove its efficiency, it was applied to solve some benchmark problems.

# CSO to OSSP

To solve the OSSP problem by the CSO, its operators and operations (elementary and global) were enhanced. The improvements are described as follows:

#### **Cat's parameters**

In CSO algorithm, the solution presents the global best solution (Gbest) found by the cats in the swarm; for each cat, the position presents the solution that should be a schedule in OSSP problem. The velocity is used to move from a position to another; in OSSP, a novel solution is obtained by applying a set of swaps to the solution, and thus, the set of swaps is presented by the velocity, and the flag is used to know the cat mode. To sum up, the used operators of each cat in a swarm are:

Mode	Parameter	Role
SM and TM	Position	The schedule solution presented by a sequence of all operations
	Flag	The cat mode (seeking or tracing mode)
ТМ	Velocity	Set of couple permutation $(i,j)$ that will be applied to a position, where <i>i</i> and <i>j</i> are a range of two velocities in the selected position
SM	SMP	Number copies of cats in the SM
	CDC	Percent length of the mutation
	SRD	First rang in the selected solution vector
	SPC	A Boolean value

## Cat's process

The metaheuristic is known by its intelligent combination of two principal concepts which are exploring and exploiting. For the CSO metaheuristic, in each mode, we find the concept of exploration and exploitation. The two modes are combined intelligently with the mixture ratio (MR). The proposal CSO process respects the definition proposed by Chu and Tsai (2006), but some improvements are provided to solve the open shop scheduling problem, and these improved modes are described as follows:

# Seeking mode

The seeking mode (SM) presents the cat at rest and also as being alert-looking around its environment for its next move. The position is presented by a vector of schedule, and for that the four parameters of this mode were adapted, and the new role of each one is:

The seeking mode steps can be described as follows:

- 1. Put *j* copies of the present position of the cat k, with j = SMP. If the value of SPC is true or j = SMP-1, and retain the cat as one of the candidates.
- 2. Generate a random value of SRD
- 3. If the fitness (FS) is not equal, calculate the probability of each candidate by Eq. (a), and the default probability value of each candidate is 1.
- 4. Perform mutation and replace the current position.

$$Pi = \frac{|FS_i - FS_{min}|}{FS_{max} - FS_{min}} \quad \text{where } 0 < i < j \tag{a}$$

where  $FS_i$  is the fitness of cat<sub>i</sub>,  $FS_{max}$  is the maximum fitness in the swarm and the  $FS_{min}$  is the minimal fitness in the swarm. *Example* 

Let's consider in the SM, that the position (solution)  $x = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$ . The size is n = 12, SMP = 5,SPC = True and the first value of SRD = 2.

*Step 1:* The program makes four copies of the selected cat position and considering the selected position as a candidate, because SPC = True.

*Step 2:* For each copy, according to the CDC, randomly increase or decrease the current SRD percentage value, and replace the old values *b* the application of a swap between the

SRD position and the second position that is (CDC + SRD) if the sum is less than 12 (the total size of the problem), else the second position is (CDC + SRD) - (12 + 1).

The first candidate :  $x_1 = \{1,2,3,4,5,6,7,8,9,10,11,12\}$  is the cat position that has been taken in account since SPC=TRUE.



#### The tracing mode

The mode tracing (TM) presents the cat at the quick movement, according to its own velocity, while chasing a pray or any moving object. This section is devoted to describing the parameters, the process and elementary operations used in this mode

*Tracing mode parameters* The used parameters in this mode are:

- $X_{\text{best}}$  The best solution/position of the cat who has the best fitness value
- $V_k$  The old speed value (current value)
- $\vec{V'_k}$  The new value velocity of the cat<sub>k</sub>
- w The inertia weighted parameter
- c A constant
- *r* A random value in the range [0, 1]
- $X'_k$  The new value of the position of the cat<sub>k</sub>
- $X_k$  The actual position of the cat<sub>k</sub>
- $V_k$  The velocity of the cat<sub>k</sub>

(a) Tracing mode process:

The process of TM is given as:

- (1) Update the velocities of each  $cat_k$  According to the equation:
- (2) check if the velocities are of the highest order.

 $V'_{k} = w * V_{k} + r * c * (X_{\text{best}} - X_{k})$  (a)

(3) update the position of the  $cat_k$  according to equation:

$$X'_k = X_k + V_k \tag{b}$$

Elementary operations:

The elementary operations (addition, subtraction and multiplication) used in tracing mode to solve the OSSP are not the same as those defined by Chu and Tsai (2006) to solve continuous optimization problem. The used operation is like the elementary operations defined to PSO algorithm, by Clerc (2004), to solve the combinatorial optimization problem. These operations will be performed on the velocity and the position of each cat in the TM mode.

Let's put x and x' two positions (schedules), and a velocity v represents all permutations to perform.

Let's put:  $X = \{1, 2, 3, 4, 5\}$  and  $v = \{(2, 5), (3, 1), (4, 3)\}$ Opposite of velocity:

Let's put |v| presents the size (number of permutations couple (i, j)) of the velocity  $v = \{(i_k, j_k)[k: 0 \rightarrow |v|]\}$ .

The opposite is defined by:  $\neg v = \{(i_k, j_k) [k: |v| \rightarrow 0]\}$ , with:  $v + \neg v = \emptyset$ .

#### Addition:

This is done between a position  $\mathbf{x}$  and velocity v, in order to have a new position x'.

x + v = x'

Adding operation which translates the movement represents the set of permutations to be applied to the position x to getting a new position x'.

Example

 $x + v = \{4, 5, 1, 3, 2\}$ 

Subtraction (position-position):

This operation is performed between two positions to get a velocity.

x' - x = v

The subtraction is the opposite of the addition operation  $(x'-x=v \Leftrightarrow x+v=x')$ . In this case, by two positions x and x', the result is all permutations performed on x, to obtain x'. These pairs of permutations are the velocity v.

Example

Let's 
$$x' = x + v = \{4, 5, 1, 3, 2\} \Rightarrow x' - x = v$$
  
Multiplication:

This operation is performed between a real *r* and velocity  $v = (i_k, j_k)[k:0 \rightarrow |v|]$ ; the result is a velocity. The different possible cases, according to the real *r*, are:

- If r=0:  $r \times v = 0$
- If  $((r > 0) \text{ and } (r \le 1))$ : Then  $r \times v = (i_k j_k)[k: 0 \rightarrow (c \times |v|)]$
- If (r>1): then separate. Decimal and integer part, r=n+x.
  Where n is the integer part of r, and x corresponds to decimal parts. And returns to each party to the previous cases.
- If (r<0): r×v=(-r)׬v. Now (-r)>0, and you will consider one of the previous case.

#### Example

Let's put  $v = \{(2, 5), (3, 1), (4, 3)\}$  and  $r = 0, 4 \Rightarrow r \times v = \{(2, 5)\}.$ 

The complete mode process:

The flowchart represents the description of the complete CSO process as shown in Fig. 4.

## **Computational results and discussion**

This section presents the obtained results and the discussion of the proposal of CSO to solve some benchmark instances proposed by Taillard (1993) and Guéret and Prins (1999). This proposed adaptation is coded in Visual C++, which runs on an Ultrabook characteristic's 2.1 GHz 2.59 Ghz Intel Core i7 PC with 8G of RAM. Each instance runs for 10 times in the maximum time of 1 h.



Fig. 4 CSO process flowchart

## **Parameter tuning**

The used parameters values in CSO process are the SMP, CDC used in the seeking mode, the parameters w, r and c used in tracing mode, and the MR used in the general process.

For respecting the real life of cats, this paper dose not have to change the SMP, CDC, MR, *c* values and also the range of the variation of the random value *r*.

About the inertia weighted parameter w, this paper had used a fix parameter values such that it was consider in the proposal of CSO to solve combinatorial problem (Bouzidi and Riffi 2014b), that values were analyzed and discussed by the application to solve the TSP problem (Bouzidi and Riffi 2013). After that it was applied to solve other combinatorial problems by using this parameters values, such as the QAP (Riffi and Bouzidi 2014), JSSP (Bouzidi and Riffi 2014a) and FSSP (Bouzidi and Riffi 2015).

To resume, the used parameters values are shown in Table 1.

#### Evaluation of the proposed algorithm

This section presents two tables that show the collected results by the application of the adapted CSO algorithm to the benchmark *instances* of Taillard (1993) in Table 2, and Guéret and Prins (1999) in Table 3. For each instance, the number of job *J* and machines *M* is defined ( $J \times M$ ), the best-known fitness solution (BKS) is found by the existing methods to solve the OSSP to the selected problem instance, the best obtained solution (BS) is found by applying CSO algorithm got in ten runs of the program, and the BS lower than the BKS is marked by \* after the instance name. To prove the efficiency of the CSO, the relative percentage deviation (RPD) is calculated. And the average execution time (Aver\_T) is taken into seconds.

The *RPD* is calculated by:

$$RPD = \frac{BS - BKS}{BKS}$$

Table 2 shows the obtained results by the application of proposed CSO to solve the Taillard (1993) benchmark instances.

Table 2 shows that the application of CSO to solve all proposed *Taillard* instances problems has a lower-to-negligible RPD value, and each instance problem solution is obtained in a reasonable execution time.

Table 3 shows the obtained results by the application of CSO to solve the OSSP benchmark instances proposed by Guéret and Prins (1999).

Also the CSO can find the optimal solution of many benchmark instance problems of *Guéret and Prins* that have the lower values of *RPD*, and the solutions are obtained in a reasonable execution time. Also, when the application takes more time running, the CSO algorithm gives better solutions to all selected benchmark instances. Table 4 proves that CSO application with more time (more than 900 s) can find the best optimal solutions. Table 4 shows some benchmark instance, its size (number of jobs *J* and number of machines *M*), the best-known solution BKS for each one, the best solution (BS) found by the application of CSO method, the number of jobs *J* and the number of machines *M*; the RPD1 presents the relative percentage deviation by executing the application for a maximal time 900 s, and the RPD2 presents the relative percentage deviation by executing the application more than 900 s, and

Table 1      Used parameter's        values in CSO	Parameter	SMP	CDC	MR	w	r	С
	Value	5	0.8	0.3	0.7	[0,1]	2.05

Table 2Result obtained byapplying CSO to solve OSSPinstances proposed by Taillard

Instance	$J \times M$	BKS	BS.	WS	RPD	Aver_T (s)
tail41	4×4	193	193	193	0.00	0.001
tail42	$4 \times 4$	236	236	236	0.00	0.001
tail43	$4 \times 4$	271	271	271	0.00	0.001
tail44	$4 \times 4$	250	250	250	0.00	0.156
tail45	$4 \times 4$	295	295	295	0.00	0.125
tail46	$4 \times 4$	189	189	189	0.00	0.003
tail47	$4 \times 4$	201	201	201	0.00	0.109
tail48	$4 \times 4$	217	217	217	0.00	0.359
tail49	$4 \times 4$	261	261	261	0.00	0.219
tail410	$4 \times 4$	217	217	217	0.00	0.156
Average RPD					0.00	
tail51	5×5	300	300	300	0.00	0.610
tail52	5×5	262	262	262	0.00	0.735
tail53	5×5	323	323	323	0.00	2.235
tail54	5×5	310	310	310	0.00	8.906
tail55	5×5	326	326	326	0.00	1.344
tail56	5×5	312	312	312	0.00	13.813
tail57	5×5	303	303	303	0.00	14.688
tail58	5×5	300	300	300	0.00	35.236
tail59	5×5	353	353	353	0.00	4.032
tail510	5×5	326	326	326	0.00	2.453
Average RPD		520	020	520	0.00	2.155
tail71	7×7	435	435	435	0.00	24.375
tail72	7×7	443	443	444	0.00	26.065
tail73	7×7	468	468	477	0.00	51.658
tail74	7×7	463	463	464	0.00	227.313
tail75	7×7	416	416	416	0.00	169.751
tail76	7×7	451	410	410	0.22	640.466
tail77	7×7	422	432	432	0.22	349.208
tail78	7×7	424	420	424	0.00	21.567
tail79	7×7	458	458	458	0.00	83.953
tail710	7×7	398	438 398	398	0.00	112.39
Average RPD		570	570	570	0.00	112.39
tail101	10×10	637	645	650	1.26	160.762
tail101	10×10	588	588	588	0.00	474.782
tail102	$10 \times 10$ $10 \times 10$	598	599	606	0.17	68.567
tail105	$10 \times 10$ $10 \times 10$	577	577	577	0.00	41.04
tail105	$10 \times 10$ $10 \times 10$	640	640	645	0.00	679.018
tail105	$10 \times 10$ $10 \times 10$	538	538	538	0.00	126.936
tail100*	$10 \times 10$ $10 \times 10$	616	616	619	0.00	22.877
tail108	$10 \times 10$ $10 \times 10$	595	595	601	0.00	375.292
tail100	$10 \times 10$ $10 \times 10$	595	595	599	0.00	263.801
tail109	$10 \times 10$ $10 \times 10$	596	596	600	0.00	112.65
Average RPD		590	570	000	0.00 0.14	112.05
tail151	15×15	937	937	937	0.00	250.323
tail152	15×15 15×15	937 918	937 920	937 926	0.00	230.323 501.669
tail152 tail153			920 871	926 871		498.766
	15×15	871 934	871 934	871 934	0.00	498.766 112.994
tail154	15×15				0.00	
tail155 tail156	15×15	946 022	952 033	959 022	0.63	834.63
tail156	15×15	933	<i>933</i>	933	0.00	149.578
tail157	$15 \times 15$	891	891	898	0.00	867.539

## Table 2 (continued)

Instance	$J \times M$	BKS	BS.	WS	RPD	Aver_T (s)
tail158	15×15	893	893	893	0.00	176.073
tail159	15×15	899	913	931	1.56	658.615
tail1510	15×15	902	902	910	0.00	891.272
Average RPD	):				0.24	
tail201	$20 \times 20$	1155	1166	1170	0.95	457.839
tail202	$20 \times 20$	1241	1260	1267	1.53	618.409
tail203	$20 \times 20$	1257	1257	1257	0.00	340.266
tail204	$20 \times 20$	1248	1253	1259	0.40	816.467
tail205	$20 \times 20$	1256	1256	1256	0.00	432.391
tail206	$20 \times 20$	1204	1204	1204	0.00	806.064
tail207	$20 \times 20$	1294	1310	1317	1.24	859.499
tail208	$20 \times 20$	1177	1210	1234	2.80	695.772
tail209	$20 \times 20$	1289	1289	1289	0.00	207.641
tail2010	$20 \times 20$	1241	1241	1241	0.00	489.458
Average RPD	) <u>:</u>				0.69	

Best results are shown in bolditalics

Table 3Result obtained byapplying CSO to solve OSSPinstances of Guéret and Prins

Instance	J×M	BKS	BS.	WS	%RPD	Aver_T (s)
gp03-01	3×3	1168	1168	1168	0.00	0.001
gp03-02	3×3	1170	1170	1170	0.00	0.001
gp03-03	3×3	1168	1168	1168	0.00	0.001
gp03-04	3×3	1166	1166	1166	0.00	0.001
gp03-05	3×3	1170	1170	1170	0.00	0.001
gp03-06	3×3	1169	1169	1169	0.00	0.001
gp03-07	3×3	1165	1165	1165	0.00	0.001
gp03-08	3×3	1167	1167	1167	0.00	0.001
gp03-09	3×3	1162	1162	1162	0.00	0.001
gp03-10	3×3	1165	1165	1165	0.00	0.001
Average RPD	:				0.00	
gp04-01	4×4	1281	1281	1281	0.00	0.002
gp04-02	$4 \times 4$	1270	1270	1270	0.00	0.002
gp04-03	4×4	1288	1288	1288	0.00	0.001
gp04-04	4×4	1261	1261	1261	0.00	0.003
gp04-05	$4 \times 4$	1289	1289	1289	0.00	0.003
gp04-06	$4 \times 4$	1269	1269	1269	0.00	0.001
gp04-07	4×4	1267	1267	1267	0.00	0.007
gp04-08	4×4	1259	1259	1259	0.00	0.002
gp04-09	$4 \times 4$	1280	1280	1280	0.00	0.005
gp04-10	4×4	1263	1263	1263	0.00	0.001
Average RPD	:				0.00	
gp05-01	5×5	1245	1245	1245	0.00	0.008
gp05-02	5×5	1247	1247	1247	0.00	0.003
gp05-03	5×5	1265	1265	1265	0.00	0.006
gp05-04	5×5	1258	1258	1258	0.00	0.009
gp05-05	5×5	1280	1280	1280	0.00	0.005
gp05-06	5×5	1269	1269	1269	0.00	0.009
gp05-07	5×5	1267	1267	1269	0.00	0.002

Table 3 (continued)

Instance	J×M	BKS	BS.	WS	%RPD	Aver_T (s)
gp05-08	5×5	1287	1287	1287	0.00	0.002
gp05-09	5×5	1262	1262	1262	0.00	0.003
gp05-10	5×5	1254	1254	1254	0.00	0.422
Average RPD:					0.00	
gp06-01	6×6	1264	1264	1264	0.00	0.281
gp06-02	6×6	1285	1285	1285	0.00	1.014
gp06-03	6×6	1255	1255	1255	0.00	0.484
gp06-04	6×6	1275	1275	1275	0.00	0.390
gp06-05	6×6	1299	1299	1299	0.00	0.187
gp06-06	6×6	1284	1284	1284	0.00	0.250
gp06-07	6×6	1290	1290	1290	0.00	0.140
gp06-08	6×6	1265	1265	1265	0.00	0.506
gp06-09	6×6	1243	1243	1243	0.00	0.203
gp06-10	6×6	1254	1254	1254	0.00	0.234
Average RPD:					0.00	
gp07-01	7×7	1159	1159	1159	0.00	0.406
gp07-02	7×7	1185	1185	1185	0.00	0.375
gp07-03	7×7	1237	1237	1237	0.00	0.391
gp07-04	7×7	1167	1167	1167	0.00	5.756
gp07-05	7×7	1157	1157	1157	0.00	0.797
gp07-06	7×7	1193	1193	1193	0.00	0.688
gp07-07	7×7	1185	1185	1185	0.00	1.030
gp07-08	7×7	1180	1180	1180	0.00	12.813
sp07-09	7×7	1220	1220	1220	0.00	0.437
gp07-10	7×7	1270	1270	1270	0.00	0.250
Average RPD:	,,,,,	1270		1270	0.00	0.200
gp08-01	8×8	1130	1130	1130	0.00	27.373
gp08-02	8×8	1130	1130	1135	0.00	3.646
gp08-03	8×8	1110	1110	1110	0.00	76.871
sp08-03 gp08-04	8×8	1153	1153	1153	0.00	6.652
gp08-04 gp08-05	8×8	1218	1133	1218	0.00	5.288
gp08-05 gp08-06	8×8	1115	1115	1115	0.00	198.506
gp08-00 gp08-07	8×8	1113	1113	1126	0.00	214.562
			1120	1120		
gp08-08	8×8	1148	1148 1114		0.00	13.500
gp08-09	8×8	1114		1114	0.00 0.00	240.140
gp08-10	8×8	1161	1161	1161		50.338
Average RPD:	0 0	1120	1100	1100	0.00	200.027
gp09-01	9×9	1129	1129	1129	0.00	209.037
gp09-02	9×9	1110	1110	1112	0.00	72.290
gp09-03*	9×9	1116	1115	1116	0.00	9.028
gp09-04	9×9	1130	1130	1130	0.00	57.012
gp09-05	9×9	1180	1180	1180	0.00	3.723
gp09-06	9×9	1093	1193	1093	0.00	122.432
gp09-07*	9×9	1091	1090	1090	0.00	89.763
gp09-08*	9×9	1106	1105	1105	0.00	200.877
gp09-09	9×9	1123	1123	1139	0.00	84.270
gp09-10	9×9	1112	1120	1121	0.72	741.101
Average RPD:					0.07	
gp10-01	$10 \times 10$	1093	1111	1121	1.65	273.601
gp10-02	$10 \times 10$	1097	1097	1097	0.00	84.298

#### Table 3 (continued)

Instance	J×M	BKS	BS.	WS	%RPD	Aver_T (s)
gp10-03	10×10	1081	1110	1151	2.68	356.432
gp10-04	$10 \times 10$	1083	1090	1109	0.65	428.704
gp10-05	$10 \times 10$	1073	1090	1108	1.58	567.397
gp10-06	$10 \times 10$	1071	1100	1120	2.71	600.557
gp10-07	$10 \times 10$	1080	1084	1117	0.37	475.311
gp10-08	$10 \times 10$	1095	1117	1119	2.01	465.301
gp10-09	$10 \times 10$	1115	1122	1127	0.63	285.534
gp10-10	$10 \times 10$	1092	1113	1123	1.92	262.229
Average RPD	:				1.42	

Best results are shown in bolditalics

**Table 4** Results in more than900 s of CPU time

Instance	$J \times M$	BKS	BS.	RPD2	RPD1	Aver_T (s)
in152	15×15	918	918	0.00	0.76	5391.31
in155	15×15	946	946	0.00	0.85	1763.04
in201	$20 \times 20$	1155	1155	0.00	0.95	2089.60
in204	$20 \times 20$	1248	1248	0.00	0.40	1248.00
in207	$20 \times 20$	1294	1294	0.00	0.53	5050.18
gp10-08	$10 \times 10$	1095	1097	0.18	2.01	1486.45

until it obtains the best solution, and the average time execution in ten runs (Aver\_T) to seconds.

# Comparison with other metaheuristics and discussion

This part aims to compare the average RPD of seven methods, including the one obtained by applying CSO to OSSP. Those other methods are two of hybrid variable neighborhood search methods (VNS), which are VNS-based curtailed fashion VNS (CLS) and VNS-based greedy local search VNS (GLS), two-phase solution method (TPSM), genetic algorithm (GA), the genetic algorithm incorporating the mutation (MGA) (Naderi and Zandieh 2014) and the electromagnetism algorithm (EA). All these methods run in a PC with 2.0 GHz Intel Core 2 Duo and 2 GB of RAM memory.

The average RPD obtained by each metaheuristic for the different problem size of two known benchmark instances (Taillard 1993; Guéret and Prins 1999) is presented as follows:

In order to do the comparative study, the best way used is the graphical representation that provides a visual display to more assess the collected average RPD results to solve the differents benchmark instances by the metaheuristics in study. For this reason, the results in Table 5 were translated into two graphs; Fig. 5 represents the variation of RPD of the seven methods for the different size of *Taillard* benchmark instances problems; Fig. 6 is like the first but of the benchmark instances are of Guèret and Prins.

Figure 5 shows that the CSO algorithm had the lower RPD for the different problem size instances, which means that it has more efficiency than the others.

Again, Fig. 6 shows that the CSO algorithm had the lower RPD for the different problem sizes, which means that the CSO is more efficient than other methods.

# Conclusion

To conclude, this paper presented the efficiency of the cat swarm optimization algorithm to solve the theoretical problem, open shop scheduling problem, by its ability to find the best-known solution for some benchmark instances and to find the new best solutions. The comparison of the results of the CSO method to some recent existing methods to solve OSSP problem has also proved the efficiency of the CSO algorithm to solve the OSSP

Table 5      The average RPD        obtained of each of the methods	Benchmark instances size	Algori	thms					
against two well-known		CSO	VNS (CLS)	VNS (GLS)	GA	MGA	TPSM	EA
benchmarks	Taillard							
	4×4	0.00	0.00	2.26	3.53	0.00	3.89	0.42
	5×5	0.00	1.30	3.51	4.49	2.48	5.54	2.20
	7×7	0.55	1.67	3.17	4.76	3.11	6.08	1.68
	10×10	0.16	2.66	4.46	3.68	0.13	6.35	2.10
	15×15	0.67	_	_	_	-	-	2.03
	$20 \times 20$	1.22	4.08	5.64	3.46	1.66	8.46	1.72
	Guèret and Prins							
	3×3	0.00	0.00	2.97	2.41	0.00	3.21	0.75
	4×4	0.00	0.00	3.98	3.05	0.00	4.80	0.89
	5×5	0.00	0.48	3.90	4.50	1.89	5.06	1.47
	6×6	0.00	1.56	3.49	4.93	2.34	5.18	1.99
	7×7	0.00	2.15	3.10	5.33	2.49	4.73	2.08
	8×8	0.00	1.26	3.77	4.91	1.53	5.05	1.36
	9×9	0.06	2.32	4.54	4.83	1.06	5.10	1.64
	10×10	1.94	3.05	5.69	5.43	2.80	6.82	2.74



Fig. 5 Mean plots for metaheuristic versus the problem size of Taillard benchmark instances



Fig. 6 Mean plots for metaheuristic versus the problem size of Guèret and Prins benchmark instances

problem. That is why, the aim is to extend the proposed metaheuristic to be applied to various real applications based on OSSP.

## **Compliance with ethical standards**

Conflict of interest There is no conflict of interest with this research as known by the authors.

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