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A New Image Encryption Algorithm Using a Hyperchaotic Lorenz System to Produce Efficient and Sufficiently Swift Responses to Different Security Needs of Clients

Zahra Kaviyani¹, Mahnaz Mohammadi*^{,2}, Abbas Kamali³

- ^{1, 2} Department of Electrical Engineering Telecommunications, Faculty of Engineering Sciences, Shiraz Branch, Islamic Azad University, Shiraz, Iran
- 3 Department of Electrical Engineering, Faculty of Engineering Sciences, Fasa Branch, Islamic Azad University, Fasa, Iran

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Abstract

This paper proposes a new plaintext-related mechanism based on plaintext encryption. For simplicity, PCODE was proposed as the image encryption code. The original picture was encoded to get the proposed encryption and plaintext encryption with a chaotic sequence to control the PCODE rules. Another chaotic sequence was encoded into a PCODE sequence for the PCODE XOR operation. The remaining two chaotic sequences were then processed with the proposed scheme to get two key streams for the permutation phase. The cipher image was obtained after the conventional permutation and PCODE XOR operations. The use of the proposed plaintext encryption leads to the correlation between the keystreams used in the displacement phase and both the secret key and the plaintext image. This correlation increases the sensitivity and security of the encryption system with respect to the plaintext. The experimental findings from simulation show that the proposed encryption system shows significant efficiency and security.

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*Corresponding author: Mahnaz Mohammadi

Address: Department of Electrical engineering telecommunications, Faculty of Engineering Sciences, Shiraz Branch, Islamic Azad University, Shiraz, Iran. Tell: 00989177135548 Email: mahnazlm53@gmail.com

1.INTRODUCTION

 Cryptography reduces maintaining the confidentiality of a message of large and arbitrary length to maintaining the confidentiality of a short key. The foremost criterion that determines the robustness of an encryption algorithm has nothing to do with the possibility of cracking it: if sufficient plaintext-ciphertext pairs are available, any encryption algorithm will eventually crack [1-2- 3]. The greatest strength of an encryption algorithm is the ability to run it in a reasonable time window. The text that takes years to crack, let alone with a network of supercomputers, is actually extremely secure [4]. Early cryptographic systems substantially depended on maintaining the confidentiality of the encryption algorithm to ensure security. Gradually, these algorithms evolved to resolve the problem of key length dependence and confidentiality [5]. Today, the most reliable encryption algorithms have no choice but to successfully pass multiple rounds of scrutinized and non-confidential investigation to gain the trust of enterprises and customers. Naturally, it is

intractable to develop reliable encryption algorithms and test them publicly rather than confidentially [5-6-7-8-9]. Choosing weak or poorly protected keys is a sincere invitation to penetrators. If an intruder gains access to an encryption key, even the most robust encryption algorithms will fail to protect the data [8- 9-10].

Modern encryption algorithms fall into symmetric and asymmetric groups. Symmetric encryption schemes can be divided into direct, partial, and compression-encryption designs. Each method can encrypt a different volume of data from an image. They also provide different levels of security and efficiency [11-12-17]. In direct encryption, the entire contents of the image are directly encrypted using a new or standard method, while in partial encryption, only some specific parts of an image are encrypted and the rest remains unencrypted. In a compression-encryption scheme, compression is combined with encryption. Since direct encryption encrypts a large portion of the image data, it provides improved security at the expense of slower speed. Instead, the volume of encrypted data decreases in partial and compression-encryption, and the amount of encrypted data decreases, thus enabling higher rates at the cost of lower security [18-19]. This study aims to achieve high security and reasonable image encryption speed efficiency. Therefore, direct symmetric encryption is used to ensure sufficient security.

 This paper provides a systemic perspective on image encryption, a subject that has a significant research gap. While AES is the preferred method for symmetric

encryption of text documents, it is not well-suited for image encryption due to its low-speed performance and the reflection of correlation and pixel redundancy in the encrypted image [13]. Therefore, image cryptography requires encryption algorithms that preserve the unique properties of the image during encryption. Most studies that do not systematically address image encryption are mainly concerned with confidentiality, an element that can be achieved by a comprehensive image encryption scheme. Multimedia data communications have become very important due to the openness and sharing of networks, especially for digital images related to the military, medicine, and other disciplines dealing with sensitive information. The development of a secure digital image encryption technique has become a critical research focus. Nonetheless, with the inherent properties of digital images - massive data capacity, the strong correlation between adjacent pixels, and high redundancy common text cryptography systems, such as data encryption standard (DES), advanced encryption standard (AES), and similar systems, are unsuitable for image encryption [1]. Many plaintext or non-plaintext algorithms for image encryption based on chaotic systems are insecure and inefficient against chosenplaintext attacks (CPAs).

2.THE THEORY OF THE PROPOSED ALGORITHM

The proposed design implements encryption using a four-dimensional hyperchaotic Lorenz system [10]. Eq. (1) describes the theory:

$$
x = a(y - x) + w
$$

\n
$$
y = cx - y - xz
$$

\n
$$
z = xy - bz
$$

 (1) where $a = 10$, $b = 8/3$, $c = 28$, etc. $-1.52 \le r \le -0.06$ are the parameters of the hyperchaotic Lorenz system. Using the Lyapunov exponents spectrum on the differential system proposed in [9], if the parameter is set to $r = -1$, four Lyapunov exponents are obtained: $λ1=0.3381$, $λ2=0.1586$, $λ3=0$, and $λ4=$ 15.1752. Furthermore, Fig. 1 shows the hyperchaotic attractors.

Fig. 1. The hyperchaotic Lorenz system, (a) $a = 10$ $\cdot b = 8/3$ $\cdot c = 28$ \cdot (b) $a = 1$ $\cdot b = 1$ 8/3 \cdot c = 28 \cdot (c) a = 10 \cdot b = 1/3 \cdot c = 28 \cdot (d) a = 10 \cdot b = 8/3 \cdot c = 2

As you can see in Fig. 1, compared to low-scale systems, a hyperchaotic system has complicated attractors.

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3.THE PERFORMANCE OF THE PROPOSED CODE

In the context of the binary system, it can be seen that the binary data represented by the digits 00 and 01 are correspond to the corresponding 11's and 10's complements. Hence, by assigning the four operands, X, Y, Z, and W to represent the binary numbers 00, 01, 10, 11, respectively a total of 24 distinct encoding rules can be formulated. However, only eight encoding rules correspond to the complementary base pairing principle. The rules are listed in Table 1.

many res

The image encoding process involves the initial conversion of pixel values into binary numbers, which are subsequently encoded into the designated PCODE encoding sequence. In contrast, the PCODE sequence can be decoded using the same coding rule to extract the corresponding pixel value. For instance, A pixel with a value of 188, which corresponds to the binary representation of "10111100", can be encoded as a PCODE sequence of "YWWZ" according to Rule 3, and as "WXXY" according to Rule 7. Various binary sequences can be derived from the same PCODE sequence using distinct PCODE. the PCODE sequence "WXYZ" can be decoded as "10001101" and "11100100" by applying rules 1 and 5. Table 2 shows the performance of XOR operation on PCODE, which is used in the dissemination stage.

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4. A GENERAL DESCRIPTION OF THE PROPOSED ALGORITHM

Fig. 2 illustrate the flow diagram of the suggested algorithm.

Fig. 2. The flow diagram of the suggested algorithm

Without undermining the totality, it is assumed that we have an original image named I with $M \times N$ dimensions. First, I is changed into the one-dimensional array P with $M \times N$ dimensions. In the proposed design, four secret keys, including fx0, y0, z0, w0g, have been selected as the primary values of the fourdimensional hyperchaotic Lorenz system. They are resolved using the fourthorder Runge-Kutta algorithm as much as the h=0.002 stage. In order to generate four random sequences xn, yn, zn, and wn, all of which have the same size $r =$ $M * N$, equation (2) is used, which leads to the elimination of the previous N0 iteration values.

$$
\begin{aligned}\nx_n &= \{x_1, x_2, x_3, \dots, x_r\} \\
y_n &= \{y_1, y_2, y_3, \dots, y_r\} \\
z_n &= \{z_1, z_2, z_3, \dots, z_r\} \\
w_n &= \{w_1, w_2, w_3, \dots, w_r\} \\
x_n &= \{x_1, x_2, x_3, \dots, x_r\} \\
y_n &= \{y_1, y_2, y_3, \dots, y_r\} \\
z_n &= \{z_1, z_2, z_3, \dots, z_r\} \\
w_n &= \{w_1, w_2, w_3, \dots, w_r\}\n\end{aligned}\n\tag{2}
$$

Then, Eq. (3) is run on x_n and y_n sequences to obtain X and Y sequences.

$$
X = f \text{loor}\left(\text{mod}(x n(i) \times 10^{15}, 8)\right) + 1
$$

$$
Y = f \text{1} \text{ppr}(\text{mod}(y n(j) \times 10^{15}, 256))
$$
 (3)

Where

I, $j=1, 2, ..., r$

In the next stage, Array P and Sequence Y are converted into Pb and Yb binary arrays. Then, using Sequence X as an encryption rule, the binary Pb and Yb are encoded to obtain PCODE_P and PCODE_Y. Note that any PCODE_Pi or PCODE Yi consists of the four elements represented by "X" \cdot "Y" \cdot "Z" and "W".

This paper introduces a new plaintext-related mechanism based on PCODE plaintext encryption (PPPC). First, the numbers X , Y , Z , and W in PCODE P are calculated. They are respectively named numX \cdot numY \cdot numZ and numW. Then, their values are used in Eqs. [2] to calculate the plaintext encryption. Unquestionably, invaders cannot be aware of the value of X elements; thus, it is impossible to obtain the amount of the plaintext encoding and select or create special images to break the proposed algorithm.

Finally, the PPPC, which is used to process the zn and wn chaotic sequences, is employed with the following equation to produce two Z and W sequences in

the permutation stage of the PCODE level. Algorithm 4-1 involves the precise permutation process.

$$
\begin{cases}\nZ = floor\left(mod\left((z_n(k) \times PPPC), M\right)\right) + 1 \\
W = floor\left(mod\left((w_n(l) \times PPPC), 4 \times N\right)\right) + 1\n\end{cases} (9)
$$

Fig. 3 shows the stream flowchart of the encryption-decryption system to encrypt a 3×3 image. In this flowchart, the original image and a secret key are used along with the scrambled sequence, which provides an encrypted image after two stages of coding. More details of this method are provided below.
Password key

Fig. 3. displays an example of an encryption scheme.

Figure 3 shows the flow diagram of the proposed algorithm for encoding a 3x3 image. In this figure, the process of transforming the image into a onedimensional array P, generating random sequences, converting the sequences xn and yn into sequences X and Y, converting the arrays P and Y into binary arrays Pb and Yb, encoding the binary arrays using the sequence X and Simple text computation is shown to generate the Z and W sequences. The innovative method proposed in the proposed algorithm is to use plain text to maintain security and prevent various attacks. Also, using random sequences and combining random data in the proposed algorithm has an advantage for security

and increasing the randomness of information.

5.IMPLEMENTATION OF THE PROPOSED METHOD

In the proposed method, confidential information is encrypted using the proposed algorithm. The encrypted information is then encoded into the host images. The data volume that can be stored in a host depends on the nature of the host and to what extent the data can be concealed without seriously compromising transparency .

Here, encryption is performed first on text information and then on digital images. To that end, standard, common images were used. After encryption, the encrypted data into different images is then encrypted to compare the quality of the encrypted images. The performance and efficiency of the design were also compared to previous works. The proposed method was implemented in MATLAB. The proposed method's output image was better than the image outputs of other algorithms. Many functions were expressed through this implementation. In this section, image simulation was carried out in standard conditions key $x0 = 1.1$, etc. key $y0 = 2.2$, etc. key $z0 = 3.3$, etc. key $w0 = 4.4$, and $N0 = 2000$. Figs. (4) and (7) show the original and encrypted images, respectively. The simulation results indicate that the plaintext image information cannot be identified from the cipher image. Fig. 5 displays the decrypted image, which fully retrieves the plaintext image information. Fig. 7 shows the image decrypted with the wrong key $x0 = 1.10000000000001$, key $y0 = 2.2$, key z0 $= 3.3$, key w0 = 4.4, and N0 = 2000. As shown, the wrong key fails to retrieve the original key.

Fig. 4. The image of the host used in encryption, (a) nature image, (b) airplane (c)

Fig. 5. The encrypted images, (a) Encrypted nature image, (b) Encrypted airplane (c) Lena encrypted

Fig. 7. The images were decrypted with the wrong key, (a) Wrong key decrypted nature image, (b) Wrong key decrypted airplane (c) Wrong key decrypted Lena

There is generally a strong correlation between adjacent pixels in the plaintext image. This correlation should be reduced to near zero after encryption with a

secure encryption system (note that the theoretical value is zero). In the experiment, the correlation coefficients of all adjacent pixels in four directions of the unencrypted and encrypted images (See Table 3). Table 4 compares the proposed algorithm's results with other algorithms in detail.

TABLE III

TABLE IV THE CORRELATION COEFFICIENTS OF THE IMAGE OF LENNA, ENCRYPTED WITH DIFFERENT ENCRYPTION SCHEMES

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FIG. 8. The images decrypted with the wrong key, (a) Original image correlation (b) Encrypted image correlation

Fig. 8. The histogram diagram of the original and encrypted images of Lenna at a higher resolution, (a) Original image correlation (b) Encrypted image correlation

Table 5 presents the results of the histogram variance of the image encrypted by various encoding algorithms. Compared to similar algorithms, our proposed design's histogram of the encrypted image is flatter.

TABLE V							
THE HISTOGRAM VARIANCE OF THE GRAY IMAGE ENCRYPTED BY VARIOUS							
	Proposed	[3]	[4]	[5]	[6]	[7]	[8]
	algorith						
	m						
Lenna	957.2	1104.711			1043.214 977.02 973.2578	1027.593	5118.094

TABLE V

6.ENCRYPTION TIME ANALYSIS

In practical applications, the speed at which the system runs the encryption is also a critical indicator in addition to the security function. This section evaluates the running time in seconds. Table 6 illustrate the implementation time of the image encryption system proposed. As shown, the proposed design performs better at encryption speed. Moreover, time complexity (represented by Q) is demonstrated and analyzed. In our proposed design, time consumption mainly involves stages of generating key streams, encoding/decoding of PCODE, permutation, and dissemination. For a gray-scale image with a dimension of M \times N, the time complexity of encryption and decryption is Q (8 \times $M \times N$). At the stage of permutations and dissemination, the modified object is the PCODE sequence with a complexity of $Q(4 \times M \times N)$. Moreover, the hyperchaotic Lorenz system is solved to obtain chaotic sequences in which time complexity is $Q(M \times N)$. Therefore, the proposed design's time complexity is $Q(8 \times M \times N)$. The proposed method's encryption and decryption have higher time complexity through time complexity analysis.

7. CONCLUSION

This paper proposes a new mechanism involves encoding the original image to obtain PCODE encryption and PPPC encoding. The PPPC encoding is then utilized to process chaotic sequences, which generates key streams to be used in the permutation phase. This approach for generating key streams is different from the methods used in previous PCODE-based chaotic image encryption algorithms. The main strength of any encryption algorithm is the possibility of executing it at an acceptable time. A text that can be broken after years with a network of supercomputers is actually very secure [14-15-16-20]. Early encryption systems were very dependent on the confidentiality of the encryption algorithm to maintain security; gradually, encryption algorithms based on key length and confidentiality have prevailed [21]. Today, the most reliable cryptographic algorithms have to pass several rounds of rigorous and nonconfidential research in order to win the trust of organizations and customers [17-18]. Naturally, it is very difficult to create reliable encryption algorithms and test them publicly and non-confidentially [22-23-24-25].

Choosing a weak key or protecting it improperly opens the way for intruders to enter, if an intruder gets access to an encryption key, even the strongest encryption algorithms are not able to protect the desired data [14]. In this article, the most important thing is the system view of the image encryption category, which has been neglected until now. In image encryption, algorithms are needed to consider the special features of the image during encryption. In this article, the main concern is the aspect of confidentiality in security, which is provided by a comprehensive system design. This article presents a fuzzy adaptive model based on user needs for image encryption using AES, chaotic function and genetic operators.

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