



## Controlled/Uncontrolled Rectifier Harmonic Modeling Using Differential Function Averaging Method

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Article info	Abstract
<p><b>Keywords:</b></p> <p>Numerical Model Recursive functions Harmonic Components Line Commutation Differential Equation</p> <p><b>Article history:</b> Received: 23 Apr 2024 Accepted: 10 Jul 2024</p>	<p>Modeling techniques play a crucial role in enabling designers to gain a deep understanding of the internal variables and dynamic behavior of power electronic systems, thereby facilitating accurate hardware implementation and performance optimization. In the case of line-commutated switching converters, precise modeling of voltage and current harmonics is essential for evaluating system performance, electromagnetic compatibility, and component stress. This paper presents a mathematical modeling approach based on recursive differential equations to accurately calculate voltage and current harmonics in line-commutated converters. Due to the inherently nonlinear voltage–current characteristics of power semiconductor switches, conventional linear modeling techniques are inadequate for capturing the true behavior of such systems. Consequently, a nonlinear modeling framework is required. The proposed method begins by transforming the nonlinear characteristic curves of the switching devices through a rotation process, allowing the extraction of an equivalent voltage–current representation suitable for mathematical analysis. Subsequently, the impedance and transmission matrices of the linear components within the converter are derived using classical mesh and nodal analysis techniques. These matrices provide a structured representation of the passive network elements and their interactions. In the next stage, a comprehensive system block diagram of the converter is constructed, incorporating differential operators that describe the system dynamics. A recursive differential computation method based on multivariable Runge–Kutta algorithms is then employed to calculate the instantaneous values of system variables, including voltages and currents, over time. This approach enables accurate time-domain analysis while preserving the nonlinear behavior of the switching elements. Using the computed instantaneous parameters, the off-state switching angles are determined, and the amplitudes of voltage and current harmonics up to desired orders are extracted. These results are subsequently used to derive a complete numerical model of the converter. Finally, simulation results obtained through the proposed modeling technique are compared with those derived from conventional analytical–algebraic methods. The comparative analysis demonstrates strong agreement between the two approaches, confirming the accuracy and effectiveness of the proposed method. The results highlight the capability of the suggested modeling framework to reliably estimate voltage and current harmonics in nonlinear switching converters, making it a valuable tool for advanced power electronics design and analysis.</p>

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## 1. Introduction

Within industry, the ultimate cost of a switch is a determinative parameter. Due to this, in high-power rectifiers, usage of switches such as Thyristor and Triac are economically advantageous compared to other switches. The high-power rectifiers are used within application like welding machine, HVDC, remote control, etc. [1]. The aim of the modeling is to determine an equivalent circuit for the switch so that it can substitute the switch while showing the actual state of the characteristics of the electrical circuit. Here, the better the modeling would be, the more precise estimation capability of the operation point of the switch is [2]. For switches in which the conduction interval or their on-off timing are specified, the modeling process is easier, however, for thyristor and triac it can be more complicated since although their firing angles are given, but the extinction angle is dependent on the circuit conditions [3]. The traditional method to determine the voltage and current of the switches in converters is to state the corresponding differential equations and solve them. Nonetheless, as the number of the switches increases, finding the solution become cumbersome. The solution includes two components which are the permanent and transient parts even though in the rectifier power analysis, only the permanent characteristic is important. On the other hand, for higher powers, it can be claimed with acceptable approximation that most of the signal power is included within the first three components of the Fourier series, that is, the DC part of the signal and the first and second harmonics [4]. There are various method to describe linearly the nonlinear devices, however, these method are mostly complicated and of low performance. In the ideal case, the semiconductor switches can be seen as a switch that is in on and off state, each for a while [5]. When the on and off periods of the switch and the equivalent impedance across it are known, the voltage and current harmonics of the switch can be determined for each frequency and harmonic independently. Here, using the vector-matrix operations, values of the active and reactive powers of each component can be obtained. We assume that other than the switches within the circuit, the rest of the devices are all linear. If a model is presented for a triac, it can be used for the thyristor family too [6].

## 2. Rotated Switch Characteristic Curve

The characteristic curve of triac is shown in fig. 1.

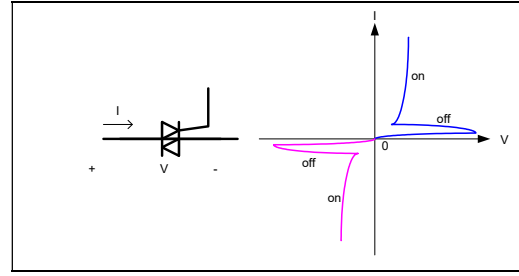


Fig. 1: The characteristic Curve of Triac

Also, its states of voltage and current for an ideal on and off case are depicted in fig. 2 [7].

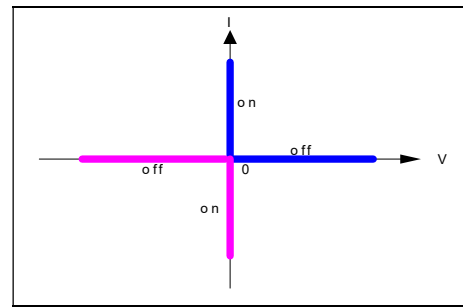


Fig. 2: The Ideal Characteristic Curve

This curve can be interpreted as two perpendicular line, one for  $V = 0$  for on state and the other for  $I = 0$  in off state. When the curve in fig. 2 is rotated 45 degrees clockwise, the curve in fig. 3 would be obtained [8]. This curve is combined of two line segment, one from the relation  $I' = V'$  for the on state and  $I' = -V'$  for the off state. The length of each line segment within the curve is proportional to the applied voltage, firing angle and amplitude of the flowing current. The operating point of the switch at each moment is located on one of the line segments and when it changes into another operating point, it must cross in the coordinated system [8].

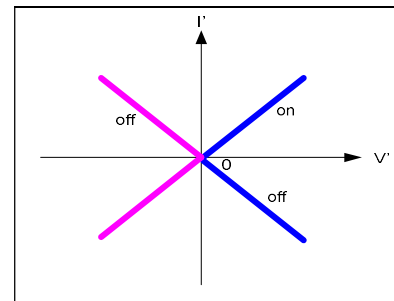


Fig. 3: The Ideal Rotated characteristic Curve

The Rotation matrix and its inverse are respectively denoted by  $T$  and  $T'$ . The analysis of the switch

behavior using two different individual matrices makes the modeling process easier. Now, the triac behavior can be described using the matrix transformation in fig. 4. Using the rotation, the I-V curve would be transformed into a function which facilitate the finding the equations' solutions.

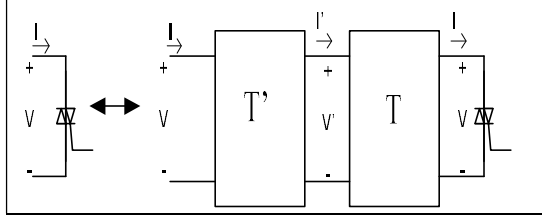


Fig. 4: The Equivalent Block of the Triac

The T and T' matrices along with the related transformations are stated in (1) and (2), which can be inserted into the block diagram, correspondingly.

$$\begin{bmatrix} V' \\ I' \end{bmatrix} = [T] \begin{bmatrix} V \\ I \end{bmatrix}, T = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ -1 & 1 \end{bmatrix} \quad (1)$$

$$\begin{bmatrix} V \\ I \end{bmatrix} = [T'] \begin{bmatrix} V' \\ I' \end{bmatrix}, T' = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix} \quad (2)$$

Multiplication of T and T' gives the identity matrix I. Even through using the ideal curve in fig. 2 instead of the actual characteristic curve in fig. 1 causes some error in the subsequent equations, the value of this error is negligible. Because the line commutation here mostly is used in converter of high powers, the mentioned error would be very small and insignificant. Also, the voltage loss across the switch and its inverse saturated current are negligible compared to the converter current [9].

The characteristic curve presented here can be generalized to all the switches of thyristor family; the firing time in all members is arbitrary and extinction time is determined by the line commutation conditions [10]. The reason behind choosing triac, is that it is bidirectional and second its characteristic curve is more general; it goes without saying that the modeling process presented here has similar routine for all the members of the triac family [11].

In order to estimate the extinction angle of the switch, the resulted mathematical equations of the transformation matrices will be expanded.

### 3. Switch's Voltage and Current calculation

To determine voltage and current of the switch, the third and higher order harmonics will be neglected from consideration. This assumption is totally safe for high powers [12]. To find a unique solution, the calculations are done in the I'-V' coordination; thus, the Fourier expansion of the switch's voltage and current can be computed using (3) and (4).

$$(3) \quad V'(t) \cong V'_0 + V'_1 \sin(\omega t + \phi'_1) + V'_2 \sin(2\omega t + \phi'_2)$$

$$(4) \quad I'(t) \cong I'_0 + I'_1 \sin(\omega t + \psi'_1) + I'_2 \sin(2\omega t + \psi'_2)$$

The on/off interval of the switch shown in fig. 5.

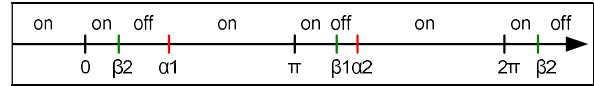


Fig. 5: on and off states of the switch within one period

In fig. 5,  $\alpha_1$  and  $\alpha_2$ , respectively, denote the firing angles in the positive and negative half-period and  $\beta_1$  and  $\beta_2$  are their corresponding extinction angles. As the triac goes to the off state when the line commutation occurs, the voltage loss across the switch and its holding current are assumed to be zero. The triac goes to off state when the anode-cathode voltage becomes zero. Thus, given the firing angles, the extinction angles can be determined through solving the equation  $V'(t) = 0$  [13]. Therefore, by expansion of (3), the relation (5) can be derived. Then, solving (5) and determining the true solutions gives the extinction angles [14].

$$\begin{aligned} \kappa_4 \sin^4(\alpha) + \kappa_3 \sin^3(\alpha) + \kappa_2 \sin^2(\alpha) + \kappa_1 \sin(\alpha) + \kappa_0 &= 0 \Rightarrow \\ \kappa_4 &= 4V'^2_2 \\ \kappa_3 &= 4V'_1 V'_2 \sin(\phi'_1 - \phi'_2) \\ \kappa_2 &= V'^2_1 - 4V'^2_2 - 4V'_0 V'_2 \sin \phi'_2 \\ \kappa_1 &= 2V'_1 (V'_2 \sin(\phi'_2 - \phi'_1) + V'_0 \cos \phi'_1 - V'_2 \sin \phi'_1 \cos \phi'_2) \\ \kappa_0 &= (V'^2_2 - V'^2_1) \sin^2 \phi'_2 + V'^2_0 + 2V'_0 V'_2 \sin \phi'_2 \end{aligned} \quad (5)$$

Since when the switch is on we have  $I'=V'$  and when it is off,  $I'=-V'$ , the 0'th and 1'th and 2'th harmonic component can be calculated where the sine and cosine parts can be expressed as in (6)-(12) through the following equations.

$$I'_0 = \frac{1}{2\pi} \int_0^{2\pi} I'(t) d(\omega t) \quad (6)$$

$$I'_{1C} = \frac{1}{\pi} \int_0^{2\pi} I'(t) \cos(\omega t) d(\omega t) \quad (7)$$

$$I'_{1S} = \frac{1}{\pi} \int_0^{2\pi} I'(t) \sin(\omega t) d(\omega t) \quad (8)$$

$$I'_1 = \sqrt{I'^2_{1C} + I'^2_{1S}}; \psi'_1 = \tan^{-1}\left(\frac{I'_{1S}}{I'_{1C}}\right) \quad (9)$$

$$I'_{2C} = \frac{1}{\pi} \int_0^{2\pi} I'(t) \cos(2\omega t) d(\omega t) \quad (10)$$

$$I'_{2S} = \frac{1}{\pi} \int_0^{2\pi} I'(t) \sin(2\omega t) d(\omega t) \quad (11)$$

$$I'_2 = \sqrt{I'^2_{2C} + I'^2_{2S}}; \psi'_2 = \tan^{-1}\left(\frac{I'_{2S}}{I'_{2C}}\right) \quad (12)$$

Where,  $I_0$  is the DC component of the current,  $I_s$ , the sine component,  $I_c$ , the cosine component and  $\psi'$ , the angle of the corresponding component. The parametric solution of the extinction angles are expressed in (13).

$$V'(t) = 0 \Rightarrow \beta_1, \beta_2; \frac{dV'(\beta_1)}{dt} < 0, \frac{dV'(\beta_2)}{dt} > 0 \quad (13)$$

In the equation, in the first extinction angle  $\beta_1$ , the slope of the voltage is negative while in the second,  $\beta_2$ , the slope of the voltage is positive. Therefore, the current components are determined in terms of the voltage, which are expressed in (14)-(18) after some manipulation. In the following relations,  $\alpha$  is the firing angle,  $\beta$ , the extinction angle and  $\psi$  the phase difference. Also, the indices 1 and 2 denote the first and second half-cycles. Eqs. (15)-(16) are for the first component and (17)-(18) for the second one.

$$\begin{aligned} I'_0 &= \frac{V'_0}{\pi} (\pi + \beta_2 + \beta_1 - \alpha_2 - \alpha_1) + \\ &\frac{V'_1}{\pi} (\cos(\alpha_1 + \phi'_1) + \cos(\alpha_2 + \phi'_1) - \cos(\beta_1 + \phi'_1) - \cos(\beta_2 + \phi'_1)) + \\ &\frac{V'_2}{2\pi} (\cos(2\alpha_1 + \phi'_2) + \cos(2\alpha_2 + \phi'_2) - \cos(2\beta_1 + \phi'_2) - \cos(2\beta_2 + \phi'_2)) \end{aligned} \quad (14)$$

$$\begin{aligned} I'_{1C} &= \frac{2V'_0}{\pi} (\sin\beta_2 + \sin\beta_1 - \sin\alpha_2 - \sin\alpha_1) + \\ &\frac{V'_1}{\pi} (\pi + \beta_2 + \beta_1 - \alpha_2 - \alpha_1) \sin\phi'_1 + \\ &\frac{V'_1}{2\pi} (\cos(2\alpha_1 + \phi'_1) + \cos(2\alpha_2 + \phi'_1) - \cos(2\beta_1 + \phi'_1) - \cos(2\beta_2 + \phi'_1)) + \\ &\frac{V'_2}{\pi} (\cos(\alpha_1 + \phi'_2) + \cos(\alpha_2 + \phi'_2) - \cos(\beta_1 + \phi'_2) - \cos(\beta_2 + \phi'_2)) + \\ &\frac{V'_2}{3\pi} (\cos(3\alpha_1 + \phi'_2) + \cos(3\alpha_2 + \phi'_2) - \cos(3\beta_1 + \phi'_2) - \cos(3\beta_2 + \phi'_2)) \end{aligned} \quad (15)$$

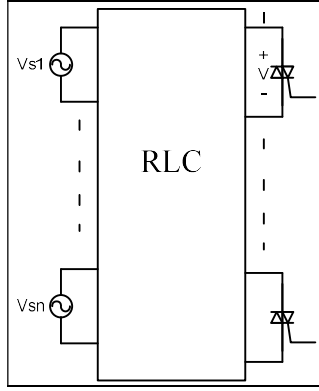
$$\begin{aligned} I'_{1S} &= \frac{-2V'_0}{\pi} (\cos\beta_2 + \cos\beta_1 - \cos\alpha_2 - \cos\alpha_1) + \\ &\frac{V'_1}{\pi} (\pi + \beta_2 + \beta_1 - \alpha_2 - \alpha_1) \cos\phi'_1 + \\ &\frac{V'_1}{2\pi} (\sin(2\alpha_1 + \phi'_1) + \sin(2\alpha_2 + \phi'_1) - \sin(2\beta_1 + \phi'_1) - \sin(2\beta_2 + \phi'_1)) - \\ &\frac{V'_2}{\pi} (\sin(\alpha_1 + \phi'_2) + \sin(\alpha_2 + \phi'_2) - \sin(\beta_1 + \phi'_2) - \sin(\beta_2 + \phi'_2)) + \\ &\frac{V'_2}{3\pi} (\sin(3\alpha_1 + \phi'_2) + \sin(3\alpha_2 + \phi'_2) - \sin(3\beta_1 + \phi'_2) - \sin(3\beta_2 + \phi'_2)) \end{aligned} \quad (16)$$

$$\begin{aligned} I'_{2C} &= \frac{V'_0}{\pi} (\sin 2\beta_2 + \sin 2\beta_1 - \sin 2\alpha_2 - \sin 2\alpha_1) + \\ &\frac{V'_2}{\pi} (\pi + \beta_2 + \beta_1 - \alpha_2 - \alpha_1) \sin\phi'_2 + \\ &\frac{V'_2}{4\pi} (\cos(4\alpha_1 + \phi'_2) + \cos(4\alpha_2 + \phi'_2) - \cos(4\beta_1 + \phi'_2) - \cos(4\beta_2 + \phi'_2)) - \\ &\frac{V'_1}{\pi} (\cos(\alpha_1 + \phi'_1) + \cos(\alpha_2 + \phi'_1) - \cos(\beta_1 + \phi'_1) - \cos(\beta_2 + \phi'_1)) + \\ &\frac{V'_1}{3\pi} (\cos(3\alpha_1 + \phi'_1) + \cos(3\alpha_2 + \phi'_1) - \cos(3\beta_1 + \phi'_1) - \cos(3\beta_2 + \phi'_1)) \end{aligned} \quad (17)$$

$$\begin{aligned} I'_{2S} &= \frac{-V'_0}{\pi} (\cos 2\beta_2 + \cos 2\beta_1 - \cos 2\alpha_2 - \cos 2\alpha_1) + \\ &\frac{V'_2}{\pi} (\pi + \beta_2 + \beta_1 - \alpha_2 - \alpha_1) \cos\phi'_2 + \\ &\frac{V'_2}{4\pi} (\sin(4\alpha_1 + \phi'_2) + \sin(4\alpha_2 + \phi'_2) - \sin(4\beta_1 + \phi'_2) - \sin(4\beta_2 + \phi'_2)) - \\ &\frac{V'_1}{\pi} (\sin(\alpha_1 - \phi'_1) + \sin(\alpha_2 - \phi'_1) - \sin(\beta_1 - \phi'_1) - \sin(\beta_2 - \phi'_1)) + \\ &\frac{V'_1}{3\pi} (\sin(3\alpha_1 + \phi'_1) + \sin(3\alpha_2 + \phi'_1) - \sin(3\beta_1 + \phi'_1) - \sin(3\beta_2 + \phi'_1)) \end{aligned} \quad (18)$$

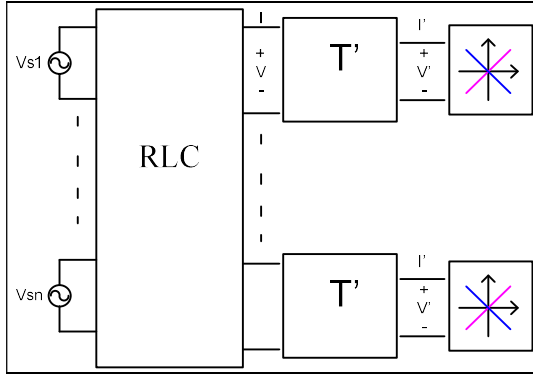
#### 4. Extraction of Converter Overall Model

Here a converter composing number of nonlinear switches and linear elements will be analyzed using the proposed method. The desired converter according to [fig. 6](#) includes passive elements and a number of triacs and voltage and current sources.



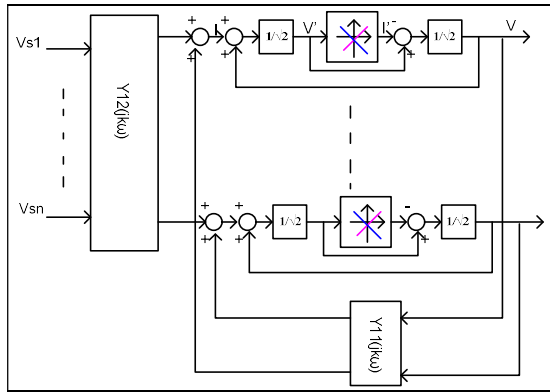
**Fig. 6:** The architecture of the converter with n switches

Using the matrix transformation in (1) and (2), the above circuit will be transformed to [fig. 7](#).



**Fig. 7:** The Equivalent transformed of the converter circuit in [fig. 6](#)

Now, given the admittance seen across the switch Y and inserting the values into the matrix T', the circuit in [fig. 8](#) can be derived.



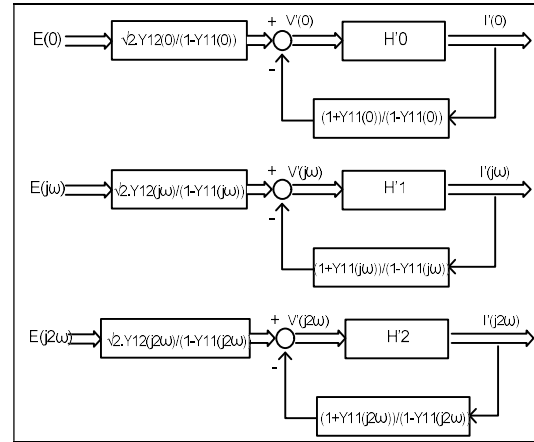
**Fig. 8:** The System Block Diagram of the Converter in [fig. 6](#)

The computations will be done only for the first three expressions of the current and voltage because computation for higher order expressions is time-consuming and complicated in one hand, and their

values will not impact the solutions significantly, on the other. In (19), the transfer function of current to voltage is denoted by H'.

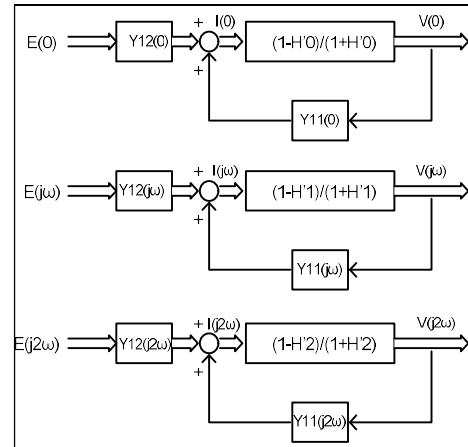
$$H'_0 = \frac{I'_0}{V'_0} ; H'_1 = \frac{I'_1.e^{j\psi'_1}}{V'_1.e^{j\phi'_1}} ; H'_2 = \frac{I'_2.e^{j\psi'_2}}{V'_2.e^{j\phi'_2}} \quad (19)$$

With the insertion of (19) into (8), the voltage and current harmonics for each switch are calculated and the system block diagram for the components is depicted as in [fig. 9](#). In this block diagram, where the output I' is in terms of the variables V' and E, the parameter E is the harmonic component of the voltage source. By expanding the transformation matrix T as in (2) and adopting a process as in [fig. 9](#), the block of [fig. 10](#) can be derived in terms of I-V.



**Fig. 9:** The Block Diagram of each component in Terms of I'-V'

This block diagram encompasses recursive loop which is used for numerical calculation of harmonic components while it can be expanded for larger n.



**Fig. 10:** The Block Diagram of each component in terms of I-V

The block diagrams shown in fig. 9 and fig. 10 are recursive function for numerical calculation of the harmonic components within the I'-V' or I-V spaces. Through enough iteration of the computational loop of the block diagrams 9 and 10, acceptable precision for each component is attainable. The recursive function in the I'-V' space is expressed in (20).

$$C_{11}(jn\omega) = \frac{1 + Y_{11}(jn\omega)}{1 - Y_{11}(jn\omega)} ; C_{12}(jn\omega) = \frac{\sqrt{2} Y_{12}(jn\omega)}{1 - Y_{11}(jn\omega)} \quad (20)$$

The recursive function used for harmonic calculation and increasing the precision using function H is described in (21) as follows.

$$I'_n(\kappa) = H'_n(\kappa) \cdot V'_n(\kappa) \quad (21)$$

$$V'_n(\kappa + 1) = -C_{11}(jn\omega) \cdot I'_n(\kappa) + C_{12}(jn\omega) \cdot E(jn\omega)$$

## 5. Proposing the Modeling Flowchart and a Typical Converter

In this section, the operating computational flowchart described before will be presented. Then, using a typical converter circuit, the results of the proposed method will be illustrated using computer simulation. The simulations of the proposed model and the corresponding circuit are, respectively, performed within the MATLAB and SPICE software packages. Fig. 11 shows the typical circuit here.

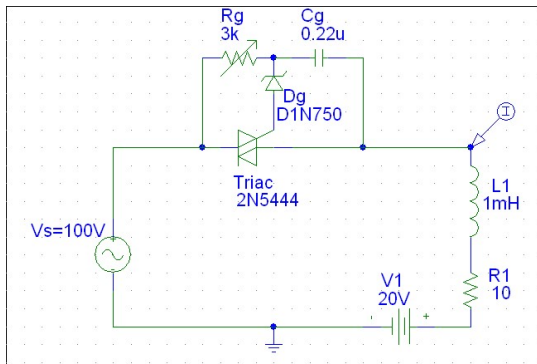


Fig. 11: The Typical Converter Circuit

The results of modeling methods and related simulations are given in table I, where it can be seen that the highest error is lower than 5%. The small difference of the results obtained through two methods given in table 1 is caused by the idealization of the I-V curve. Fig. 13 shows flowchart of the proposed method.

Table 1: Comparison of the Results of the Proposed Method

Simulation	Modeling	Converter Characteristics
$\alpha_1=072^\circ$	$\alpha_1=072^\circ$	Firing Angles
$\alpha_2=213^\circ$	$\alpha_2=213^\circ$	
$\beta_1=170^\circ$	$\beta_1=165^\circ$	Extinction Angles
$\beta_2=372^\circ$	$\beta_2=366^\circ$	
$I_0=2.2A$	$I_0=2.1A$	Current Components
$I_1=8.6A$	$I_1=8.3A$	
$I_2=1.3A$	$I_2=1.2A$	

Fig. 12 depicts the amplitude of the input harmonics.

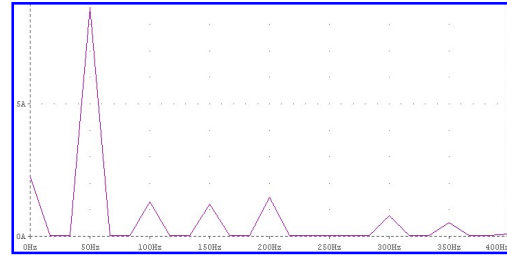


Fig. 12: The Amplitude of the Converter's Input Harmonics

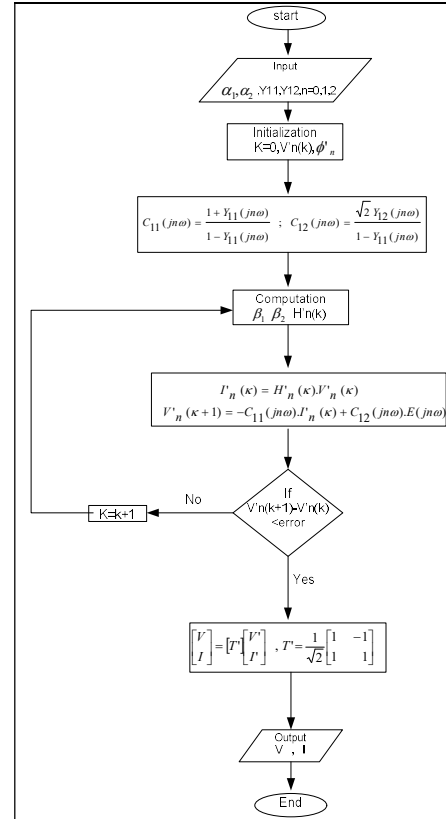


Fig. 13: Flowchart of the Proposed Modeling Method

Fig. 14 shows the voltage across the converter's load.

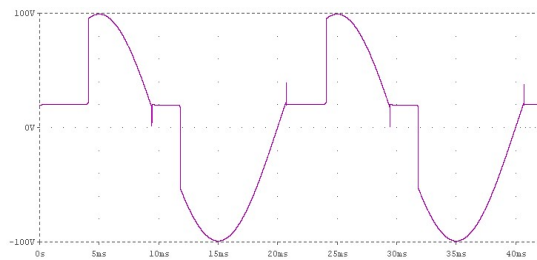


Fig. 14: Voltage across the Converter Output

Fig. 15 illustrates the current of the converter output which does not show any voltage spike due to the inductive load.

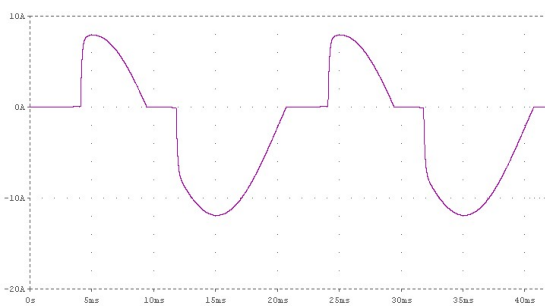


Fig. 15: Load Current of the converter output

## 6. Conclusion

In this paper, a numerical recursive method has been proposed to modeling the switches in line commutated converters. The proposed approach has high speed and precision; in addition, it can be combined with the computational algorithms included in circuit simulators so that convergence of the computational loop can be obtained within the minimum possible time. Results of the simulation along with their comparison with those of modeling are verifying these advantages. Values of the error in the results of the suggested method with respect to the actual ones are less than 5%. The method can be generalized for harmonic computation of higher orders too. It has been assumed that all the devices other than switches are linear. Since characteristic curve of such devices as diode, diac, thyristor, triac are similar to each other, thus the proposed method can be applied to a vast range of converter configurations. It should be noted that part of the ultimate error is resulted from the ideal assumption of the switch characteristic curve; this can be decreased using parasitic elements of the switch accordingly.

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