Research article

Dynamic model of static synchronous compensator in Single-Machine Infinite-Bus power system

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Abstract

Electric loads such as electric arc furnaces, and heavy industrial plants can produce or absorb reactive power. Due to the instantaneous change of loads, the reactive power balance is essential in a power system. Static synchronous compensator (STATCOM) is usually used to control the reactive power. By controlling the reactive power absorbed or injected into the power system, it makes the voltage at the point of connection to the grid. This compensator is used in two stable operating modes, inductive (lag) and capacitive (leading), to improve the performance of the power system. In this paper, a single-machine power system with shunt compensator is considered and the aim is to determine the relationship between voltage and current between the compensator and the transmission line. An approximate model is considered for the compensator, where the compensator current plays the main role. Then, using the analysis of algebraic equations, the voltage in the compensator for different modes.

Keywords: Modelling, Shunt device, Static synchronous compensator

1-Introduction

The rapid development of power electronics and the construction of high-power semiconductors have provided amazing possibilities for the development of new equipment in the field of power system compensators [1,2]. So far, many control tools have been designed and completed under the name of flexible alternating current transmission systems (FACTS) technology for transmission and distribution networks [3, 4]. FACTS devices are divided into two groups based on the mode of operation, devices based on reactive impedance and devices based on voltage source [5,6]. In another division, flexible ac transmission systems are divided into three groups of thyristor-controlled FACTS devices, FAC-TS devices based on voltage source converters, and hybrid devices. In terms of connection type, FACTS controllers, according to Fig. 1 are divided into four types [7,8], a) series controller such as thyristor controlled series capacitor (TCSC) [9,10] and synchronous static series compensator (SSSC) [11,12], b) shunt controller such as static variable compensator (SVC) [13,14] and static synchronous compensator (ST-ATCOM) [15,16], c) series-series controller such as inter-line power flow controller (IPFC) [17,18] and adjustment thyristor controlled phase angle controller (TCPAR) [19] and d) series-parallel controller such as uniform power distribution controller (UPFC) are divided [20,21].



Fig. 1 Classification of FACTS devices

From the use of FACTS devices, we can mention the control of load distribution and minimizing the losses of transmission lines, increasing dynamic stability, strengthening transient stability, reliability or security, improving power quality and improving voltage profile [22,23,24].

Various studies have been presented on the application of STATCOM to improve the performance of power systems, such as ferroresonance overvoltage mitigation in grid-connected wind energy conversion systems [25], mitigate resonance in wind farms [26], power oscillation damping in PV solar system [27], reactive power compensation [28] and transient stability enhancement in distribution system with wind farms [29].

A static synchronous compensator along with a variable frequency drive for voltage and frequency control of a small-hydro turbine driven self-excited induction generator system is proposed in [30], in which a control algorithm based on adaptive noise cancellation filter is used for STATCOM control.

A comprehensive review of various techniques employed to enhance the low voltage ride-through capability of the fixed-speed induction generators- based wind turbines is presented in [31], which, based on the simulated results, series connection dynamic voltage restorer and shunt connection static synchronous compensators are the highly efficient low voltage ride through capability enhancement approaches.

To control the controllers and clarify the objectives, the nonlinear controller is proposed in [32] as an alternative to the traditional STATCOM controller in a wind farm equipped with a double-fed induction generator (DFIG). So that the reactive power required to stabilize the wind farm

equipped with DFIG is considered when a fault occurs.

The integration of a STATCOM in a wind park (WP)-based DFIG is presented in [33], and the effect of the STATCOM on the high voltage ride-through (HVRT) capability of the WP is analyzed. In this study, the size of the STATCOM is selected based on the network code to control the power factor and different wind turbine and medium voltage feeder outage scenarios. Finally, the simulation results show the use of STATCOM to significantly improve the HVRT WP capability.

This paper presents the single-machine infinite-bus (SMIB) power system model with a compensator. In this model, the compensator is represented by a current source. The algebraic equations of the power system have been analyzed by ignoring the resistance of the transmission line. The simulation results are obtained and shown in MATLAB software using equations.

2- Static Synchronous Compensator

The static synchronous compensator is a power electronic converter designed to be shunt-connected with the grid to compensate for reactive power [34, 35].

STATCOM has the following components: A voltage source converter (VSC), dc capacitor, inductive reactance and harmonic filter [36]. By controlling the reactive power absorbed or injected into the power system through the VSC, the STATCOM performs voltage regulation at its connection point [37, 38]. Harmonic filter attenuates the harmonics and other high frequency components due to the VSC [39,40]. А simplified diagram of STATCOM is shown in Fig. 2. The operation of STATCOM can be classified

into two modes: voltage regulation mode and VAR control mode (Fig. 3).



Fig. 2 Compensator structure schematic



Fig. 3 Compensating performance area

3- Power System with Compensator

A single-machine system connected to an infinite bus with shunt compensator is shown in Fig. 4, where the generator bus voltage is U_T , the infinite bus voltage is U_B and the compensating bus voltage is U_M. Also, the terminal current of the generator I_T and compensating current I_s being considered. The length of the line is "a" and " λ " is a parameter between 0 and 1, and it represents the ratio of the compensator distance from the generator terminal to the total length of the line. The impedance between the generator bus and the compensator bus and the compensator bus with the infinite bus are respectively based on the location of the compensator regardless of the capacitance of the transmission line R_1+jX_1 and R_2+jX_2 .



Fig. 4 Single-machine system connected to infinite bus with shunt compensator

4- System Equations

The compensating equivalent circuit is considered equivalent to the controllable reactive current source according to Fig. 5. The output current can be controlled separately in both capacitive and capacitive ranges. According to the voltage converter in the compensator, the compensator current is post-phase or pre-phase Due to the bus voltage.

Based on the relationship between voltage (KVL) and current (KCL) in the transmission line, the compensating bus voltage is:

$$\bar{U}_{M} = \frac{X_{2}}{X_{T}}\bar{U}_{T} + j\frac{X_{1}X_{2}}{X_{T}}\bar{I}_{S} + \frac{X_{1}}{X_{T}}\bar{U}_{B}$$
(1)

In the following, the analysis of system equations is expressed in two frameworks, and the compensatory behavior is simulated using it.



Fig. 5 Compensating equivalent circuit in power system transmission line

A- Analysis in two-axis dq framework

The angle between compensating bus voltage and "q" axis is considered θ .

 i_{sd} and i_{sq} are the compensating current components and U_{Bd} and U_{Bq} are compen-

sating bus voltage components in dq axis framework.

a) Generator terminal current components According to the relationship between generator terminal voltage components u_d and u_q and generator terminal current components i_d and i_q , and also according to the definition of biaxial components of infinite bus voltage and compensating current, the terminal current components Generators include:

$$\begin{aligned} &\left(i_{d} = \frac{E_{q}^{'} - X_{2} I_{s} \cos\theta - U_{B} \cos\delta}{X_{1} + X_{2} + X_{d}^{'}} \\ &i_{q} = \frac{X_{2} I_{s} \sin\theta + U_{B} \sin\delta}{X_{1} + X_{2} + X_{q}} \end{aligned}$$

$$\end{aligned}$$

$$(2)$$

b) Compensating bus voltage components Using the generator terminal current components, we have:

$$\begin{cases} (X_{1} + X_{q}) U_{B} \sin \delta \\ U_{Md} = \frac{+(X_{1} + X_{q}) X_{2} I_{S} \sin \theta}{X_{1} + X_{2} + X_{q}} \\ X_{2} E_{q}^{'} + (X_{1} + X_{d}^{'}) U_{B} \cos \delta \\ U_{Mq} = \frac{+(X_{1} + X_{d}^{'}) X_{2} I_{S} \cos \theta}{X_{1} + X_{2} + X_{d}^{'}} \end{cases}$$
(3)

c) Compensating bus voltage angle

Using compensating bus voltage components in dq biaxial device, we have:

$$tg\theta = \frac{U_{Md}}{U_{Mq}} = \frac{X_1 + X_2 + X_d}{X_1 + X_2 + X_q}$$
$$\frac{(X_1 + X_q)(U_B \sin \delta + X_2 I_S \sin \theta)}{X_2 E_q^{'} + (X_1 + X_d^{'})(U_B \cos \delta + X_2 I_S \cos \theta)}$$
(4)

d) Active power of the generator

Based on the definition of the mixed power of the generator, the active power is equal to:

$$P_{E} = \frac{U_{M}^{2}}{2} \frac{X_{d}^{2} - X_{q}}{(X_{1} + X_{d}^{2})(X_{1} + X_{q})} \sin 2\theta + \frac{E_{q}^{2}U_{M}}{(X_{1} + X_{d}^{2})} \sin \theta$$
(5)

B- Analysis in two-axis xy framework

The compensating reactive current in capacitive mode is:

$$\bar{I}_{S} = I_{S} e^{j(\delta_{M} - 90)} \tag{6}$$

So the components are:

$$\begin{cases} i_{Sx} = I_S \sin \delta_M \\ i_{Sy} = I_S \cos \delta_M \end{cases}$$
(7)

a) voltage magnitude of compensating bus The magnitude of compensating bus voltage components is:

$$\begin{cases} U_{Mx} = \frac{X_2}{X_T} U_x + \frac{X_1 X_2}{X_T} I_S \cos \delta_M + \frac{X_1}{X_T} U_B \\ U_{My} = \frac{X_2}{X_T} U_y + \frac{X_1 X_2}{X_T} I_S \sin \delta_M \end{cases}$$
(8)

Therefore, the magnitude and phase of the compensating bus voltage is equal to:

$$\delta_{\rm M} = tg^{-1} \left(\frac{X_2 U_{\rm T} \sin \delta_{\rm T}}{X_2 U_{\rm T} \cos \delta_{\rm T} + X_1 U_{\rm B}} \right)$$

$$X_1 X_2 I_{\rm S} + X_2 U_{\rm T} \cos(\delta_{\rm T} - \delta_{\rm M})$$
(9)

$$U_{\rm M} = \frac{+X_{\rm I} U_{\rm B} \cos \delta_{\rm M}}{X_{\rm T}}$$
(10)

As found, the compensating current has an effect on the magnitude and phase of the compensating bus voltage. The magnitude of the compensating bus voltage can be expressed as follows:

$$U_{M} = \frac{1}{X_{T}} \sqrt{(X_{1}U_{B})^{2} + (X_{2}U_{T})^{2} + 2X_{1}X_{2}U_{T}U_{B}\cos\delta_{T}} + \frac{X_{1}X_{2}}{X_{T}}I_{S}$$
 (11)

The first component is the bus voltage M without the compensating effect, and the second component shows the compensating effect on the voltage magnitude.

b) Voltage angle of the generator bus

According to the voltage components of the generator terminal in the xy framework, the voltage angle in the generator bus is equal to:

$$\delta_{\rm T} = tg^{-1} [\frac{[X_{\rm T}U_{\rm M} - X_{\rm I}X_{\rm 2}I_{\rm S}]\sin\delta_{\rm M}}{[X_{\rm T}U_{\rm M} - X_{\rm I}X_{\rm 2}I_{\rm S}]\cos\delta_{\rm M} - X_{\rm I}U_{\rm B}}] \quad (12)$$

c) Generator Active and reactive powers

Based on the mixed power in the terminal bus of the generator, the active and reactive powers of the generator are equal to:

$$P_{\rm E} = \frac{U_{\rm T} U_{\rm B}}{X_{\rm T}} \sin(\delta_{\rm T}) + \frac{X_2 U_{\rm T}}{X_{\rm T}} I_{\rm S} \sin(\delta_{\rm T} - \delta_{\rm M})$$
(13)

$$Q_{E} = \frac{U_{T}^{2}}{X_{T}} - \frac{U_{T}U_{B}}{X_{T}} \cos \delta_{T} - \frac{X_{2}U_{T}}{X_{T}} I_{S} \cos(\delta_{T} - \delta_{M})$$
(14)

Therefore, the active power consists of two components, the first component is related to the time when there is no compensator, and the second component shows the effect of the compensator, which is a function of the compensator current.

d) Compensating bus voltage angle

The compensating bus voltage phase can be determined according to the output power. Because the transmission line losses are zero, the active power produced by the generator is equal to the active power delivered to the infinite bus. The phase angle of the compensating bus voltage is independent of the compensating current, and the compensating current cannot change the voltage angle in the M bus. The compensating bus angle is:

$$\delta_{\rm M} = tg^{-1} \left(\frac{X_2 U_{\rm T} \sin \delta_{\rm T}}{X_2 U_{\rm T} \cos \delta_{\rm T} + X_1 U_{\rm B}} \right) \tag{15}$$

5- Simulation results

In this section, based on the relationships expressed in MATLAB software, the simulation results of compensatory behavior are presented.

Figs. 6 and 7 show the changes in active and reactive power at the generator terminal.



Fig. 6 Active power changes at the generator terminal according to the voltage angle of the generator terminal



Fig. 7 Reactive power changes at the generator terminal according to the voltage angle of the generator terminal

Figs. 8 and 9 show changes in compensating bus voltage and compensating reactive power according to the generator terminal voltage angle. The above results have been obtained for three cases without compensator (zero compensator current is assumed), maximum and minimum compensator current.

The simulation results show that in the maximum state of the compensating current, the maximum active power value has increased, and it improves the system's stability against possible changes. Fig. 10 shows the effect of compensating current on compensating output power.



Fig. 8 Compensatory reactive power changes according to generator terminal voltage angle



Fig. 9 Variations of compensating bus voltage according to generator terminal voltage angle



Fig. 10 Effect of compensating current on output power

6- Conclusion

Using STATCOM at the appropriate point or points in the power system improves the ability to transfer power to loads, which is done in different network conditions by increasing voltage stability and setting a smooth voltage profile. This paper presents the power system model equipped with a compensator. Then, using the analysis of algebraic equations in two devices, voltage and current changes and electric power, have been shown. As the results show, the system characteristics can be improved with the current source controlled by the compensator.

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