



Predicting the Next State of Traffic by Data Mining Classification Techniques

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Abstract

Traffic prediction systems can play an essential role in intelligent transportation systems (ITS). Prediction and patterns comprehensibility of traffic characteristic parameters such as average speed, flow, and travel time could be beneficiary both in advanced traveler information systems (ATIS) and in ITS traffic control systems. However, due to their complex nonlinear patterns, these systems are burdensome. In this paper, we have applied some supervised data mining techniques (i.e. Classification Tree, Random Forest, Naïve Bayesian and CN2) to predict the next state of Traffic by a categorical traffic variable (level of service (LOS)) in different short-time intervals and also produce simple and easy handling if-then rules to reveal road facility characteristic. The analytical results show prediction accuracy of 80% on average by using methods.

Keywords: Traffic prediction, Level of Service Prediction, Data Mining, Naïve Bayesian, Random forest, Classification tree, CN2

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1. Introduction

Traffic state prediction has an important role in intelligent transportation systems (ITS). It can be classified into short-term prediction which predict traffic state changes in short periods (e.g. 15 min or 30 min) and long-term prediction for monthly or yearly traffic state information [1]. Short-term predictions either may be used directly by traffic experts to take relevant actions or could be injected as inputs to proactive congestion management approaches. These approaches could include route guidance, dynamic congestion pricing, variable speed limit systems. The long-term predictions can be used for transportation planning. Although traffic prediction method studies usually use a measure of algorithm performance based only on predictive accuracy, it is accepted by many researchers and practitioners that, in many application domains, the comprehensibility of the knowledge (or patterns) discovered by an algorithm is another important

evaluation criterion. For example, the pattern discovered by this algorithm is used to support a decision that will be made by a human user, rather than for automated decision-making. Therefore, an ideal method is one that covers both application aspects.

Lili et al [28] specify three factors that affect the quality of the predicted real-time traffic information. These factors include: (1) Variability in the quality of real-time data from different sources (sensors or other road facilities). (2) Dynamic nature of real-time traffic conditions, which cause delay between the time data, is collected and is used. (3) Randomness and stochastic inherent of traffic networks which appear in supply, demand, and performance of the traffic network. For these reasons, they conclude that predicting short-term traffic conditions is more meaningful.

Besides short-term and long-term predictions classes, there exist various classification standards that categorize traffic prediction methods such as

single link or transportation network, freeways or urban streets, univariate or multivariate, physical models or mathematical methodologies, etc [49]. Applying statistical methodology, prediction methods are divided into two main categories:

(1) Parametric method which includes linear and nonlinear regression ([48], [45], [44]) filtering techniques ([43], [46]) autoregressive moving average family (ARMA/ARIMA/SARIMA) [32]. These techniques try to detect a function between the past information and the predicted state. However, they are typically sensitive to errors and data quality.

(2) Non-parametric method such as Neural Networks (Feed-Forward Neural Network (FFNN) [50], Radial Basis Function Neural Networks (RBF-NN) ([34], etc.), Bayesian networks [20], K-Nearest Neighbor (KNN) Algorithms [41], Support Vector Regression (SVR) ([10], [24]). This kind of techniques can generally handle imprecise data and as a result, usually perform well in treating the nondeterministic, complex and nonlinear systems.

Up to now, several approaches (usually by utilizing unsupervised algorithms) consider prediction of continuous traffic parameters: flow, travel time, etc. ([13], [28], [12], [41]). In this paper, we predict short-term level of service (LOS) of a highway section by using supervised learning algorithms and also propose representations of classification models in terms of if-then rule sets which can give the comprehensibility of the knowledge (or patterns) discovered by a classification algorithm. In following, we describe some motivations for prediction of this traffic state categorical variable:

Traffic patterns and driver behavior in different times and traffic states (e.g. free-flow, stable or synchronized flow, congested flow and flow near to jam density) is quite different [9]. This phenomena cause some problem for traffic simulation models to capture characteristics of traffic flow. For example analytical functions that is used to describe the relationship between flow and density (fundamental diagram) fails to satisfy all of the desirable properties so that the traffic simulation models that use these functions as input model parameters will deteriorate and only make a reasonable prediction in relatively short time scale [27]. One of the key applications of categorically traffic state prediction can be setting specific boundary conditions and calibration parameters for simulation models, or fitting separate functions (to describe fundamental diagrams) for each LOS, and then using them according to the predicted LOS in advance. This method can increase accuracy of macroscopic simulation models which has broad usage in ITS proactive controller ([33], [22], [19]).

Classification prediction methods which have been used in this study for prediction, also produce simple and easy handling if-then rules that can be used in designing expert systems, scheming decision tree of a traffic controller system with very light computation (such as Variable Speed Limit system [2]). However, in addition to controller system traffic experts also could mine these simple produced IF-THEN rules to find performance quality of road, facility characteristics and propose optimal speed for that section or detect any failure in the specified state.

Classification methods such as Naïve Bayesian can also offer a valuable insight into the structure of the training data and effects of each attributes of traffic state and providing traffic engineers with a comprehensible explaining the system's predictions. Which guide them by interpretation traffic state occurring, recognition important attribute and reasons for and using this information to off line network planning.

The rest of the paper is organized as follows: Section 2 describes the model-learning framework, brief description of each classification learner and setting parameters and heuristic, which is used in the learning process. Section 3 presents the results and discusses the experiments performed and finally the conclusion is presented in section 4.

2. Proposed Approach

Data mining proposes varieties knowledge discovery methods. These methods include classification and prediction, and presenting the mining results using visualization tools. The term prediction denotes to both numeric prediction and class label prediction.

In particular, a classification problem aims to generate (to learn) a model, called classifiers, which is able to predict the value of a categorical target variable (class labels) based on several input variables (sometimes called predictor variables, fields, attributes or features). This model actually is a function that maps an input attribute vector X from attributes space to output class label $Y \in \{C_1, C_2, \dots, C_k\}$. Before learning the model, the class labels and the values of the attributes for each record (observation, instance or example) must be known. Data in a labeled training set comes in records of the form:

$$(X, Y) = ((x_1, x_2, x_3, \dots, x_n), Y) \quad (1)$$

The dependent variable (class labels) Y is the target variable that we are trying to predict (understand, classify or generalize) and the

vector X is composed of the attributes $x_1, x_2, x_3, \dots, x_n$.

In this study, we have tested four famous data mining classification algorithm, i.e. Classification tree, Random Forest, Naïve Bayesian and CN2, which are widely utilized in artificial intelligence. In addition to this method, we tested support vector machine for prediction but it did not show good enough accuracy so we left it out from our study, this result match with previous Chen and et al [12] study.

In our application, first, the reliable data are gathered, then the days with missing or error record was omitted after that, traffic parameters of each time interval extracted from data. We learn the predictive model of extracted training set comes in the records include Flow (veh/15 min), Density (veh/km), Speed (km/h), Time Duration (start time of interval in min) as the attributes for different time intervals (of 10, 15, and 30 minutes). LOS of the next time interval is considered as class label or the target variable of it. For example the record form of time interval one ($t=1$) is in the form of (2).

$$(Flow_1, Speed_1, Density_1, TimeDuration_1, LOS_2) \quad (2)$$

In fact, this prediction framework is independence of current traffic's state. The keynote has laid down on learning offline prediction models with traffic's history data and using it to preform prediction based on classification current data. This ability makes it robust to handle given noisy data or data with missing values.

The reminder of this Section will present a brief description of well-known classification methods, their logical sequence of the prediction method and specific modification of them that we have used in this paper.

2.1. Classification Tree

Decision Tree is a convenient, nonparametric and widely used learning approach in data mining as a classifier. Classification and Regression tree [7] are two main types of Decision trees. Classification tree used when the value of predicted item is a class and Regression tree is utilized when predicted item have a real number.

Decision Tree is a directed rooted tree of nodes and connecting branches. Nodes indicate decision points, chance events, or branch terminals, which correspond to one of the input variables. Branches correspond to each possible value of that input variable or event outcome emerging from a node. Each leaf represents a value of the target variable. When Decision Tree receives a new data, a passing through nodes of it, determine the next state of traffic and will give new instance's target variable. Each

path from the root of a decision tree to one of its leaves results a rule.

This tree model is usually learned top-down by recursively partitioning [16] the instance space (The set of all possible observations which equals to the training set in learning phase). At each node, a predictor variable select to split the set so that the created partitions have similar target variable value. The selection criteria for choosing variable defined as how homogeneous the resulted partitions are. Different algorithms use various selection criteria e.g., Gini index [7], Information Gain [36], Likelihood-Ratio Chi Squared Statistics [4], etc. These selection criteria can be grouped according to the source of them such as information theory, dependence, and distance [5] or according to the measure structure: impurity based criteria, normalized impurity based criteria and binary criteria [39]. This process continues until no partitions gain a sufficient splitting criterion measure or meets one or more stopping criteria. For example, all cases put into a similar target variable partition or the tree reaches the specified maximum depth. This phase of learning the decision tree called Growing phase. Exploiting loosely stopping criteria tends to generate large decision trees. To handle this situation some algorithm utilized pruning phase suggested in [7]. This phase transforms large decision trees to smaller one by cutting some sub-branches that absent of them does not make big accuracy change and the tree model keep its sufficient generalization exactness.

Algorithms that generate a decision are called decision tree inducers. Various decision trees inducers exist such as ID3 [35], C4.5 [37], CART [7], CHAID [25], QUEST [29].

In our application, we select Information Gain, which will be explained in following subsection, in the role of selection criterion for the learner. Pruning during induction is based on the minimal number of two instances in leaves i.e. the algorithm does not construct a split, which would put less than two of training examples in any of the branches. Since target variable (LOS) value is a class then the resulted decision tree is a classification tree (Fig.2).

2.1.1. Information Gain

This measure is based on information theory, which indicates required information to classify a given record of data. The expected information to encode possible class label Y of an arbitrary record of a training set in bits is given by (3).

$$H(Y) = -\sum_{i=1}^k P(Y = C_i) \log_2(P(Y = C_i)) \quad (3)$$

Where $P(Y = C_i)$ is the nonzero probability that the record belongs to a class C_i . A log function to the base two is used, because the information is

encoded in bits. $H(Y)$ is also known as the entropy of the data. This parameter gets a high value if class label Y has uniform distribution in training set and low value if its distribution varies. The conditional entropy $H(Y|x_a)$ is the expected information required to classify a record based on some known attribute x_a :

$$H(Y|x_a) = -\sum_{u \in \text{val}(x_a)} P(x_a = u)H(Y|x_a = u) \quad (4)$$

Information gain is defined as the difference between the original information requirement (3) and the new requirement after obtaining the value of x_a (4). That is

$$I(x_a) = H(Y) - H(Y|x_a) \quad (5)$$

In other words, $I(x_a)$ reveal how much information would be gained by splitting on x_a . We like to do splitting on the attribute that would produce partitions that are more pure and the amount of information still required to finish classifying their records is minimal. Therefore, it is sufficient to choose the attribute with the highest information gain and using it as a splitting attribute on the current node in Decision Tree.

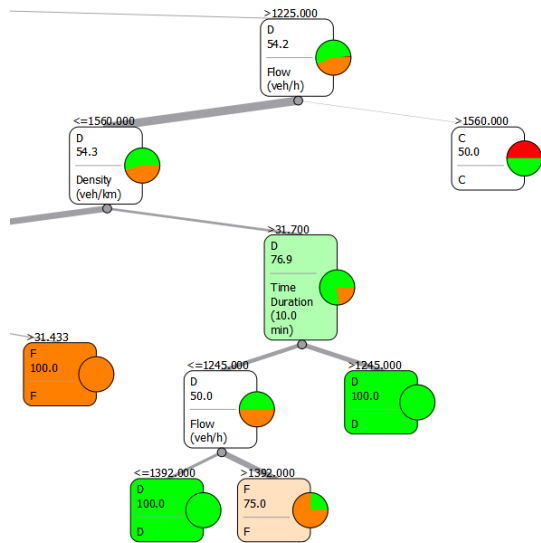


Fig.2. A portion of the resulted classification tree, the color of the node report on the probability of the majority class (Majority class probability) that the color intensity would be higher towards the leaves of the node

2.2. Random Forest

Random forest method, proposed firstly by Leo Brieman [8], builds ensemble or committee of decision trees (classification or regression trees) with given the set of class-labeled data and aggregate results of them for prediction. For inducing each individual tree, the algorithm utilizes bagging idea

[6] and the random selection [17] of features, introduced independently by Ho [23] and Amit and Geman [3].

Similar to bagging, the algorithm grows each individual tree from a bootstrap sample (with the same size, drawn randomly with replacement) or a subsample (with smaller size, drawn randomly without replacement) of the training data. Another technique that Random forest uses to develop trees, that are even more diverse, is the random variable selection. It draws an arbitrary subset of variable from which the best variable is selected for the split. Originally, Brieman [8] proposed to grow the trees without any pruning. Its final prediction is the mean prediction (regression) or class with maximum votes (classification) of the decision trees.

Let N_{trees} be the number of trees and M_{try} the number of predictor variable drawn at each node. In case of traffic state application, we set $N_{trees} = 4$ classification trees to be included in the forest and $M_{try} = 2$ for splitting consideration at each node. As the stopping condition, minimal number five of instances in the node before splitting was set.

2.3. Naïve Bayesian

Naïve Bayesian is statistical classifier that determines class membership probabilities of a given sample for each class $P(Y = C_m|X)$, $m \in \{1, \dots, k\}$. Naïve Bayesian classifier is based on "naive" class-conditional independence assumption and Bayes' theorem. Class-conditional independence implies that the probability distribution of an attribute value of a given class is independent of the values of the other attributes. Naïve assumption allows us to estimate each distribution independently as a one-dimensional distribution rather than computation-intensive joint distribution.

$$P(x_i|C_m, x_j) = P(x_i|C_m), \quad i \neq j \quad (6)$$

According to Bayes' theorem, the posterior probability of class $Y = C_i$ conditioned on attribute vector X expresses in terms of the marginal (evidence) probability $P(X)$, the prior probability (probability of hypothesis $Y = C_i$ before seeing any data X) $P(Y = C_i)$ and the likelihood probability (probability of the data X if the hypothesis $Y = C_i$ is true) $P(X|Y = C_i)$ as (7).

$$P(Y = C_m|X) = \frac{P(Y=C_m)P(X|Y=C_m)}{P(X)} \quad (7)$$

The numerator of (7) transforms to the joint distribution probability $P(Y = C_m, X)$ which by n times applying chain can be described in terms of conditional probabilities equation (8).

$$P(C_m) \times P(x_1|C_m) \times P(x_2|C_m, x_1) \times P(x_3|C_m, x_1, x_2) \times \dots \times P(x_n|C_m, x_1, x_2, \dots, x_{n-1}) \quad (8)$$

And by using Naïve assumption of (6), this equation expressed as

$$P(C_m) \times P(x_1|C_m) \times P(x_2|C_m) \times P(x_3|C_m) \times \dots \times P(x_n|C_m) = P(C_m) \times \prod_{i=1}^n P(x_i|C_m) \quad (9)$$

When a new record of attribute values $X = (x_1 = u_1, x_2 = u_2, x_3 = u_3, \dots, x_n = u_n)$ come, the classifier predicts the value of Y the class C_m makes having the highest posterior probability $P(Y = C_m|X)$. This is known as the maximum a posteriori (MAP) decision rule. Therefore, since the numerator of (7) does not depend on C_m and by using equation (9) the Naïve Bayesian classifier is a function which defined as:

$$\hat{Y}(X) = \text{Arg}_{C_m} \max(P(C_m) \times \prod_{i=1}^n P(x_i|C_m)) \quad (10)$$

The parameters of a naive Bayes model i.e. the class prior probabilities $P(Y = C_m)$ and the posterior probability $P(x_i|Y = C_m)$. They can be estimated from data by maximum-likelihood estimation (MLE). Given the training data, the class prior probabilities may be simply estimated by the relative frequency (number of samples in the class) / (total number of samples)). To compute $P(x_i|Y = C_m)$ one must assume a distribution or generate nonparametric models for the attribute. The typical approach in two following situations is [21]:

1. If x_i is categorical then $P(x_i|Y = C_m)$ can be estimated by the relative frequency.
2. If x_i is continuous-valued then it assume that $P(x_i|Y = C_m)$ have Normal (Gaussian distribution), calculate the mean μ_{C_m} and standard deviation σ_{C_m} of the attribute values x_i for training samples in the class C_m and substitute them into Gaussian distribution formula (11).

$$P(x_i|Y = C_m) = \frac{1}{\sqrt{2\pi}\sigma_{C_m}} e^{-\frac{(x-\mu_{C_m})^2}{2\sigma_{C_m}^2}} \quad (11)$$

Depending on the precise nature of the probability model, naive Bayes classifiers can be trained very efficiently in a supervised learning setting. In many practical applications, parameter estimation for naive Bayes models uses the method of maximum likelihood; in other words, one can work with the naive Bayes model without believing in Bayesian probability or using any Bayesian methods.

In our traffic state prediction, we also used Laplace estimator [11] in probability estimation of prior and conditional probability. It avoids subsequent problem in the situation when there is no training sample for the specific class. This situation

would return a zero probability and would cancel the effects of all the other (posterior) probabilities involved in the product (9) Laplace estimator assumes that the training data is so large and simply add one to each count that is needed to estimate probabilities.

2.4. CN2

Beside decision tree, a second way to generate if-then rules is to use rule induction algorithms, which search for propositional rules directly from the training data. CN2 [15] is one the most famous example of this type of approach. It has two main procedures:

On upper level it runs a sequential covering strategy (also known as separate-and-conquer or cover-and-remove), first employed by the AQ Algorithm [30]. This process sequentially extracts rule from the training set by calling the lower level procedure (conquer step), and remove data records that are covered by the rule (separate step). It continues this routine until no more efficient rules be discovered. In addition to this exclusive covering strategy, as in the original CN2 is used [15], Alternative type of covering is weighted covering, which only decreases the weight of covered records instead of removing them[26].

On the lower level, a beam search method is done. Beam search start with an empty rule (no conditions on its if-part) and iteratively specialize it, evaluates the extended rules created by the specialization operation, and keep the b best-extended rules (Beam width). This process is repeated until a stopping criterion is satisfied. In this process, rule evaluation is done with the aim of heuristic functions that consider coverage (number of records covered by a rule) and accuracy during the process of building a rule. Taking inspiration from ID3, original CN2 uses entropy (1) as the rule evaluation function but Clark and Boswell [14] present the Laplace estimation as an alternative rule quality measure to overcome undesirable “downward bias” of entropy and it is defined in Equation (12).

$$\text{laplaceEstimation}(R) = \frac{p+1}{p+n+k} \quad (12)$$

In the formula (12), P represent the number of positive examples covered by a rule R in the training set, n is the number of negative examples covered by a rule R and k is the number of classes available in the training set. In addition to these functions there is many others like m-estimate of probability [18] and WRACC (weighted CN2-SD algorithm), used in CN2-SD algorithm [26].

In addition to the evaluation function, CN2 uses a statistical significance test to ensure the new rule

reflects a true correlation between attributes and classes, and is not due to chance. Actually, it is pre-pruning method, which avoids generating too specific rule. It applies the likelihood ratio statistic test (LRS) to compare the observed class distribution among examples satisfying the rule with the class distribution result if the rule had selected examples randomly. The user determines required significance level of a rule (i.e. Alpha in LRS test).

The rule models generated by a rule induction algorithm can be different slightly by changes in upper level process. Classical CN2 [15] generates ordered rules (also known as rule lists or decision lists) in this case the first rule in the ordered list that covers the new example will classify it. Unordered CN2 [14] induces unordered rules (rule sets). Similar to learning in classical CN2, the process of on the upper level is separated to learn rules for each class.. In the latter case, all the rules in the model are used to classify a new example and when more than one rule covers a new example, and the class predicted by them is not the same, a tiebreak criterion is used to decide which rule assess the class of new example more accurate.

In our implementation, on the upper level we adopt an exclusive covering, as Unordered CN2 [14]. On the lower level, we used Laplace estimation as evaluation functions. Pre-pruning of rules is done by using of two LRS test and indicating minimum rule coverage threshold. The First LRS test ensures the minimum required significance level α_1 of a rule when compared to the default rule. In addition, we use a second LRS test; in this case, the rule is compared to its parent rule: it verifies whether the last specialization of the rule has enough significant level α_2 . Finally Minimum coverage threshold specifies the minimal number of examples that each induced rule must cover. The value for the setting parameters are listed in Table.2.

Table.2
The setting parameters of CN2

Time Interval (min)	α_1	α_2	Minimum Coverage
10	0.050	0.020	9
15	0.065	0.020	7
30	0.070	0.020	6

3. Results

To test performance, we used Java programming language to write required procedures for extracting traffic parameters and Level of service with the definition corresponded to the Highway Capacity Manual [42] form raw data then the classification model was built through the widget and python scripting in Orange software. Data for this study come from real-world traffic data set of Hakim highway in Tehran, Iran, which has been gathered in the autumn 2011 with radar traffic sensor. This data set has been obtained from Tehran Traffic control Co. that includes 2519011 instances. Processing these instances, traffic parameters extracted for time intervals with the length of 10, 15 and 30 minutes which respectively result in 12358, 8245, 4121 records. Due to lack of records in LOS B and E, these levels have been merged with their adjacent ones.

3.1. Model Evaluation

The holdout method was used for model evaluation (Fig.2). According to this method, the given data were randomly partitioned into two independent sets, a training set and a test set. The records of 14 days of the data are allocated to the training set, and the remaining is allocated to the test set In Model Builder part that contains Classification Tree, Random Forest, Naïve Bayes and CN2 model inducers, the training set was used to derive the model. Test Learner and Calculate Accuracy part uses output models of Model builder part for prediction of next state of test data and compare it with the real state of traffic to estimate model's accuracy.

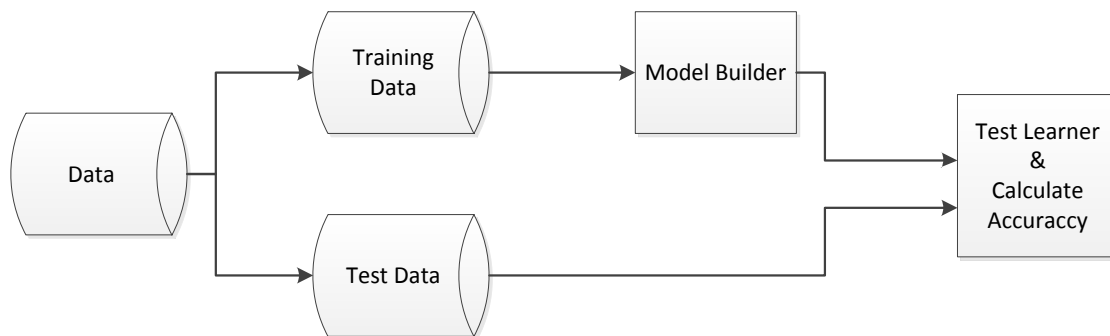


Fig.3. Accuracy estimation with the holdout method

Table.2 provides the model evaluation results and compare the performance of all the classification models on the record forms of 10, 15, and 30 minutes time intervals. In these tables:

Classification accuracy (CA) is the proportion of correctly classified examples, Sensitivity (Sens) (also called true positive rate (TPR), hit rate and recall) is the number of detecting positive examples

among all positive examples, e.g. The proportion of sick people correctly diagnosed as sick, Brier score (Brier) measures the accuracy of probability assessments, which measures the average deviation between the predicted probabilities of events and the actual events.

Table.3
Performance comparison of the classification models

Method	Time Interval (min)	CA	Sens				Brier
			Class A	Class B	Class C	Class D	
Classification Tree	10	0.7962	89.50%	84.00%	70.40%	81.40%	0.2994
	15	0.8105	89.70%	86.90%	71.50%	80.10%	
	30	0.8146	92.20%	85.00%	72.60%	86.00%	
Naïve Bayes	10	0.7807	92.20%	79.00%	65.00%	87.60%	0.3355
	15	0.7749	93.50%	81.60%	62.80%	87.00%	
	30	0.772	92.20%	76.50%	65.50%	90.00%	
Random Forest	10	0.7867	88.00%	88.20%	65.50%	75.20%	0.2994
	15	0.8057	93.60%	88.90%	68.30%	79.50%	
	30	0.8166	94.10%	83.50%	66.40%	92.00%	
CN2	10	0.7746	90.30%	81.10%	68.80%	79.00%	0.3355
	15	0.7846	91.70%	84.10%	66.80%	77.00%	
	30	0.7964	90.20%	93.00%	69.00%	80.00%	

As Table.2 shows, all the four classification methods perform nearly equal quality prediction on three time interval type data sets that shows the models are not depending on time intervals. Classification Tree has the best classification accuracy and Random Forest after Classification tree shows better accuracy proportionately, these models concentrate on entropy and information gain parameters that helps covering noise factor in the data set. Result in Table.2 also shows the naïve Bayes method has a nearly invariant accuracy by changing the length of time interval, this is because of its more depend on numerical data of the current state of traffic. CN2 has a mediocre performance this could be because sequential covering form of building CN2 model. Random Forest and Classification Tree methods consider the whole of the data set and operate in splitting manner. In contrast to them, CN2 covers a portion of the training set the covered by the extracted rule in each iteration so overlapping between inference rules occurs more and cause decreased CN2's performance.

To demonstrate better the performance of prediction methods, scatter diagrams of Fig.3 to Fig.7 compares the real LOS of 30 min time intervals of training set with the predicted LOS that obtained from each classification model. As these diagrams shows, except some boundary point in LOS C and D in other points, the predictions have acceptable correspondent with real-world next state LOS.

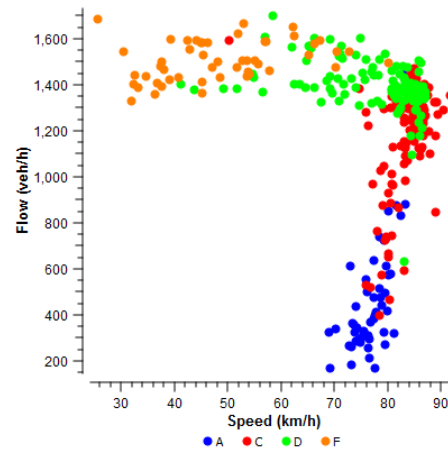


Fig.4. The real next state LOS for 30 min time intervals

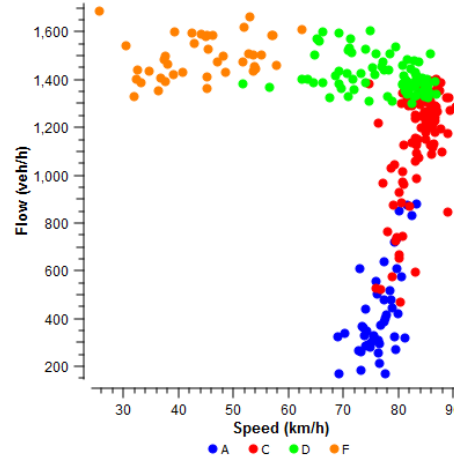


Fig.5. The predicted next state LOS for 30 min time intervals with Classification Tree

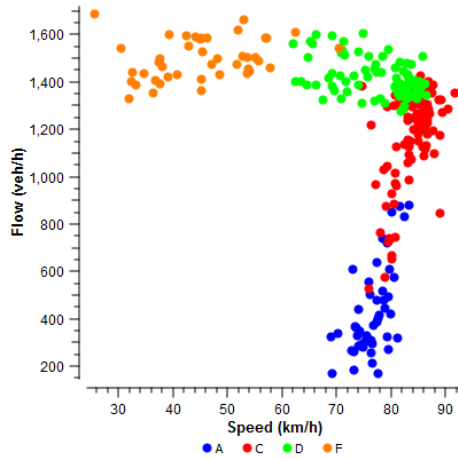


Fig.6. The predicted next state LOS for 30 min time intervals with Random Forest

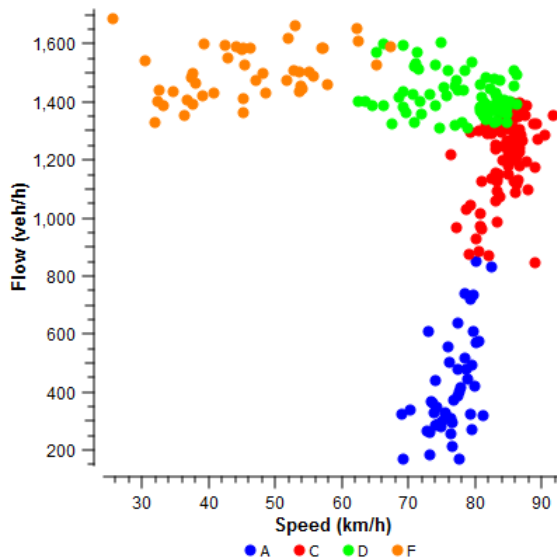


Fig.7. The predicted next state LOS for 30 min time intervals with Naïve Bayes

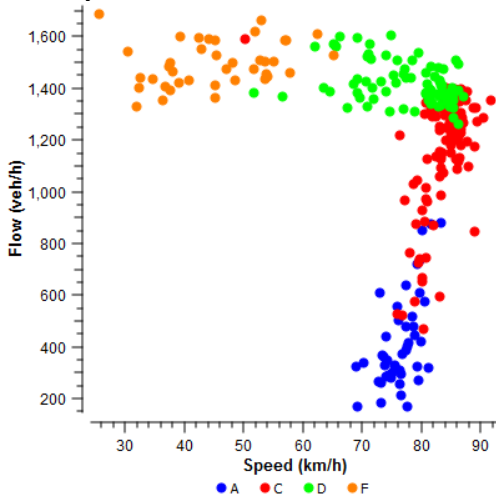


Fig.8. The predicted next state LOS for 30 min time intervals with CN2

3.2. Naïve Bayesian Nomogram

Nomogram is a simple and intuitive, yet useful and powerful representation of linear models, such as logistic regression, naïve Bayesian classifier and linear SVM. Fig.4 shows a Naïve Bayesian nomogram to assess the prediction probability of class A. In statistical terms, the nomogram plots log odds ratios for each value of each attribute. For more information, readers can refer to Mozina & et al. [31]. The topmost horizontal axis of this diagram represents the point scores, e.g. the odds ratio, which are estimated from the training data. To get log odds ratios for a particular value of the attribute, find the vertical axis to the left of the curve corresponding to the attribute. Then imagine a line to the left, at the point where it hits the curve, turn upwards and read the number on the top scale. The curve thus shows a mapping from attribute values on the left to log odds at the top. The lower part of the nomogram (bottom two axes of the nomogram) relates the sum of points as contributed by the known attributes to the class probability $P(Y = C_m|X)$.

The Naïve Bayesian nomogram structure reveals influences of the attribute values to the class probability. According to Fig.4 Flow has the biggest potential influence on the prediction probability of class A, since the corresponding line in the nomogram for this attribute is the longest. After that Speed, Density and Time are respectively influential parameters in the probability of the class A for the next time interval. This diagram also shows that effect of Speed and Time is not monotonous.

3.3. Rule Evaluation

Using CN2 model, the number of 527, 353 and 229 if-then rules generated respectively for 10, 15 and 30 min time intervals which correspondingly in 224, 166 and 102 cases the rule quality was greater than or equal to 0.9. Table.3 lists 14 rules of the whole rule set generated by CN2 on 30 min time interval records. These rules selected by rule quality threshold 0.9 and coverage threshold 40. For example, the rule No. 2 that only depends on Speed and Flow to ensure next state will be in LOS A can be interesting for indicating maximum flow in free-flow condition. The rule No. 14 says between 3:30 PM to 5:30 PM if Speed is less than or equal to 63 km and Flow is greater than 1598, LOS will change to F. Rules like this latter case are interesting in designing traffic management and traveler information systems because they declare detailed

statement with proper variable and precise thresholds.

Table.4 shows an overview of classification tree learned model as a hierarchy in a textual form that can be used to extract propositional rule. This table assesses the probabilities with class A. Columns

respectively shows Majority class, probability of majority class, the probability of the target class, number of instances, relative distribution and absolute distribution.

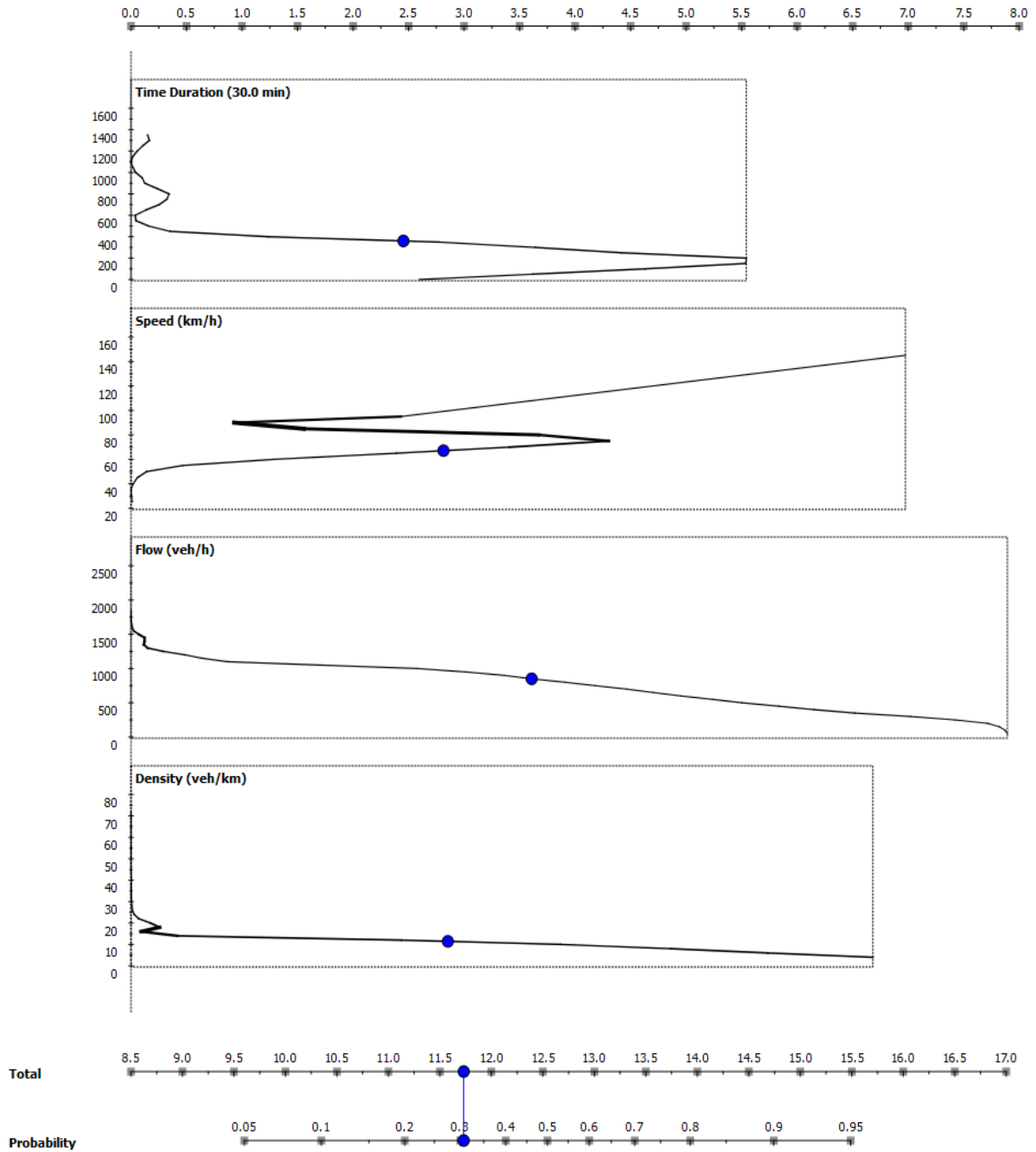


Fig.9. Naïve Bayesian nomogram for prediction of short-term level of service for target class: A, the relative number of examples for each value of attributes was shown by the thickness of the curve corresponding to the attribute where the number of examples is higher.

Table.3
Selected Rules (obtained from 30 min time interval records) with Rule quality threshold 0.9 and coverage threshold 40

No.	Rule length	Rule quality	Coverage	Predicted class	Distribution	Rule
1	4	0.998	430	A	430.0:0.0:0.0:0.0	IF Time Duration (min) \leq 240 AND Flow (veh/h) \leq 774 AND Time Duration (min) $>$ 30 AND Speed (km/h) $>$ 69 THEN nextState=A
2	2	0.978	43	A	43.0:0.0:0.0:0.0	IF Speed (km/h) \leq 95 AND Flow (veh/h) \leq 170 THEN nextState=A
3	3	0.987	74	C	0.0:74.0:0.0:0.0	IF Time Duration (min) $>$ 1350 AND Speed (km/h) $>$ 65 AND Flow (veh/h) $>$ 42 THEN nextState=C
4	3	0.994	152	C	0.0:152.0:0.0:0.0	IF Speed (km/h) $>$ 85 AND Time Duration (min) \leq 390 AND Flow (veh/h) $>$ 102 THEN nextState=C
5	4	0.981	50	C	0.0:50.0:0.0:0.0	IF Flow (veh/h) $>$ 104 AND Speed (km/h) $>$ 90 AND Flow (veh/h) $>$ 1264 AND Density (veh/km) \leq 15 THEN nextState=C
6	4	0.979	45	C	0.0:45.0:0.0:0.0	IF Speed (km/h) $>$ 83 AND Time Duration (min) $>$ 1050 AND Flow (veh/h) \leq 1286 AND Flow (veh/h) $>$ 1246 THEN nextState=C
7	6	0.987	73	C	0.0:73.0:0.0:0.0	IF Flow (veh/h) \leq 1254 AND Density (veh/km) $>$ 11 AND Speed (km/h) $>$ 77 AND Time Duration (min) \leq 390 AND Time Duration (min) $>$ 120 AND Speed (km/h) \leq 84 THEN nextState=C
8	7	0.986	70	C	0.0:70.0:0.0:0.0	IF Density (veh/km) \leq 15 AND Time Duration (min) $>$ 270 AND Time Duration (min) \leq 360 AND Density (veh/km) $>$ 7 AND Speed (km/h) $>$ 74 AND Speed (km/h) \leq 82 AND Flow (veh/h) $>$ 636 THEN nextState=C
9	4	0.979	46	D	0.0:0.0:46.0:0.0	IF Time Duration (min) \leq 900 AND Density (veh/km) \leq 19 AND Density (veh/km) $>$ 18 AND Density (veh/km) \leq 19 THEN nextState=D
10	7	0.977	41	D	0.0:0.0:41.0:0.0	IF Flow (veh/h) $>$ 1356 AND Time Duration (min) \leq 900 AND Density (veh/km) $>$ 16 AND Density (veh/km) \leq 22 AND Speed (km/h) \leq 76 AND Flow (veh/h) \leq 1480 AND Flow (veh/h) $>$ 1410 THEN nextState=D
11	5	0.983	58	D	0.0:0.0:58.0:0.0	IF Density (veh/km) $>$ 15 AND Time Duration (min) \leq 900 AND Density (veh/km) \leq 18 AND Speed (km/h) \leq 83 AND Time Duration (min) $>$ 750 THEN nextState=D
12	6	0.984	60	D	0.0:0.0:60.0:0.0	IF Flow (veh/h) $>$ 1254 AND Density (veh/km) $>$ 16 AND Speed (km/h) \leq 73 AND Time Duration (min) $>$ 990 AND Time Duration (min) \leq 1170 AND Speed (km/h) $>$ 67 THEN nextState=D
13	4	0.988	83	F	0.0:0.0:0.0:83.0	IF Speed (km/h) \leq 53 AND Flow (veh/h) $>$ 1480 AND Density (veh/km) $>$ 37 AND Time Duration (min) \leq 1170 THEN nextState=F
14	4	0.985	65	F	0.0:0.0:0.0:65.0	IF Speed (km/h) \leq 63 AND Flow (veh/h) $>$ 1598 AND Time Duration (min) $>$ 930 AND Time Duration (min) \leq 1050 THEN nextState=F

4. Conclusion

In this study, a classification data mining approach has proposed for the prediction of road facility's level of service and producing simple and easy handling if-then rules. This method can be used in designing intelligent transportation and expert systems and in studying of traffic pattern by traffic engineers.

The results show Classification Tree and Random Forest have the best result in prediction. The Naïve Bayesian nomogram also showed that Flow has the biggest potential influence between other attributes

on the prediction. CN2 model generated some well-suited if-then rules that can be used in studying of the traffic pattern.

A considerable number of topics can be investigated in this area for future work, including: setting boundary conditions and calibration parameters of macroscopic simulation models according to predict LOS, finding road facility characteristics and recognition effective variable information and prediction of congestion, designing the decision tree controller, expert traffic systems and knowledge base systems based on the generated if-then rules.

Table.4
Hierarchy rules of classification tree with target class: A; Tree size: 615 nodes, 308 leaves

Classification Tree	Class	P(Class)	P(Target)	# Inst	Distribution (rel)	Distribution (abs)
Density (veh/km) <=16.314	C	0.375	0.173	4121	0.173:0.375:0.306:0.145	713:1547:1263:598
	C	0.577	0.292	2416	0.292:0.577:0.129:0.002	706:1393:311:6
Flow (veh/h) <=899	A	0.752	0.752	896	0.752:0.232:0.015:0.001	674:208:13:1
Time Duration (min) <=255	A	0.96	0.96	572	0.960:0.040:0.000:0.000	549:23:0:0
Time Duration (min) <=45	C	0.789	0.211	19	0.211:0.789:0.000:0.000	4:15:0:0
Flow (veh/h) <=798	A	0.5	0.5	8	0.500:0.500:0.000:0.000	4:4:0:0
Flow (veh/h) >798	C	1	0	11	0.000:1.000:0.000:0.000	0:11:0:0
Time Duration (min) >45	A	0.986	0.986	553	0.986:0.014:0.000:0.000	545:8:0:0
Time Duration (min) >255	C	0.571	0.386	324	0.386:0.571:0.040:0.003	125:185:13:1
Flow (veh/h) <=458	A	0.8	0.8	105	0.800:0.171:0.029:0.000	84:18:3:0
Flow (veh/h) <=184	A	0.92	0.92	50	0.920:0.020:0.060:0.000	46:1:3:0
Flow (veh/h) >184	A	0.691	0.691	55	0.691:0.309:0.000:0.000	38:17:0:0
Flow (veh/h) >458	C	0.763	0.187	219	0.187:0.763:0.046:0.005	41:167:10:1
Density (veh/km) <=8.142	C	0.596	0.362	94	0.362:0.596:0.043:0.000	34:56:4:0
Density (veh/km) >8.142	C	0.888	0.056	125	0.056:0.888:0.048:0.008	7:111:6:1
Flow (veh/h) >899	C	0.78	0.021	1520	0.021:0.780:0.196:0.003	32:1185:298:5
Density (veh/km) <=14.990	C	0.884	0.037	845	0.037:0.884:0.077:0.002	31:747:65:2
Time Duration (min) <=405	C	0.936	0.058	360	0.058:0.936:0.006:0.000	21:337:2:0
Speed (km/h) <=85.242	C	0.891	0.1	211	0.100:0.891:0.009:0.000	21:188:2:0
Speed (km/h) >85.242	C	1	0	149	0.000:1.000:0.000:0.000	0:149:0:0
Time Duration (min) >405	C	0.845	0.021	485	0.021:0.845:0.130:0.004	10:410:63:2
Speed (km/h) <=81.499	D	0.538	0.077	13	0.077:0.231:0.538:0.154	1:3:7:2
Speed (km/h) >81.499	C	0.862	0.019	472	0.019:0.862:0.119:0.000	9:407:56:0
Density (veh/km) >14.990	C	0.649	0.001	675	0.001:0.649:0.345:0.004	1:438:233:3
Time Duration (min) <=1155	C	0.575	0.002	511	0.002:0.575:0.417:0.006	1:294:213:3
Speed (km/h) <=86.899	D	0.556	0	279	0.000:0.434:0.556:0.011	0:121:155:3
Speed (km/h) >86.899	C	0.746	0.004	232	0.004:0.746:0.250:0.000	1:173:58:0
Time Duration (min) >1155	C	0.878	0	164	0.000:0.878:0.122:0.000	0:144:20:0
Speed (km/h) <=83.418	C	0.783	0	69	0.000:0.783:0.217:0.000	0:54:15:0
Speed (km/h) >83.418	C	0.947	0	95	0.000:0.947:0.053:0.000	0:90:5:0

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