# Developing a Decision Model as Budget Assignment Method for Locating Industrial Facilities: Real Case Study 

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#### Abstract

In today's world, due to the existence of several criteria in every decision, budgeting has become a complex issue. Applying decision-making methods significantly helps to make optimal decisions. Multiple criteria decision making (MCDM) is a branch of operational research dealing with finding optimal results in complex scenarios including various indicators, conflicting objectives, criteria, and various indicators. The paper presents a location-allocation decision-making problem resulting in the selection of the most desirable location for the consulting service center in the Qazvin state of Iran. In the first stage, different location criteria are determined. Then, the decision-making matrix preparation is completed based on the criteria dimension and expert opinions. The decision problem is formulated as a multiple criteria ranking problem (MCDM). In the second stage, the decision-making is performed by using all three models of the PROMETHEE method. Finally, considered locations are ranked from the best choice to the worst one with the application of the PROMETHEE MCDM/A method.


Keywords: Locational alocation, multicriteria decision making, PROMETHE, location problems.

## 1.Introduction

In today's economy, characterized by a dynamic and volatile environment, many researchers stress the significance of location factors(Kaboli \& et. al., 2007). Location allocation decisions are made in both private and public sectors. For example, governments need to determine the locations for emergency bases highway patrol vehicles, fire bases, ambulances, television antennas, and exploratory oil wells. In all cases, poor locations can increase the likelihood of property damage and cost life. In private sectors, locations of warehouses and distribution centers, production and assembly facilities, offices, and retail outlets must be onsidered. Facility location applications are concerned with the location of one or more facilities in such a way that a certain objective such as minimizing transportation cost, providing equitable service to consumers, capturing the largest market share, and etc. Facility location problems may rise challenging geometrical and combinational problems. The research on facility location problems spans many research fields such as operations research/management science, industrial engineering, geography, economics, computer science, mathematics problems considering both qualitative and quantitative factors. Kahne (Kahne, 1975) considered 29 attributes and
and marketing (Kim \& et.al, 1999). Location theory was first introduced by Weber (Tabari \& et. al., 2008), who considered the problem of locating a single warehouse in order to minimize the total travel distance between the warehouse and a set of spatially distributed costumers. In fact, he proposed a material index for selecting the location in which if this index is grater than one, the warehouse should be installed in the vicinity of the source of raw material; or otherwise, it should be close to the market. Smithies and Stevens (Stevens \& et. al., 1961) extended the Hotelling's problem later. Hakimi (Hakimi, 1964) considered a general problem to locate one or more facilities on a network by minimizing the sum of the distances and the maximum distance between facilities and points on a network. Considerable research and theoretical interest in the location problem have been carried out after this seminal paper. Brown and Gibson (Tabari \& et. al., 2008), and Buffa and Sarin proposed a facility location model for a multidimensional location problem based on critical factors, objective factors, and subjective factors. Fortenberry and Mitra (Fortenberry \& Mitra, 1986) resented a model for the location-allocation

[^0]used a weighting model to determine the relative mportance with uncertainty in attributes. Kirkwood (Kirkwood, 1982) discussed a multi-disciplinary study conducted to select a site for a nuclear power facility. Linares and Romrero (Liang, 2000) roposed a methodology that combined several multi-criteria methods to address electricity planning problems. Several MCDM methods for the location selection are used such as Liang and Wang ( Liang \& Wang, 1991) who proposed an algorithm for a site selection based on the concepts of the fuzzy set theory. Lianares (2000) proposed a holistic MCDM model for the facility location selection. Montajabiha and Wang (2016) proposed a fuzzy TOPSIS model in the facility location problem. Finally, this paper concludes with gained results.
approach to select the best facility location under linguistic environment. MCGDM methods if decision makers (DMs) are not able to treat precise data in order to define their preferences, the intuitionistic fuzzy set (IFS) theory enables them (Montajabiha and Wang, 2016). The ranking of options is done by comparing their pairs in each index. The ROMETHEE method provides six generalized criteria to define the superiority function for the decision maker (Figueroa, 2019).The structure of this paper is as follows: First, the PROMETHE model is introduced. Second, the case study is described in detail. Analysis of a case study is then discussed in order to verify the practicability and effectiveness of the proposed

$P_{j}$ : Preference Function of Criteria $j$<br>sc: Sign of Criteria ( $1 \times n$ vector)<br>DC: Differences on Criteria (Deviation between alternatives over $j^{\text {th }}$ criteria)

## PFC: Preference Function on Criteria

## PFV: Preference Function Value

## PI: Preference Index Value

## WPI: Weighted Preference Index

pfv : Preference Function Value Vector

## PI: Preference Index

## 2. PROMETHEE Decision-Making Process

## 2.1

Before describing the detailed process of the algorithm some notations are summarized for more simplification.

The PROMETHEE method is well-known as a multicriteria decision-making method in which alternatives ranking is obtained based on preference function, criteria, and their criteria. For this purpose, determined preference function $P_{j}\left(f_{j} a_{1} a_{2}\right)$ has been used to show preference of alternative $\boldsymbol{a}_{1}$ over alternative $\boldsymbol{a}_{2}$ for specific criteria, $f j$. In other words, $P_{j}\left(f_{j} a_{1} a_{2}\right)$ is a type of function that can
convert alternative differences on $j^{\text {th }}$ criteria $f_{j} a_{1} a_{2}=$ $\pm l *\left(x_{I}-x_{2}\right)$ to find required values for further calculation. Sign of criteria $\left(c_{j}\right)$ can be stored in $\boldsymbol{s c} 1 \times n$ vector ( $\boldsymbol{s c}=[ \pm 1$ $\pm 1 \ldots \pm 1]$ ) and criteria weights are demonstrated in weight wector ( $\boldsymbol{w}$ ). The PROMETHEE method encompasses six types of preference function for criteria as mentioned in table 1 .

Table 1.
Preference function types in the PROMETHEE method

Type I (Usual criterion)

$P(d)= \begin{cases}0 & d \leq 0 \\ 1 & d>0\end{cases}$

Type IV (Level-criterion)


Type II (Quasi-criterion)


$$
P(d)= \begin{cases}0 & d \leq q \\ 1 & d>q\end{cases}
$$

Type V (Linear criterion)


Type III (V-sharp criterion)

$P(d)= \begin{cases}\frac{d}{p} & d \leq p \\ 1 & d>p\end{cases}$
Type VI (Gaussian criterion)

$P(d)=\left\{\begin{array}{cc}0 & d \leq q \\ \frac{1}{2} & q<d \leq q+p \\ 1 & q+p<d\end{array} \quad P(d)=\left\{\begin{array}{ll}0 & d \leq q \\ \frac{d-q}{p-q} & q<d \leq q+p \\ 1 & q+p<d\end{array} \quad P(d)= \begin{cases}0 & d \leq 0 \\ 1-e^{-\frac{d^{2}}{2 \sigma^{2}}} & d>0\end{cases}\right.\right.$

### 2.1.1

PROMETHEE as a powerful decision-making tool can calculate alternatives ranking by various criteria consideration, in 2 phases. In the method, $w_{j}$ is the weight of the $j^{t h}$ criteria and normalized weights aggregation should be equal to on $\left(\sum_{j=1}^{n} w_{j}=1\right)$.

Phase 1 started by gathering and preparing data in the shape of a matrix, which introduces alternatives and their criteria values in every row as $x_{i j}$.

Table 2.
Decision matrix (alternatives and criteria)

| $a$ |  | $\pm c 1$ |  | $\pm$ cn |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $x_{11}$ | $x_{12}$ | $\pm \begin{array}{rr} \\ \\ & \ldots \\ & \ldots\end{array}$ | $x_{1 n}$ | $i=1, \ldots, m$ |
|  | $\boldsymbol{a}_{2}$ | $x_{21}$ | $x_{22}$ | ... | $x_{2 n}$ |  |
| $D=$ | ! | ! | $\vdots$ | $\vdots$ | : |  |
|  | $a_{m}$ | $x_{m 1}$ | $x_{m 2}$ | ... | $x_{m n}$ | ., $n$ |

By considering the criteria sign vector ( $\boldsymbol{s c}$ ), the elements ( $f_{j} a_{1} a_{2}$ ) of matrix $\boldsymbol{D C}$ can be interpreted as the deviation values between alternatives and all pairwise comparisons over $j_{\mathrm{th}}$ criteria (size of DC matrix $m^{2} \times n$ ). In table 3, $f_{3} 12$
$= \pm 1 *\left(x_{13}-x_{23}\right)$ illustrates mentioned comparison between alternative $\boldsymbol{a}_{\boldsymbol{1}}$ and $\boldsymbol{a}_{\mathbf{2}}$ on $3^{\text {rd }}$ criteria considering $c_{j}$ sign for instance.

Table 3.
Matrix of differences on criteria

2.1.2

Preference function value and weighted preference index show a relation between alternatives. Based on criteria features, elements of $\boldsymbol{D C}$ have to adjust with the
preference function of $j^{\text {th }}$ criteria. Here preference functions convert $\boldsymbol{D C}$ matrix to $\boldsymbol{P F C}$ which is a fundamental matrix for further calculation, including $\boldsymbol{P F V}$ , PI and finally alternative ranking can be obtained

Table 4.
Matrix of preference function on DC

|  |  | $\pm c_{1}$ | $\pm c_{2}$ | ... | $\pm c_{n}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $a_{1} a_{1}$ | $P_{1}\left(f_{111}\right)$ | $P_{2}\left(f_{211}\right)$ | ... | $P_{n}\left(f_{n 11}\right)$ |  |
|  | $a_{1} a_{2}$ | $P_{1}\left(f_{12}\right)$ | $P_{2}\left(f_{212}\right)$ | ... | $P_{n}\left(f_{n} 12\right)$ |  |
| $P F C=$ | ; | : | ! | : | ! | $j=1, \ldots, n$ |
|  | $a_{m} a_{m-1}$ | $P_{1}\left(f_{1 m(m-1)}\right)$ | $P_{2}\left(f_{2 m(m-1)}\right)$ | $\ldots$ | $P_{n}\left(f_{n m(m-1)}\right)$ |  |
|  | $a_{m} a_{m}$ | $P_{1}\left(f_{1 m m}\right)$ | $P_{2}\left(f_{2 m m}\right)$ | $\ldots$ | $P_{n}\left(f_{n m m}\right)$ |  |

### 2.1.3 Preference Function Value

Horizontal summation of $P F C$ expresses $\boldsymbol{p} \boldsymbol{f} \boldsymbol{v}$ vector of all pair alternatives within $m^{2} \times 1$ vector which could be elaborately reshaped to matrix $P F V m \times m$ as table 5

Table 5.
Matrix of preference function value

|  | $a_{1}$ | $a_{2}$ | $\cdots$ | $a_{m}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $a_{1}$ | $\sum P_{j}\left(f_{j 11}\right)$ | $\sum P_{j}\left(f_{j 11}\right)$ | $\ldots$ | $\sum P_{j}\left(f_{j m 1}\right)$ |  |
| $P F V=$ | $a_{2}$ | $\sum P_{j}\left(f_{j 12}\right)$ | $\sum P_{j}\left(f_{j 21}\right)$ | $\cdots$ | $\sum P_{j}\left(f_{j m 2}\right)$ |$\quad i=1, \ldots, m$

### 2.1.4.Weighted Preference Index

By applying criteria weights on the $P F C$ matrix, needed matrixes like WPI and PI are obtainable. According to Eq.1, the PI matrix is obtained from the multiplication of $\boldsymbol{w}_{\boldsymbol{j}}$ to $\boldsymbol{c}_{\boldsymbol{j}}$ value of PFC. In this study, $\boldsymbol{w}_{\boldsymbol{j}}$ values of all criteria
$\pi\left(a_{i}, a_{i}\right)=\sum_{j=1}^{n} w_{j} \times P_{j}\left(f_{j} i i^{\prime}\right)$
follow the normalization condition which means criteria weights summation is equal to $1\left(\sum_{j=1}^{n} w_{j}=1\right)$.
Horizontal summation on WPI matrix results in $\boldsymbol{p i}$ vector with the size of $m^{2} \times 1$. As each element of $\boldsymbol{p i}$ vector expresses a relation of two alternatives, it could be reshaped to PI matrix $m \times m$ as it is shown in table 6 .

Table 6.
preference index Matrix

|  |  | $a_{1}$ | $\boldsymbol{a}_{2}$ | ... | $\boldsymbol{a}_{\boldsymbol{m}}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $a_{1}$ | $\pi\left(a_{1} a_{1}\right)$ | $\pi\left(a_{1} a_{2}\right)$ | $\ldots$ | $\pi\left(a_{1} a_{m}\right)$ | $i=1, \ldots, m$ |
|  | $\boldsymbol{a}_{2}$ | $\pi\left(a_{2} a_{1}\right)$ | $\pi\left(a_{2} a_{2}\right)$ | $\ldots$ | $\pi\left(a_{2} a_{m}\right)$ | $j=1, \ldots, n$ |
| $P I=$ | : | ! | ! | : | ! |  |
|  | $a_{m}$ | $\pi\left(a_{n} a_{1}\right)$ | $\pi\left(a_{n} a_{2}\right)$ | ... | $\pi\left(a_{m} a_{m}\right)$ |  |

## 2.2.

In the second step, based on PROMETHEE method, pertinent calculations on alternatives obtain alternatives out ranking.

### 2.2.1 PROMETHEE I

As PROMETHEE basis is on a relation between alternatives,the entering and leaving flows are determined through Eq.

$$
\begin{equation*}
a_{1} P^{+} a_{2} \text { if } \phi^{+}\left(a_{1}\right)>\phi^{+}\left(a_{2}\right) \tag{4}
\end{equation*}
$$

$a_{1} I^{+} a_{2}$ if $\phi^{+}\left(a_{1}\right)=\phi^{+}\left(a_{2}\right)$

In this method, the $a_{1}$ alternative is superior to alternative $a_{2}$, as Eq.8..

$$
a_{1} P^{I} a_{2} \quad \text { if }: \begin{align*}
& a_{1} P^{+} a_{2} \text { and } a_{1} P^{-} a_{2}  \tag{9}\\
& a_{1} P^{+} a_{2} \text { and } a_{1} I^{-} a_{2}  \tag{8}\\
& a_{1} I^{+} a_{2} \text { and } a_{1} P^{-} a_{2}
\end{align*}
$$

### 2.2.2. PROMETHEE II

In this method, net flow of alternatives is obtained from Eq. 10 and then a comparison between pairs of alternatives is accomplished by Eq.11.The $a_{1}$ alternative is better than the alternative $a_{2}$ under the condition of Eq. 9 and Eq. 10 .

$$
\begin{align*}
& \phi\left(a_{i}\right)=\phi^{+}\left(a_{i}\right)-\phi^{-}\left(a_{i}\right), \quad i=1,2, \ldots, m \\
& a_{1} P^{I I} a_{2} \text { if }: \phi\left(a_{1}\right)>\phi\left(a_{2}\right) \tag{11}
\end{align*}
$$

Furthermore, two alternatives are indifferent to each other under the condition of Eq. 12.

$$
\begin{equation*}
a_{1} I^{I I} a_{2} \text { if }: \phi\left(a_{1}\right)=\phi\left(a_{2}\right) \tag{12}
\end{equation*}
$$

### 2.2.3 PROMETHEE III

In this technique, final alternatives ranking is calculated by using interval values. The interval values are obtained from Eqs.15. and Eq. 16.
lternatives flow calculations based on PROMETHEE I are determined through Eq. 4 to Eq. 7.(2) and Eq.(3).

$$
\begin{align*}
& a_{1} P^{-} a_{2} \text { if } \phi^{-}\left(a_{2}\right)>\phi^{-}\left(a_{1}\right)  \tag{6}\\
& a_{1} I^{-} a_{2} \text { if } \phi^{-}\left(a_{1}\right)=\phi^{-}\left(a_{2}\right) \tag{7}
\end{align*}
$$

In addition, the alternatives $a_{1}$ and $a_{2}$ are indifferent to each other under the condition of Eq.9.

$$
a_{1} I^{I} a_{2} \text { if : } a_{1} I^{-} a_{2} \text { and } a_{1} I^{+} a_{2}
$$



$$
\left\{\begin{array}{l}
\left\{\begin{array}{l}
X_{a_{i}}=\bar{\phi}\left(a_{i}\right)-\alpha \sigma_{a_{i}} \\
Y_{a_{i}}=\bar{\phi}\left(a_{i}\right)+\alpha \sigma_{a_{i}}
\end{array} \quad i=1,2, \ldots, m\right. \\
\bar{\phi}\left(a_{i}\right)=\frac{1}{m} \sum_{A_{i} \in A}\left[\pi\left(a_{i}, a_{i^{\prime}}\right)-\pi\left(a_{i^{\prime}}, a_{i}\right)\right]=\frac{1}{m} \phi\left(a_{i}\right) \\
\sigma_{a_{i}}^{2}=\frac{1}{m} \sum_{A_{i} \in A}\left[\pi\left(a_{i}, a_{i^{\prime}}\right)-\pi\left(a_{i^{\prime}}, a_{i}\right)-\bar{\phi}\left(a_{i}\right)\right]^{2}
\end{array}\right.
$$

## 3. Problem Definition and Decision-Making Process

Industrial Estates Management Organization of Ghazvin province tends to establish a consulting service department in one of five main industrial estates. This department provides companies with engineering and financial consulting. All cities are located in the province with different specifications which are defined as their
criteria. Included cities or alternatives in this decisionmaking case are Abeyek $\left(\boldsymbol{a}_{1}\right)$, Arasanj ( $\boldsymbol{a}_{2}$ ), Heydariyeh $\left(\boldsymbol{a}_{3}\right)$, Khorram Dasht $\left(\boldsymbol{a}_{4}\right)$, Lia $\left(\boldsymbol{a}_{5}\right)$.

Problem features include 17 criteria which are defined by experts after a deep field survey as mentioned in table 7. By conducting meetings with informants and converting qualitative elements to quantitative, matrix (D) values have been prepared as mentioned in table 8 .

Table 7
criteria of the location budget assignment case study

| $c_{1}:$ | General conditions of land |
| :--- | :--- |
| $c_{2}:$ | Subside supporting |
| $c_{3}:$ | Welfare and healthcare facilities |
| $c_{4}:$ | Public infrastructure facilities |
| $c_{5}:$ | Number of industrial units that can be installed in the state |
| $c_{6}:$ | Counselors willingness to settle in the center |
| $c_{7}:$ | Special features and infrastructure |
| $c_{8}:$ | Employable people population in the state |
| $c_{9}:$ | Cultural and social contexts in the state |
| $c_{10}:$ | Recruiting potential of the state |
| $c_{11}:$ | Distance to the capital of the province |
| $c_{12}:$ | Distance to roads and highways |
| $c_{13}:$ | Distance to the railway |
| $c_{14}:$ | Distance to the airport |
| $c_{15}:$ | Distance to research centers and universities |
| $c_{16}:$ | Distance to other industrial states |
| $c_{17}:$ | Distance to administrative centers |

Table 8.
Decision matrix for location- budget assignment

|  |  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ | $c_{5}$ | $c_{6}$ | $c_{7}$ | $c_{8}$ | $c_{9}$ | $c_{10}$ | $c_{11}$ | $c_{12}$ | $c_{13}$ | $c_{14}$ | $c_{15}$ | $c_{16}$ | $c_{17}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $D=$ | $a_{1}$ | 85 | 77 | 88 | 104 | 91 | 92 | 92 | 85 | 76 | 99 | 72 | 103 | 93 | 67 | 70 | 78 | 75 |
|  | $a_{2}$ | 110 | 77 | 89 | 115 | 93 | 80 | 81 | 87 | 74 | 89 | 74 | 106 | 100 | 83 | 82 | 92 | 81 |
|  | $a_{3}$ | 112 | 70 | 69 | 100 | 84 | 58 | 69 | 76 | 65 | 74 | 96 | 122 | 97 | 104 | 99 | 104 | 108 |
|  | $a_{4}$ | 113 | 72 | 68 | 104 | 85 | 57 | 74 | 85 | 65 | 74 | 132 | 124 | 103 | 104 | 105 | 119 | 91 |
|  | $a_{5}$ | 121 | 88 | 116 | 126 | 123 | 112 | 101 | 120 | 92 | 108 | 69 | 100 | 79 | 78 | 74 | 77 | 74 |



Fig.1. Alternatives of the research in Ghazvin province case study.

Criteria sign vector is introduced based on criteria characteristics as shown in the table.9. The positive signs express the fact that larger amounts are more favorable in
the criteria, and in the negative criteria smaller values play this role.

Table 9
Sign of criteria

| $c_{j}$ | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ | $c_{5}$ | $c_{6}$ | $c_{7}$ | $c_{8}$ | $c_{9}$ | $c_{10}$ | $c_{11}$ | $c_{12}$ | $c_{13}$ | $c_{14}$ | $c_{15}$ | $c_{16}$ | $c_{17}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sign | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 |

With the respect to criteria features, 17 different values were gathered for every alternative by expert informant questionnaire and field survey as shown in table.3. So, alternatives comparisons and calculations have been accomplished based on thier $\boldsymbol{D}$ matrix.

As mentioned in 2.1.1 deviation between alternatives over $j^{t h}$ criteria is demonstrated in $\boldsymbol{D C}$ matrix in table 10. The values of the matrix are obtained based on a pairwise comparison of alternatives in all criteria. Obviously, $\boldsymbol{a}_{i i}$ values of the matrix are zero as there is no difference between one alternative with itself.

Table 10
DC matrix

| $a_{1} a_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a_{1} a_{2}$ | 0 | 0 | 0 | 0 | 0 | 0.165 | 0.236 | 0 | 0.014 | 0.118 | 0 | 0 | 0 | 0.5 | 0.5 | 0.5 | 0 |
| $a_{1} a_{3}$ | 0 | 0.092 | 0 | 0 | 0 | 0.764 | 0.691 | 0.063 | 0.343 | 0.542 | 0.5 | 0.5 | 0 | 0.5 | 0.5 | 0.5 | 0.5 |
| $a_{1} a_{4}$ | 0 | 0.066 | 0 | 0 | 0 | 0.784 | 0.513 | 0 | 0.343 | 0.542 | 0.5 | 0.5 | 0 | 0.5 | 0.5 | 0.5 | 0.5 |
| $a_{1} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.5 | 0 | 0 | 0 |
| $a_{2} a_{1}$ | 0.227 | 0 | 0 | 0 | 0 | 0 | 0 | 0.003 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{2} a_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{2} a_{3}$ | 0 | 0.092 | 0 | 0 | 0 | 0.454 | 0.274 | 0.092 | 0.245 | 0.245 | 0.5 | 0.5 | 0 | 0.5 | 0.5 | 0 | 0.5 |
| $a_{2} a_{4}$ | 0 | 0.066 | 0 | 0 | 0 | 0.484 | 0.103 | 0.003 | 0.245 | 0.245 | 0.5 | 0.5 | 0 | 0.5 | 0.5 | 0.5 | 0 |
| $a_{2} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{1}$ | 0.245 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{2}$ | 0.018 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{4}$ | 0 | 0 | 0 | 0 | 0 | 0.001 | 0 | 0 | 0 | 0 | 0.5 | 0 | 0 | 0 | 0 | 0.5 | 0 |
| $a_{3} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{1}$ | 0.255 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{2}$ | 0.027 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{3}$ | 0.009 | 0.026 | 0 | 0 | 0 | 0 | 0.054 | 0.063 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.5 |
| $a_{4} a_{4}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{5} a_{1}$ | 0.327 | 0.145 | 1 | 1 | 0 | 0.393 | 0.165 | 0.625 | 0.589 | 0.096 | 0 | 0 | 0.5 | 0 | 0 | 0 | 0 |
| $a_{5} a_{2}$ | 0.1 | 0.145 | 1 | 0 | 0 | 0.722 | 0.589 | 0.582 | 0.675 | 0.363 | 0 | 0 | 0.5 | 0 | 0 | 0.5 | 0 |
| $a_{5} a_{3}$ | 0.082 | 0.237 | 1 | 1 | 1 | 0.974 | 0.897 | 0.787 | 0.92 | 0.764 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 |
| $a_{5} a_{4}$ | 0.073 | 0.211 | 1 | 1 | 1 | 0.977 | 0.802 | 0.625 | 0.92 | 0.764 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 |
| $a_{5} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

According to 2.1.2, applying appropriate preference function on $\boldsymbol{D C}$ matrix can transform it into $\boldsymbol{P F C}$ matrix. In this case study, preference function type 2 has been used for $c_{1}$ and $c_{2}$ and type 1 for criteria $c_{3}, c_{4}$, and $c_{5}$.

Criteria $c_{6}$ to $c_{10}$ meet the type 6 preference function. The remaining criteria from $c_{11}$ to $c_{17}$ were compatible with preference type 4 and their result is demonstrated in table 11.

Table 11
PFC matrix

| $a_{1} a_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a_{1} a_{2}$ | 0 | 0 | 0 | 0 | 0 | 0.165 | 0.236 | 0 | 0.014 | 0.118 | 0 | 0 | 0 | 0.5 | 0.5 | 0.5 | 0 |
| $a_{1} a_{3}$ | 0 | 0.092 | 0 | 0 | 0 | 0.764 | 0.691 | 0.063 | 0.343 | 0.542 | 0.5 | 0.5 | 0 | 0.5 | 0.5 | 0.5 | 0.5 |
| $a_{1} a_{4}$ | 0 | 0.066 | 0 | 0 | 0 | 0.784 | 0.513 | 0 | 0.343 | 0.542 | 0.5 | 0.5 | 0 | 0.5 | 0.5 | 0.5 | 0.5 |
| $a_{1} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.5 | 0 | 0 | 0 |
| $a_{2} a_{1}$ | 0.227 | 0 | 0 | 0 | 0 | 0 | 0 | 0.003 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{2} a_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{2} a_{3}$ | 0 | 0.092 | 0 | 0 | 0 | 0.454 | 0.274 | 0.092 | 0.245 | 0.245 | 0.5 | 0.5 | 0 | 0.5 | 0.5 | 0 | 0.5 |
| $a_{2} a_{4}$ | 0 | 0.066 | 0 | 0 | 0 | 0.484 | 0.103 | 0.003 | 0.245 | 0.245 | 0.5 | 0.5 | 0 | 0.5 | 0.5 | 0.5 | 0 |
| $a_{2} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{1}$ | 0.245 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{2}$ | 0.018 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{4}$ | 0 | 0 | 0 | 0 | 0 | 0.001 | 0 | 0 | 0 | 0 | 0.5 | 0 | 0 | 0 | 0 | 0.5 | 0 |
| $a_{3} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{1}$ | 0.255 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{2}$ | 0.027 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{3}$ | 0.009 | 0.026 | 0 | 0 | 0 | 0 | 0.054 | 0.063 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.5 |
| $a_{4} a_{4}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{5} a_{1}$ | 0.327 | 0.145 | 1 | 1 | 0 | 0.393 | 0.165 | 0.625 | 0.589 | 0.096 | 0 | 0 | 0.5 | 0 | 0 | 0 | 0 |
| $a_{5} a_{2}$ | 0.1 | 0.145 | 1 | 0 | 0 | 0.722 | 0.589 | 0.582 | 0.675 | 0.363 | 0 | 0 | 0.5 | 0 | 0 | 0.5 | 0 |
| $a_{5} a_{3}$ | 0.082 | 0.237 | 1 | 1 | 1 | 0.974 | 0.897 | 0.787 | 0.92 | 0.764 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 |
| $a_{5} a_{4}$ | 0.073 | 0.211 | 1 | 1 | 1 | 0.977 | 0.802 | 0.625 | 0.92 | 0.764 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 |
| $a_{5} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

As it is explained in 2.1.3, horizontal aggregation on $\boldsymbol{P F C}$ matrix for bilateral elements results $\boldsymbol{p} \boldsymbol{f} \boldsymbol{v}$ vector with $\mathrm{m}^{2}$
rows. By putting these elements in $m \times m$ matrix respectively, $\boldsymbol{P F V}$ matrix has resulted as mentioned in table12. So, preference function values of every two alternative are depicted.

Table 12
PFV matrix

|  | $\boldsymbol{a}_{\boldsymbol{1}}$ | $\boldsymbol{a}_{2}$ | $\boldsymbol{a}_{\mathbf{3}}$ | $\boldsymbol{a}_{\boldsymbol{4}}$ | $\boldsymbol{a}_{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{a}_{\boldsymbol{1}}$ | 0 | 2.032 | 5.496 | 5.248 | 0.500 |
| $\boldsymbol{a}_{2}$ | 0.230 | 0 | 3.902 | 3.646 | 0 |
| $\boldsymbol{a}_{3}$ | 0.245 | 0.018 | 0 | 1.0012 | 0 |
| $\boldsymbol{a}_{\boldsymbol{4}}$ | 0.255 | 0.027 | 0.652 | 0 | 0 |
| $\boldsymbol{a}_{5}$ | 4.840 | 5.176 | 11.162 | 10.872 | 0 |

By multiplying normalized weights vector into PFC matrix, WPI matrix is calculated which is shown in table 13. If weight vector elements aggregation was equal to
one. These weights are called normalized weights. By using this matrix, every weighted pairwise amount of the main matrix is obtained.

Table 13
WPI matrix

| $a_{1} a_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a_{1} a_{2}$ | 0 | 0.001 | 0.007 | 0 | 0 | 0 | 0.029 | 0.029 | 0.029 | 0 | 0 | 0.001 | 0.007 | 0 | 0 | 0 | 0.029 |
| $a_{1} a_{3}$ | 0.004 | 0.020 | 0.032 | 0.029 | 0.029 | 0 | 0.029 | 0.029 | 0.029 | 0.029 | 0.004 | 0.020 | 0.032 | 0.029 | 0.029 | 0 | 0.029 |
| $a_{1} a_{4}$ | 0 | 0.020 | 0.032 | 0.029 | 0.029 | 0 | 0.029 | 0.029 | 0.029 | 0.029 | 0 | 0.020 | 0.032 | 0.029 | 0.029 | 0 | 0.029 |
| $a_{1} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0.029 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.029 |
| $a_{2} a_{1}$ | 0.000 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.000 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{2} a_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{2} a_{3}$ | 0.005 | 0.014 | 0.014 | 0.029 | 0.029 | 0 | 0.029 | 0.029 | 0 | 0.029 | 0.005 | 0.014 | 0.014 | 0.029 | 0.029 | 0 | 0.029 |
| $a_{2} a_{4}$ | 0.000 | 0.014 | 0.014 | 0.029 | 0.029 | 0 | 0.029 | 0.029 | 0.029 | 0 | 0.000 | 0.014 | 0.014 | 0.029 | 0.029 | 0 | 0.029 |
| $a_{2} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{3} a_{4}$ | 0 | 0 | 0 | 0.029 | 0 | 0 | 0 | 0 | 0.029 | 0 | 0 | 0 | 0 | 0.029 | 0 | 0 | 0 |
| $a_{3} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{3}$ | 0.004 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.029 | 0.004 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{4}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{4} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $a_{5} a_{1}$ | 0.037 | 0.035 | 0.006 | 0 | 0 | 0.029 | 0 | 0 | 0 | 0 | 0.037 | 0.035 | 0.006 | 0 | 0 | 0.029 | 0 |
| $a_{5} a_{2}$ | 0.034 | 0.040 | 0.021 | 0 | 0 | 0.029 | 0 | 0 | 0.029 | 0 | 0.034 | 0.040 | 0.021 | 0 | 0 | 0.029 | 0 |
| $a_{5} a_{3}$ | 0.046 | 0.054 | 0.045 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.046 | 0.054 | 0.045 | 0.029 | 0.029 | 0.029 | 0.029 |
| $a_{5} a_{4}$ | 0.037 | 0.054 | 0.045 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.037 | 0.054 | 0.045 | 0.029 | 0.029 | 0.029 | 0.029 |
| $a_{5} a_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Based on Eq.1, horizontal summation of every row of the WPI matrix leads to making a $\boldsymbol{p i}$ vector with $\boldsymbol{m}^{2}$ elements. Then by putting this vector values in an $\boldsymbol{m} \times \boldsymbol{m}$ matrix, a preference index value with the name of $\boldsymbol{P I}$ is created as depicted in Table14.

Table 14
PI matrix

|  | $\boldsymbol{a}_{\boldsymbol{1}}$ | $\boldsymbol{a}_{\mathbf{2}}$ | $\boldsymbol{a}_{\mathbf{3}}$ | $\boldsymbol{a}_{\boldsymbol{4}}$ | $\boldsymbol{a}_{\mathbf{5}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{a}_{\boldsymbol{1}}$ | 0 | 0.014 | 0.014 | 0.015 | 0.285 |
| $\boldsymbol{a}_{\boldsymbol{2}}$ | 0.120 | 0 | 0.001 | 0.002 | 0.304 |
| $\boldsymbol{a}_{\mathbf{3}}$ | 0.323 | 0.230 | 0 | 0.038 | 0.657 |
| $\boldsymbol{a}_{\boldsymbol{4}}$ | 0.309 | 0.214 | 0.059 | 0 | 0.640 |
| $\boldsymbol{a}_{5}$ | 0.029 | 0 | 0 | 0 | 0 |

In the first method of PROMETHEE, the priority of alternatives is determined based on the leaving and entering flow based on Eq.8. Alternatives leaving and entering flows are depicted in table 13. So, the fifth city
$\left(\boldsymbol{a}_{5}\right)$ with the greatest leaving values is the best alternative among available 5 alternatives and the ranking of alternatives is mentioned in Fig.2.

Table 15
Leaving\& entering flow of alternatives

|  | $\boldsymbol{a}_{\mathbf{1}}$ | $\boldsymbol{a}_{\mathbf{2}}$ | $\boldsymbol{a}_{\mathbf{3}}$ | $\boldsymbol{a}_{\mathbf{4}}$ | $\boldsymbol{a}_{\mathbf{5}}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Lev_flow | 0.195 | 0.114 | 0.019 | 0.014 | 0.471 |
| Ent_flow | 0.082 | 0.107 | 0.312 | 0.305 | 0.007 |



Fig.2. PROMETHEE I

In PROMETHEE II method, regarding Eq.11, alternatives net flow is computed. These gained results have been depicted in table 14. Based on alternative net-flows, the last alternative with the biggest net-flows is the best option for the budget assignment to establish an industrial facilities center. The alternatives ranking are shown in Fig.3.

For better demonstration, alternatives intervals are illustrated in Fig.4. Considering mentioned explanation, $\boldsymbol{a}_{5}$ is superior to other alternatives and its interval is greater than others. Alternatives $\boldsymbol{a}_{\boldsymbol{1}}$ and $\boldsymbol{a}_{2}$ are in second and third positions but for $\boldsymbol{a}_{3}$ and $\boldsymbol{a}_{4}$ no difference can be expressed. So, alternatives priority is depicted in Fig.5.



Fig.3. PROMETHEE II
In PROMETHEE III, alternatives’ intervals lower and upper bound are obtained based on Eq.15. As it is mentioned before, if alternative lower bound $X a_{i}$ was greater than another alternative upper bound $\boldsymbol{Y a}_{\boldsymbol{j}}$, alternative $\boldsymbol{a}_{\boldsymbol{i}}$ is superior to $\boldsymbol{a}_{\boldsymbol{j}}$. Alternatives interval bounds are shown in table 17 which is used for alternatives ranking.

Table 17
Interval values of alternatives

|  | $\boldsymbol{X}$ | $\boldsymbol{Y}$ |
| :---: | :---: | :---: |
| $\boldsymbol{a}_{\boldsymbol{1}}$ | 0.057 | 0.124 |
| $\boldsymbol{a}_{\mathbf{2}}$ | -0.026 | 0.038 |
| $\boldsymbol{a}_{\mathbf{3}}$ | -0.274 | -0.195 |
| $\boldsymbol{a}_{\boldsymbol{4}}$ | -0.270 | -0.196 |
| $\boldsymbol{a}_{5}$ | 0.331 | 0.411 |

Fig.4. Interval of alternatives


Fig.5. PROMETHEE III
All above, point out that fifth alternative is the best alternative clearly among nominated cities in Qazvin province for a consulting service department establishment.

## 4.Conclusion

In comparative analysis, the ranking results derived by all types of PROMETHEE illustrates that Lia city ( $\boldsymbol{a}_{5}$ ) was the superior than other alternatives. In another word PROMETHEE methods results were to some extent alike. The simplicity of the PROMETHEE methodology as a source for comparing to the other outranking techniques can be considered as one of the main advantages of the PROMETHEE. So based on the method and mentioned
nominated city in the province Qazvin, fifthe alternative accuaired the most desirability to allocate the location for consulting service center. The paper presents a locationallocation decision-making problem resulting in the

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