

A Review of Event-Triggered Control of Fractional-Order Multi-Agent Systems

Fatemeh Gholami ^{1,4}  | Mahnaz Hashemi ^{2,4}  | Ghazanfar Shahgholian ^{3,4} 

¹ Department of Electrical Engineering, Na. C., Islamic Azad University, Najafabad, Iran, gholami_iaun@iau.ac.ir

² Department of Electrical Engineering, Na. C., Islamic Azad University, Najafabad, Iran, mahnazhashemi100@iau.ac.ir

³ Department of Electrical Engineering, Na. C., Islamic Azad University, Najafabad, Iran, shahgholian@iau.ac.ir

⁴ Smart Microgrid Research Center, Na. C., Islamic Azad University, Najafabad, Iran

Correspondence

Dr. Mahnaz Hashemi, Associate Professor of Electrical Engineering, Na. C., Islamic Azad University, Najafabad, Iran
Email: mahnazhashemi100@iau.ac.ir

Main Subjects:

Trigger event control

Paper History:

Received: 23 April 2025

Revised: 19 May 2025

Accepted: 21 May 2025

Abstract

The application of control theory to fractional-order systems has demonstrated superior performance in aspects such as system stability, observability, and controllability. Although extensive research has been conducted on multi-agent systems based on integer-order dynamics, it has been shown that in certain scenarios, ensuring system stability using integer-order models becomes problematic. In such cases, fractional-order modeling provides a more reliable alternative. This paper presents a comprehensive review of recent advances in event-triggered control strategies for fractional-order multi-agent systems. Event-triggered mechanisms are categorized into static and dynamic schemes, based on the nature of the system's dynamic dependencies. Accordingly, the study focuses on key challenges such as the Zeno phenomenon, performance degradation due to increased triggering thresholds, and communication resource constraints. To address these challenges, dynamic and adaptive event-triggered control mechanisms are proposed and discussed.

Keywords: Event-triggered mechanism, Multi-agent system, Fractional-order system, Event-based control.

Highlights

- A review of event-based control for fractional-order multi-agent systems is presented.
- Types of event-based control in systems are classified according to the nature of dependency.
- The importance of event-based control, especially for multi-agent systems, is examined.

Citation: [in Persian].

COPYRIGHTS

©2025 by the authors. Published by the Islamic Azad University Bushehr Branch. This article is an open-access article distributed under the terms and conditions of the Creative Commons Attribution 4.0 International (CC BY 4.0) <https://creativecommons.org/licenses/by/4.0>



1. Introduction

In previous studies, the design of control algorithms has often been based on the assumption of continuous access to communication resources, so that the optimization of multi-agent systems has mainly focused on reducing tracking error or improving stability. However, recent research shows that in operational environments, especially in large-scale networks with distributed sensors and actuators, the requirements of intelligent management of resources such as bandwidth and energy are as critical as the system dynamics themselves. Control approaches are usually designed based on unlimited communication resources, and therefore the exchange of information in control loops is carried out periodically with the startup time of sensors and actuators. Recently, the investigation of event-based control strategies has been considered due to their potential applications in various fields. In the field of control of multi-agent systems, due to the large number of devices, it is very practical and necessary to make the best use of computational, communication, sampling and data transfer resources or control updates. An event-driven control system is a sampling data system in which sampling times are determined by events generated by the system state. Event-driven control requires sampling based on the minimum requirement to maintain desired control performance. Despite the advantages of event-driven control, implementing event-driven control for systems is not without challenges. Issues such as input saturation, fault occurrence, and controller design complexity can compromise performance and stability [1-7].

2. Innovation and contributions

In this review article, event-based control for fractional-order multi-agent systems is briefly discussed, and the evolutionary path of proposed control approaches in recent years is examined. First, a background of the application of event-based control is presented, and then, in continuation of the review of previous research, event-based approaches in integer-order and fractional-order multi-agent systems are examined. Also, the advantages and disadvantages of the approaches used are stated. In summary, the highlights of this study are:

- An examination of event-based control for fractional-order multi-agent systems is presented.
- Types of event-based control in systems are classified according to the nature of dependency.
- The importance of event-based control, especially for multi-agent systems, is examined.

3. Materials and Methods

Event-based control plays a fundamental role in reducing resource consumption and reducing operator depreciation. Each event structure consists of two parts: an error function and a threshold function. Based on the type of event threshold function, it is classified into two categories: static and dynamic. In terms of the nature of the dependence or non-dependence of the event structure on the system dynamics, event-based control can be classified into two categories: static event-based control and dynamic event-based control [8-13].

Zeno phenomenon is one of the challenges of event-based control. This phenomenon occurs when the system is out of equilibrium and the number of controller updates increases indefinitely. In such a case, an infinite number of events occur in a very short time interval, and in this case, event-based control becomes inefficient. Therefore, during the controller design, it must be proven analytically that Zeno phenomenon does not occur [14-16].

Since most of the studies initially used a fixed event structure, these structures are simple to design but less efficient in dealing with dynamic system changes. On the other hand, with the reduction in resource usage, it is not far from the fact that the overall performance of the control system will decrease to some extent, because less data is transmitted from the controller to the actuator. To address the challenge of reducing system performance with increasing threshold parameter, researchers have been looking for a way to reduce the number of events without sacrificing too much control performance, one solution being to increase the threshold function for the startup condition by adding a non-negative auxiliary dynamic variable. In fact, the difference between static and dynamic event-based control is in the event structure of each. Static event-based control is based on a fixed error threshold or a decreasing exponential function [17-19].

Fractional calculus is a growing research area due to its many applications in various fields of science and engineering. Since the advent of fractional calculus tools, countless literatures have been written, which have also improved the efficiency of control loops due to the improvement of modeling and improving the efficiency of controllers. Due to the high accuracy of fractional-order modeling for systems, many applications of applied systems, such as social networks and a fleet of spacecraft, unmanned underwater vehicles moving in the depths of the sea, and unmanned aircraft flying in dust storms, rain, or snow, can be considered as fractional-order systems. Also, many approaches to control integer-order nonlinear systems have been generalized to fractional-order nonlinear systems [20-23].

Multi-agent systems have attracted the attention of researchers in recent decades due to their wide applications in various sciences including applied mathematics, computer science and engineering. The collaborative control of these systems includes issues such as consensus, orchestration, containment, etc. Multi-agent systems with orchestration mode are systems in which agents are organized in a structured manner to achieve common goals. This configuration can be fixed or variable. Containment also means the control or restriction of agents by several leader agents to prevent undesirable and inconsistent behaviors. Consensus is also one of the important and vital

areas in the collaborative control of multi-agent systems, which is achieved when the follower agents agree on a common desired point by following the control rules and communicating with their neighbors. Leader-controlled consensus and leaderless consensus are two distinct approaches to achieving group consensus [24-32].

In recent years, the distributed event-based control approach for fractional-order multi-agent systems has attracted much attention from researchers and scholars in the control community due to its various advantages compared to the conventional time-based approach. Due to some limitations and technical challenges in controller design and stability analysis in fractional-order systems, the extension of event-based control protocols from integer-order multi-agent systems to fractional-order multi-agent systems has been slow, and very few research results have been reported in this field so far.

4. Results and Discussion

Despite the significant growth of research in the field of event-based control, this approach still faces several fundamental challenges, which prevent its widespread and practical implementation in industrial and complex applications. The most important of these challenges are the lack of a comprehensive theoretical framework for analyzing stability and efficiency, especially in distributed nonlinear fractional-order multi-agent systems, with guaranteed stability in the presence of delay and noise, prevention of Zeno behavior, robust designs, and the lack of experimental results and key practical challenges such as time delays and operator defects remain as major obstacles. On the other hand, the lack of practical experiments and experimental results and practical scenarios indicate a significant gap between theory and application. These challenges indicate that despite theoretical advances, the field for further research towards the practical realization of this approach is still vast and vital.

In summary, the research path based on the existing challenges can be stated as follows:

- Development of dynamic event-based methods for complex fractional-order systems
- Designs resistant to time delays and operator defects
- Development of frameworks that can be implemented in industry
- Increasing real-world experiences and practical tests to prove theoretical benefits in industrial conditions

5. Conclusion

By reviewing the research background in the field of event-based control of fractional-order multi-agent systems, it is observed that most of the existing studies have focused on simple linear or nonlinear systems, therefore, the design of event-based controllers for complex fractional-order nonlinear multi-agent systems can be investigated. Another limitation in previous research is the use of static event structures in most cases, which leads to unnecessary updates, and another gap in this regard is the lack of investigation of the effect of hardware defects such as locking defects or loss of efficiency defects in operators on the stability of fractional-order multi-agent systems has rarely been analyzed. Therefore, the investigation of dynamic event-based control for fractional-order multi-agent systems in the presence of operator defects can be considered. According to the research conducted, the application of dynamic event-based methods in fractional-order systems with complex structures, the expansion of implementation in industry, and robust design can be mentioned as challenges and future research directions.

6. Acknowledgement

This paper is an extract from a doctoral dissertation at the Islamic Azad University, Najafabad Branch. The authors would like to express their gratitude to the respected colleagues of the journal and the respected reviewers. They would also like to express their gratitude to the respected colleagues in the Research and Technology Department of the Najafabad Branch.

References

- [1] M. Parsa and M. Danesh, "Robust containment control of uncertain multi-agent systems with time-delay and heterogeneous lipschitz nonlinearity", *IEEE Trans. on Systems, Man, and Cybernetics: Systems*, vol. 51, no. 4, pp. 2312-2321, April 2021, doi: 10.1109/TSMC.2019.2912268.
- [2] F. Gholami, M. Hashemi and G. Shahgholian, "Actuator fault event-triggered compensation for multiagent fractional-order nonlinear systems", *Signal Processing and Renewable Energy*, vol. 9, no. 1, Article Number: 092503, March 2025, doi: 10.57647/j.spre.2025.0901.03.
- [3] M. Chafii, S. Naoumi, R. Alami, E. Almazrouei, M. Bennis and M. Debbah, "Emergent communication in multi-agent reinforcement learning for future wireless networks", *IEEE Internet of Things Magazine*, vol. 6, no. 4, pp. 18-24, Dec. 2023, doi: 10.1109/IOTM.001.2300102.
- [4] J. Chai, P. Casau and R.G. Sanfelice, "Analysis and design of event-triggered control algorithms using hybrid systems tools", *International Journal of Robust and Nonlinear Control*, vol. 30, no. 15, pp.5936-5965, Oct. 2020, doi: 10.1002/rnc.5141.

- [5] S.K. Mishra, A.V. Jha, V.K. Verma, B. Appasani, A.Y. Abdelaziz and N. Bizon, "An optimized triggering algorithm for event-triggered control of networked control systems", *Mathematics*, vol. 9, no. 11, Article Number: 1262, May 2021, doi: 10.3390/math9111262.
- [6] F. Mohammadzamani, M. Hashemi and G. Shahgholian, "Adaptive neural control of non-linear fractional order multi-agent systems in the presence of error constraints and input saturation", *IET Control Theory and Applications*, vol. 16, no. 13, pp. 1283-1298, Sept. 2022, doi: 10.1049/cth2.12291.
- [7] X. Meng, B. Jiang, H.R. Karimi and C. Gao, "Leader–follower sliding mode formation control of fractional-order multi-agent systems: A dynamic event-triggered mechanism", *Neurocomputing*, vol. 557, pp. 126691, Nov. 2023, doi: 10.1016/j.neucom.2023.126691.
- [8] D.N.M. Abadi, A. Moarefianpour and N.M. Dehkordi, "Finite-time bounded model-based event-triggered control for distributed fuzzy T-S systems", *Majlesi Journal of Electrical Engineering*, vol. 18, no. 1, March 2024, doi: 10.30486/mjee.2023.1994207.1226.
- [9] J. Yang, Q. Zhong, X. Liu, K. Shi, A.M.Y.M. Ghias and Z.Y. Dong, "Decentralized periodic event-triggered load frequency control for multiarea power systems", *IEEE Trans. on Systems, Man, and Cybernetics: Systems*, vol. 55, no. 2, pp. 1020-1030, Feb. 2025, doi: 10.1109/TSMC.2024.3493102.
- [10] D. Huong, T. Van and T. Hieu, "On static and dynamic triggered mechanisms for event-triggered control of uncertain systems", *Circuits, Systems, and Signal Processing*, vol. 39, no. 10, pp. 5020-5038, Oct. 2020, doi: 10.1007/s00034-020-01399-6.
- [11] A. Yesmin, A.K. Behera, M.K. Bera and B. Bandyopadhyay, "Dynamic event-triggering based design of sliding mode control", *International Journal of Robust and Nonlinear Control*, vol. 31, no. 12, pp. 5910-5925, Aug. 2021, doi: 10.1002/rnc.5604.
- [12] J. Chen, D. Yue, C. Dou, S. Weng, X. Xie, Y. Li and G. P.Hancke, "Static and dynamic event-triggered mechanisms for distributed secondary control of inverters in low-voltage islanded microgrids", *IEEE Trans. on Cybernetics*, vol. 52, no. 7, pp. 6925-6938, Dec. 2020, doi: 10.1109/TCYB.2020.3034727.
- [13] S. Shi, S. Miyata and Y. Akashi, "Event-driven model-based optimal demand-controlled ventilation for multizone VAV systems: Enhancing energy efficiency and indoor environmental quality", *Applied Energy*, vol. 377, Article Number: 124683, Jan. 2025, doi: 10.1016/j.apenergy.2024.124683.
- [14] M. Saghafi-Zanjani nad S. Mobayen, "Event-triggered global sliding mode controller design for anti-sway control of offshore container cranes", *Ocean Engineering*, vol. 268, Article Number: 113472, Jan. 2023, doi: 10.1016/j.oceaneng.2022.113472.
- [15] A.T. Nguyen, T.B. Nguyen and S.K. Hong, "Dynamic event-triggered time-varying formation control of second-order dynamic agents: application to multiple quadcopters systems", *Applied Sciences*, vol. 10, no. 8, Article Number: 2814, April 2020, doi: 10.3390/app10082814.
- [16] S. Koga, C. Demir and M. Krstic, "Event-triggered safe stabilizing boundary control for the Stefan PDE system with actuator dynamics", *Proceeding of the IEEE/ACC*, pp. 1794-1799, San Diego, CA, USA, May 2023, doi: 10.23919/ACC55779.2023.10156551 IEEE.
- [17] A. Girard, "Dynamic triggering mechanisms for event-triggered control", *IEEE Trans. on Automatic Control*, vol. 60, no. 7, pp. 1992–1997, Nov. 2014, doi: 10.1109/TAC.2014.2366855.
- [18] S. Hu, Y. Dong, X. Yu, X. Xiangpeng and M. Yong, "Adaptive event-triggered control for nonlinear discrete-time systems", *International Journal of Robust and Nonlinear Control*, vol. 26, no. 18, pp. 4104–4125, Dec. 2016, doi: 10.1002/rnc.3550.
- [19] W. Du, X. Yi, J. George, K.H. Johansson and T. Yang, "Distributed optimization with dynamic event-triggered mechanisms", *Proceedings of the IEEE/CDC*, pp. 969–974, Miami, FL, USA, Jan. 2019, doi: 10.1109/CDC.2018.8619311.
- [20] Y. Zhan, S. Sui and S. Tong, "Adaptive fuzzy decentralized dynamic surface control for fractional-order nonlinear large-scale systems", *IEEE Trans. on Fuzzy Systems*, vol. 30, pp. 3373–3383, Sep. 2021, doi: 10.1109/TFUZZ.2021.3114746.
- [21] A.B. Albidah, "Application of riemann–liouville derivatives on second-order fractional differential equations: The exact solution. fractal and fractional", vol. 7, no. 12, Article Number: 843, Nov. 2023, doi: 10.3390/fractalfract7120843.
- [22] A. Naderolasli, M. Hashemi and K.H. Shojaei, "Approximation-based adaptive fault compensation backstepping control of fractional-order nonlinear systems: an output-feedback scheme", *International Journal of Adaptive Control and Signal Processing*, vol. 34, no. 3, pp. 298–313, Mar. 2020, doi: 10.1002/acs.3084.
- [23] R. Kavikumar, O.M. Kwon, S.H. Lee and R. Sakthivel, "Input-output finite-time IT2 fuzzy dynamic sliding mode control for fractional-order nonlinear systems", *Nonlinear Dyn.*, vol. 108, no. 4, pp. 3745–3760, June 2022, doi: 10.1007/s11071-022-07442-2.
- [24] X. Dong, B. Yu, Z. Shi and Y. Zhong, "Time-varying formation control for unmanned aerial vehicles: Theories and applications", *IEEE Trans. on Control Systems Technology*, vol. 23, no. 1, pp. 340–348, Apr. 2014, doi: 10.1109/TCST.2014.2314460.

- [25] B. Wang and A. Loria, "Leader-follower formation and tracking control of underactuated surface vessels", arXiv preprint arXiv:2407.18844, Jul. 2024 doi: 10.48550/arXiv.2407.18844.
- [26] J. Sui, C. Liu, B. Niu, X. Zhao, D. Wang and B. Yan, "Prescribed performance adaptive containment control for full-state constrained nonlinear multiagent systems: A disturbance observer-based design strategy", IEEE Trans. on Automation Science and Engineering, vol. 22, pp. 179–190, June 2024, doi: 10.1109/TASE.2023.3348978.
- [27] T. Balch and R.C. Arkin, "Behavior-Based Formation Control for Multi-Robot Teams", IEEE Trans. on Robotics and Automation, vol. 14, no. 6, pp. 926–939, Dec. 1998, doi: 10.1109/70.736776.
- [28] M.A. Lewis and K.H. Tan, "High precision formation control of mobile robots using virtual structures", IEEE Trans. on Robotics and Automation, vol. 18, no. 1, pp. 113–125, Feb. 2002, doi: 10.1109/70.988979.
- [29] Z. Li, Z. Duan, W. Ren and G. Feng, "Containment control of linear multi-agent systems with multiple leaders of bounded inputs using distributed continuous controllers", International Journal of Robust and Nonlinear Control, vol. 25, no. 13, pp. 2101–2121, Sep. 2015, doi: 10.1002/rnc.3195.
- [30] P. Ali, M. Rehan, W. Ahmed, A. Basit and I. Ahmed., "A novel output feedback consensus control approach for generic linear multi-agent systems under input saturation over a directed graph topology", ISA Transactions, vol. 148, pp. 128–139, May 2024, doi: 10.1016/j.isatra.2024.02.029.
- [31] F. Muñoz, "Leader–follower consensus control for a class of nonlinear multi-agent systems using dynamical neural networks", Neurocomputing, vol. 561, pp. 126888, Dec. 2023, doi: 10.1016/j.neucom.2023.126888.
- [32] J. Huang, W. Wang, C. Wen, J. Zhou and G. Li, "Distributed adaptive leader–follower and leaderless consensus control of a class of strict-feedback nonlinear systems: A unified approach", Automatica, vol. 118, Article Number: 109021 Aug. 2020, doi: 10.1016/j.automatica.2020.109021.

Declaration of Competing Interest: Authors do not have conflict of interest. The content of the paper is approved by the authors.

Author Contributions:

Fatemeh Gholami: Methodology, researcher, writing original draft preparation; **Mahnaz Hashemi:** Thesis supervisor, methodology, manuscript editing; **Ghazanfar Shahgholian:** Thesis advisor, manuscript editing.

Open Access: Journal of Southern Communication Engineering is an open access journal. All papers are immediately available to read and reuse upon publication.