

## Corrigendum to "On $(\sigma, \tau)$ -module extension Banach algebras"

M. Fozouni\*

<sup>a</sup>Department of Mathematics, Gonbad Kavous University, P.O. Box 163, Gonbad Kavous  
Golestan, Iran.

Received 3 October 2017; Revised 14 November 2017; Accepted 10 December 2017.

Communicated by Ghasem Soleimani Rad

---

**Abstract.** In this corrigendum, we give a correction of one result in reference [1].

© 2018 IAUCTB. All rights reserved.

---

**Keywords:** Banach algebra, module extension.

**2010 AMS Subject Classification:** 46H20, 46H25, 46H10, 47B48.

The proof of Theorem 2.4, part (ii) of [1] is not correct. Indeed, the proof of  $I \times J \subseteq M$  is wrong, because we take  $a_0 \in I$ ,  $x_0 \in J$  and then conclude that

$$(a_\alpha, 0) \cdot (a_0, x_0) = (a_\alpha a_0, \sigma(a_\alpha) \cdot x_0) \rightarrow (a_0, x_0).$$

Our mistake happen here, since we assume that  $(a_\alpha, 0) \cdot (a_0, x_0)$  is in  $M$  and closedness of  $M$  implied that  $(a_0, x_0) \in M$ . But, generally  $(a_\alpha, 0) \cdot (a_0, x_0)$  is not in  $M$ .

But, if the left module action of  $X$  is zero, then we have  $M = I \times J$ . To see this, let  $a_0 \in I$ . So, there exists an  $x \in X$  such that  $(a_0, x) \in M$  and by  $x_0 \in J$ , there exists an  $a \in A$  such that  $(a, x_0) \in M$ . Now

$$(a_\alpha, 0) \cdot (a_0, x) = (a_\alpha a_0, 0) \rightarrow (a_0, 0) \in M$$

$$(a_\alpha, 0) \cdot (a, x_0) = (a_\alpha a, 0) \rightarrow (a, 0) \in M$$

$$(a, x_0) - (a, 0) = (0, x_0) \in M.$$

---

\*Corresponding author.

E-mail address: fozouni@gonbad.ac.ir (M. Fozouni).

Therefore,  $(a_0, x_0) \in M$ . Now, one can remove the hypothesis that  $(\sigma(a_\alpha))$  is a left approximate identity for  $X$ .

### **Acknowledgements**

The author would like to thank professor Abasalt Bodaghi who has pointed out this error and its correction.

### **References**

- [1] M. Fozouni,  $(\sigma, \tau)$ -module extension Banach algebras, *J. Linear. Topological. Algebra.* 3 (04) (2014), 185-194.