RESEARCH

Ripple transport and neoclassical difusion in IR‑T1 tokamak

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Abstract

In tokamaks, small variations in the magnetic feld create ripple. The discontinuous nature of the magnetic feld coils in an axisymmetric torus conduces to additional particle trapping, and it is responsible for an additional neoclassical difusion. Ripples also reduce the particle removal efficiency and disturb plasma confinement and cause constraints in the design of magnet of fusion reactor. Therefore, it is quite important to include the ripple for the design of plasma edge components. Herein, several considerations are taken into account to calculate and evaluate the diffusion coefficient and ion heat conductivity in ripple transport and also to compare it with neoclassical mode.

Keywords Neoclassical diffusion · Ripple magnetic field · Ripple transport · Diffusion coefficient · Diffusivity · Ion heat conductivity

Introduction

The axisymmetry of the magnetic feld has been assumed as one of the substantial advantages of tokamaks. Apart from the simplicity of analysis, the radial motion of particles trapped in low collision frequencies is less than that of asymmetric felds [\[1\]](#page-6-0).

It is expected that in an axisymmetric magnetic feld confguration of a tokamak D-T reactor, fusion-produced alpha particles are well confined and thus provide for efficient internal plasma heating. The presence of magnetic perturbations, however, may greatly afect the retention of these particles and lead to their loss from the confnement region [\[2](#page-6-1)].

Small variations in the magnetic feld are called magnetic ripple. In practice, the discrete nature of the magnetic feld of the toroidal coils around the torous creates a ripple in the feld intensity with a period equal to the distance between the centers of the coils. This perturbation is toroidal feld ripple (TFR).

Ripple has negative efects on fusion plasma performance including the fusion energy reduction due to particle loss, the plasma beta reduction and the rotation break. Generally,

various magnetic perturbations like toroidal feld ripples can degrade fast ions confnement. In the outer region of tokamak plasmas due to loose winding of toroidal coils, TF ripples have strongest efect and can cause fast ions to loose very quickly which in turn can also damage the frst wall of the tokamak $[2-5]$ $[2-5]$.

The ripple strength not only enhances the difusion coefficient but also changes the energy dependence $[6]$ $[6]$.

An ideal, axisymmetric tokamak has no ripple. In real-life machines, the fnite widths of the toroidal feld coils create a periodic ripple [\[7\]](#page-6-4).

Deviation from the symmetry is generally considered to be fddling. This efect will be more important probably in the next generation of machines, for two reasons. It is expected to reach higher temperatures which is accompanied by upsurging of asymmetry efect as the frequency of collision reduces. In some collisional regime for the present and next generation of tokamaks, the ripple difusion changes inversely to frequency of collision [\[1\]](#page-6-0).

In ["Ripple transport"](#page-1-0) section, we discuss about the ripple transport and the ripple magnetic feld in the toroidal coordinate and superbanana difusion. In ["A solution of the](#page-2-0) [Fokker–Planck equation for trapped particles in the mag](#page-2-0)[netic feld ripples](#page-2-0)" and ["Difusion and heat transport"](#page-3-0) sections, the Fokker–Planck equation is presented for particles trapped in the ripple magnetic feld and the equations for the particle fux and heat fux are obtained to calculate the diffusion coefficient and the ion heat conductivity and finally

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transport coefficients are compered in neoclassical and ripple mode for IR-T1 tokamak.

Ripple transport

The ripple transport is due to the drift motion of particles distributed in the ripple of a magnetic feld. The moderate number of toroidal feld coils of a tokamak expunges the perfect axial symmetry of the system. The coils create a short wavelength in the magnetic feld strength, namely "ripple," as a feld line is pursued around the torus.

For *N* coils, the magnetic field can be presented by

$$
B = B_0(1 - \varepsilon \cos \theta)(1 - \delta(r, \theta) \cos N\phi)
$$
 (1)

where θ is the poloidal angle circa the magnetic axis, ϕ indicates the angular distance around the axis of symmetry, *r* is the radial distance from the magnetic axis, R is the radius of the magnetic axis and $\varepsilon = r/R$ is the inverse aspect ratio.

An estimation for the value of δ , for the case of strongly elongated toroidal feld coils, is defned by

$$
\delta = \left(\frac{R}{R_{\text{outer}}}\right)^N + \left(\frac{R_{\text{inner}}}{R}\right)^N,
$$

where R_{outer} and R_{inner} are, respectively, the major radii of the outer and inner legs of the toroidal coils space [[3\]](#page-6-5).

For a particle to be trapped in the ripple wells it has to satisfy the condition that the parallel velocity sufficiently small that magnetic mirror refection occurs in the ripple well. This is equivalent to the statement that the banana turning point positions of the particles lie inside the ripple well region. Particles are trapped into and re-trapped out of ripple well by collisional processes, in particular by pitchangle scattering, which change the ratio between the parallel and perpendicular velocities. The typical residence time of a particle in ripple well is of the order $\Delta t \sim \delta/v$, where *v* is the collisional defection frequency. The fraction of particles which is ripple well trapped is of order $\delta^{1/2}$.

Due to the toroidal feld gradient drift, the trapped particles in the ripple well drift vertically with a velocity of $v_d \sim \rho v/R$ where ρ is the Larmor radius and *v* is the total particle velocity. Incorporating the ripple well trapped fraction, the drift velocity and the residence time, a difusion coefficient for collisional ripple well transport can be estimated as:

$$
D \sim \delta^{1/2} \left(\frac{\rho v \delta}{R v}\right) \frac{v}{\delta} \sim \frac{\delta^{3/2} \rho^2 v^2}{R^2 v} \tag{2}
$$

where D is radial diffusion coefficient for a circular plasma, averaged over the pitch angle. This implies a greater loss rate for ions than for electrons, and an ambipolar electric feld will evolve to reduce the ion particle difusion. Nevertheless, Eq. [\(2](#page-1-1)) remains an appropriate estimate. It should, however, be noted that its validity is restricted to collision frequencies $v > v_d \delta/a$, where *a* is plasma minor radius; otherwise, particles would drift out of the plasma before sufering a collision, producing a loss cone in velocity space rather than a difusion. This restriction is particularly stringent as *D* which is dominated by contributions from the more energetic particles, so that the inequality must hold for these particles. (Energies are approximately fve times the plasma temperature.) The proper poloidal averaging procedure leads to a signifcant reduction of *D* from that given in Eq. [\(2](#page-1-1)) [\[3](#page-6-5)].

The ripple-induced difusion is diferent from the superbanana difusion in stellarators. Stringer has given an ample argument of this diference which becomes evident at small values of *N* [\[3\]](#page-6-5). He showed that for values of $\alpha = \varepsilon t / N \delta$ (*t* is the rotational transformation) in excess of unity the ripple does not outcome in the constitution of local magnetic mirrors and resultant trapping over the whole minor azimuth, and that, generally for α of order unity, considerable diminution of the mirror depth arises at all angles. This can be seen from Eq. [\(1](#page-1-2)) by noting minimum in B_l (where *l* is arc length along a field line) arise only if $\alpha \sin \theta < 1$. Even when this retains, each ripple is an asymmetric mirror with mirror rotation $R_+(\theta)$ where

$$
(R_--1)<2\delta<(R_+-1)
$$

Therefore, a well depth $\Delta(\theta) \equiv (R_ - 1)$ is given by

$$
\Delta(\theta) = 2\delta[\sqrt{1 - \alpha^2 \sin^2 \theta} - \alpha \left\{ \frac{\pi}{2} - \sin^{-1}(\alpha|\sin \theta|) \right\} |\sin \theta|]
$$
\n(3)

Stringer's estimation of the decrease in difusion and ion heat fux is attained by including this decrease in the well depth from 2δ to $\Delta(\theta)$. Though this effect is a highly important factor, it undermines the asymmetric distortion of the ripple wells. In the next part, here we offer the solution of the Fokker–Planck equation for the ripple-trapped distribution, and then we deduced the resultant transport coefficients.

The analysis offered is right in the main range of collision frequencies v_j given by

$$
\frac{\delta^{1/2}v_{\text{Th}_j}^N}{R} > \frac{v_j}{\delta} > \frac{v_{\text{Th}_j}^2 \delta}{\omega_{cj}r^2}
$$
(4)

where v_{Th_j} is the thermal speed of species *j* and ω_{cj} is the gyrofrequency. Physically, it means that the effective collision frequency $v_{\text{eff}} = v/\delta$ is less than the bounce time of a ripple-trapped particle $\omega_b = \delta^{1/2} v_{\text{Th}} N/R$, but higher than the drift frequency circa of a complete superbanana orbit in the mirror azimuth of the torus $[8-11]$ $[8-11]$.

A solution of the Fokker–Planck equation for trapped particles in the magnetic feld ripples

Collision frequencies in range [\(4](#page-1-3)) can be considered by writing a kinetic equation which presumes the jump frequency and effective collision frequency $v_{\text{eff}} = v/\delta$ are comparable and then writing a secondary expansion in v_{eff}/ω_b . We define the distribution function f_j which is the average amount over a gyro-period of the Larmor radius to a Maxwellian F_j that satisfies Eq. [\(5](#page-2-1)):

$$
\sigma q \vec{n} \cdot \nabla f_j + \vec{v}_{dj} \cdot \nabla F_j = C(f_j)
$$
\n(5)

where

$$
F_j = \left(\frac{m_j}{2\pi T_j(r)}\right)^{3/2} n_j(r) \exp\left(\frac{m_j \kappa}{T_j(r)}\right)
$$
(6)

And the kinetic energy per unit mass is $\kappa = v^2/2$, and σ is the sign of the velocity *q* along the field. The gradient operators in Eq. (5) (5) are taken into account at constant energy

$$
W = \frac{v^2}{2} + \frac{e_j \Phi(r)}{m_j}
$$

where $\Phi(r)$, as a function of radius, is an electrostatic potential. The drift velocity \vec{v}_{di} is given by

$$
\vec{v}_{dj} = \frac{1}{\omega_{c_j}} \vec{n} A(\mu \nabla B + q^2 \vec{n} \cdot \nabla \vec{n}) - \frac{\nabla \Phi AB}{B^2}
$$
(7)

where \vec{n} is a unit vector along the field and the magnetic moment is expressed by μ . We know $\kappa = q^2/2 + \mu B$.

To acquire a dissolvable equation for f_j , we exchange the $C(f_j)$ by an ordinary pattern. For electron–ion collision, we can apply the Lorentz approximation

$$
C_{\rm ei}(f_{\rm e}) = v_{\rm ei}(\kappa) \frac{q}{B} \frac{\partial}{\partial \mu} q \mu \frac{\partial}{\partial \mu} f_{\rm e}
$$
 (8)

However, ion–electron collisions may be waivered in comparison with ion–ion collisions. The two like-particle collision operators C_{ee} and C_{ii} may also be exchanged by operators similar to expression ([8\)](#page-2-2), videlicet

$$
C_{jj}(f_j) = v_{jj}(\kappa) \frac{q}{B} \frac{\partial}{\partial \mu} q \mu \frac{\partial}{\partial \mu} f_j + v_{jj}(\kappa) q F_j \frac{p_j m_j}{T_j}
$$
(9)

with

$$
p_j = \frac{\int d^3 v v_{jj}(k) q f_j}{\frac{m_j}{T_j} \int d^3 v v_{jj}(k) q^2 f_j}
$$

An explanation of this form is that it may be taken from the Rosenbluth–McDonald–Judd form for distributions f_j localized in velocity space, as in the current case. The term containing p certifes momentum conservation but may be waivered here, and for a localized distribution, its portion is small. This term is needed in the axial symmetric case where momentum conservation plays a signifcant role. Eventually, we need to defne the collision frequencies as:

$$
v_{jk}(\kappa) = \frac{\sqrt{2\pi} \, n \, e^4 \lambda}{m_j^{1/2} T_j^{3/2}} A_{jk}(x_j)
$$
 (10)

where $x_j(\kappa) = m_{jk}/T_j$,

$$
A_{jk}(x_j) = \left(\eta_k + \eta'_k - \frac{\eta_k}{2x_k}\right) x_j^{-3/2}
$$
 (11)

With

$$
\eta_k(x_k) = \frac{2}{\sqrt{\pi}} \int_0^{x_k} e^{-t} t^{1/2} dt, \ \eta'_k = \frac{d\eta}{dx_k}
$$

obviously in A_{ei} , $x_i \gg x_e$, therefore

$$
A_{\rm ei}(x_{\rm e}) = x_{\rm e}^{-3/2} \tag{12}
$$

Coming back to the solution of kinetic equation (5) (5) , we need to consider the slow alteration in θ over a ripple period by using the field line equation $\theta = \theta_0 + t\phi$, where θ_0 is a reference angle for each feld line. Then, by introducing the variable θ_0 clearly into the basic kinetic equation, the first term can be expressed as:

$$
\sigma q \vec{n} \cdot \nabla f_j = \frac{\sigma q}{R} \frac{\partial f_j}{\partial \phi} \tag{13}
$$

and the second term is

$$
\vec{v}_d \cdot \nabla F_j = -\frac{B_0}{\omega_{c_j}} \left(\frac{q^2 + \mu B}{B} \right) \frac{1}{R}
$$
\n
$$
\times \frac{\partial F_j}{\partial r} \sin(\theta_0 + t\phi) + O(\varepsilon^2)
$$
\n(14)

We look for a solution for those particles trapped in a mag-netic field ripple, and for these, we expend Eq. ([5\)](#page-2-1) in v_{eff}/ ω_b . The term $\sigma q/R$ $\partial f_j/\partial \phi$ could be expunged by operator $\sum_{\sigma} \int_{\phi_1}^{\phi_2}$ d*𝜙* q^q where $q(\phi_1) = q(\phi_2)$. Unless, we make the ansatz

$$
f = \frac{\omega_b}{v_{\text{eff}}} i^{(-1)} + f^{(0)} + \frac{v_{\text{eff}}}{\omega_b} f^{(1)} + \dots
$$
 (15)

We get an inconsistence since

$$
\sum_{\sigma} \int_{\phi_1}^{\phi_2} \frac{\mathrm{d}\phi}{q} \vec{v}_{d_j} \cdot \nabla F_j \neq 0
$$

with the expansion (15) (15) (15) we see in the lowest order

$$
\frac{\partial f_j^{(-1)}}{\partial \phi} = 0\tag{16}
$$

And in the frst order, after applying the annihilator, one gets the following equation for $f_j^{(-1)}$:

$$
-\frac{\partial F_j}{\partial r} \frac{B_0}{\omega_{co_j}^R} \int_{\phi_1}^{\phi_2} \frac{d\phi (q^2 + \mu B)}{q} \sin(\theta_0 + t\phi)
$$

=
$$
\sum_{\kappa} v_{j\kappa}(\kappa) \frac{\partial}{\partial \mu} \frac{\mu}{B} J \frac{\partial f_j^{(-1)}}{\partial \mu}
$$
 (17)

where

$$
J \equiv \int_{\phi_1}^{\phi_2} q \, \mathrm{d}\phi
$$

=
$$
\int_{\phi_1}^{\phi_2} \sqrt{2[\kappa - \mu B(1 - \delta \cos N\phi - \varepsilon \cos(\theta_0 + t\phi))]} \, \mathrm{d}\phi
$$
 (18)

On the left-hand side of Eq. ([17\)](#page-3-1), considering $X = N\phi$ as the variable of integration with a range of less than 2π , we will have

$$
\sin(\theta_0 + t\phi) = \sin\left(\theta_0 + \frac{t}{N}X\right) \sim \sin\theta_0 + O\left(\frac{1}{N}\right)
$$

And since $\frac{\partial(\mu J)}{\partial \mu} = -\int_{\phi_1}^{\phi_2} \frac{d\phi}{q} (\mu B - q^2)$.
And $\frac{q^2}{\mu B} \sim O(\delta)$.
Equation (17) is as follows:

$$
\frac{\partial F_j}{\partial r} \frac{1}{\omega_{co_j}^R} \sin \theta_0 \frac{\partial}{\partial \mu} \mu J
$$
\n
$$
= \frac{\partial}{\partial \mu} \frac{\mu}{B_0} J \frac{\partial f_j^{(-1)}}{\partial \mu} \left(\sum_{\kappa} v_{j\kappa}(\kappa) \right) O\left(\delta, \frac{1}{N}\right)
$$
\n(19)

The suitable solution of this equation in the range of κ $\frac{\kappa}{B_{\text{max}}} < \mu < \frac{\kappa}{B_{\text{max}}}$ $\frac{\lambda}{B_{\min}}$ is

$$
f_j^{(-1)} = \frac{\partial F_j}{\partial r} \frac{m_j}{e_j} \frac{1}{R} \sin \theta_0 \left(\mu - \frac{\kappa}{B_{\text{max}}}\right) \frac{1}{\sum_{\kappa} v_{j\kappa}(\kappa)}
$$
(20)

where B_{max} is given by [\[10](#page-6-8)]

$$
\frac{B_{\text{max}}}{B_0} = 1 - \varepsilon \cos \theta_0 + \delta \left\{ \sqrt{1 - \alpha^2 \sin^2 \theta_0} - \alpha |\sin \theta_0| \left[\pi - \sin^{-1}(\alpha |\sin \theta_0|) \right] \right\}
$$
\n(21)

Difusion and heat transport

The particle difusion fux is defned as

$$
\Gamma_j = \int\limits_0^{2\pi} \frac{\mathrm{d}\theta}{2\pi} \int\limits_0^{2\pi} \frac{\mathrm{d}\phi}{2\pi} \sum\limits_{\sigma} \int\limits_0^{\infty} 2\pi \mathrm{d}\kappa \int\limits_{\kappa/B\max}^{\kappa/B} \frac{B d\mu}{q} f_j^{(-1)} \nu \mathrm{d}r_j, (22)
$$

and the ion heat fux is defned as

$$
Q_i = \int\limits_0^{2\pi} \frac{\mathrm{d}\theta}{2\pi} \int\limits_0^{2\pi} \frac{\mathrm{d}\phi}{2\pi} \sum\limits_{\sigma} \int\limits_0^{\infty} 2\pi \mathrm{d}\kappa \int\limits_{\kappa/B\max}^{\kappa/B} \frac{B d\mu}{q} f_i^{(-1)} m_i \kappa \nu \mathrm{d}r_i
$$
\n(23)

where
$$
\mathbf{v} dr_j = -\frac{\kappa}{\omega_{eq} R} \sin \theta_0
$$
 and
\n
$$
F_j = \left(\frac{m_j}{2\pi T_j(r)}\right)^{3/2} n_j(r) \exp\left(\frac{m_j \kappa}{T_j(r)}\right), x_j = m_{jk}/T_j, \ \kappa = v^2/2
$$
\n(24)

And

$$
f_j^{(-1)} = \frac{\partial F_j}{\partial r} \frac{m_j}{e_j} \frac{1}{R} \sin \theta_0 \left(\mu - \frac{\kappa}{B_{\text{max}}}\right) \frac{1}{\sum v_{jk}(\kappa)}\tag{25}
$$

$$
\Gamma_{j} = -\frac{A}{(2\pi)^{3/2}} \left(\frac{T_{j}}{eBR}\right)^{2} \int_{0}^{\infty} \frac{dx_{j} x_{j}^{5/2} e^{-x_{j}}}{\sum_{k} v_{jk}(x_{j})}
$$
\n
$$
\left[\frac{n'_{j}}{n_{j}} + \frac{e_{j} \Phi'}{T_{j}} - \left(\frac{3}{2} - x_{j}\right) \frac{T'_{j}}{T_{j}}\right]
$$
\n(26)

And

$$
Q_{i} = -\frac{A}{(2\pi)^{3/2}} T_{i} \left(\frac{T_{i}}{eBR}\right)^{2} \int_{0}^{\infty} \frac{\mathrm{d}x_{i} x_{i}^{7/2} e^{-x_{i}}}{\sum_{k} v_{ik}(x_{i})} \left[\frac{n_{i}'}{n_{i}} + \frac{e_{i} \Phi'}{T_{i}} - \left(\frac{3}{2} - x_{i}\right) \frac{T_{i}'}{T_{i}}\right]
$$
\n(27)

where
$$
A = -\frac{2\sqrt{2}N}{3\pi} \int_{0}^{2\pi} d\theta_0 \sin^2 \theta_0 \int_{a}^{b} d\phi \left(1 - \frac{B}{B_{\text{max}}}\right)^{3/2}, \phi' = -\frac{T_i}{e} \left[\frac{n'}{n} + 3.37 \frac{T'_i}{T_i} \right] [10, 12].
$$

Basically, collisional transport in tokamak depends on toroidal effects. In toroidal geometry, the particle and heat flux are greater than their values in the cylinder. Regardless of the magnetic field ripple effect in neoclassical transport, we can write the following equation for particle and energy flux:

$$
\Gamma_p = -D\frac{\partial n}{\partial r} + \nu n \ , \ \ q_E = -n\chi \frac{\partial T}{\partial r} + \nu nT \tag{28}
$$

[[13](#page-6-10)].

By using Eq. ([2](#page-1-1)) in Sect. [2](#page-1-0), for diffusion coefficient *D*, when $v > \delta \omega_E$ and $\omega_E = E_r/rB$, the radial excursion of a ripple banana is limited by collisions and Eq. ([2](#page-1-1)) is still true. When $\omega_E(\varepsilon T/e)^4 < \delta \omega_E < \nu$, the ripple diffusion is

$$
D_R \sim \varepsilon^2 \left(\frac{v}{r}\right)^{1/2} \left(\frac{T}{eE_r}\right)^{3/2} \left(\frac{T}{eB}\right)^{1/2} \tag{29}
$$

The most complete expressions for the ambipolar diffusion and heat transport by assumption $\alpha \ll 1$ can be written as follows:

$$
\Gamma_a = -\frac{4.1}{v_{ei}} \delta^{3/2} \left(\frac{T_e}{eBR}\right)^2
$$
\n
$$
\times \left[\left(1 + \frac{T_i}{T_e}\right) \frac{dn}{dr} + \frac{7}{2} \frac{n}{T_e} \frac{d}{dr} (T_e + T_i) \right]
$$
\n(30)

$$
Q_i = -\frac{40.6}{v_{ii}} \delta^{3/2} \left(\frac{T_i}{eBR}\right)^2 n \frac{dT_i}{dr_e}
$$

and

$$
v_{ji} = \frac{4}{3} \frac{\sqrt{2\pi}}{m_j^{1/2} T_j^{3/2}} \ln A
$$

where Γ_a is mean particle flux per unit area of either species across a magnetic surface and Q_i is the mean ion heat flux or thermal difusivity.

The simple form for radial profiles of tokamaks can be considered as follows: $n(r) = n_0(1 - x^2)$, $T_i = T_{i0}(1 - x^2)$, $\delta(r) = \delta_a x^2, \ x = r/a \, [1].$ $\delta(r) = \delta_a x^2, \ x = r/a \, [1].$ $\delta(r) = \delta_a x^2, \ x = r/a \, [1].$

The ratio of particle and heat transport for the ripple contribution can be written as foll o w s : $\chi_{iR}/D_R \sim 2(m_i/m_e)^{1/2}(T_i/T_e)^{7/2}(1+T_i/T_e)^{-1}$ while for toroidal contributions can be written as: $\chi_{ib}/D_b \sim 0.5 \, (m_i/m_e)^{1/2} (T_e/T_i)^{7/2} (1 + T_i/T_e)^{-1}$. In the condition of present tokamaks where $T_i/T_e \sim 0.5$, the χ_{iR} is relatively less important than that of in the condition which is $T_i = T_e$.

This difference in the results is due to the difference between values of T_i/T_e [[14](#page-6-11)].

Experimental setup and results

IR-T1 is an air-core transformer-type tokamak with a circular cross section, low beta and large aspect ratio, which has two stainless steels grounded fully, poloidal limiters and ohmic heating discharge system. The average pressure before discharge is in the range of $2.5-2.9 \times 10^{-5}$ Torr. It contains magnetic, electric, rake Mach probes and Mirnov coils for plasma diagnostics. Also it contains toroidal coils, ohmic coils and central solenoid and vertical coils.

Table 1 Some of IR-T1 tokamak characteristics

Fig. 1 Radial profiles of electron temperature versus $x = r/a$ for IR-T1 tokamak parameters

In IR-T1, 16 toroidal feld coils produce a magnetic feld around the torus to confne the plasma.

The experiments were performed in the hydrogen [[15](#page-6-12)]. Some of the main characteristics of IR-T1 are shown in Table [1](#page-4-0) [\[16\]](#page-6-13).

The simple shape of the radial profles of temperature and density is plotted according to Sect. [4,](#page-3-0) formulas. We observed the reduction as we move away from the center and move toward the plasma edge (Figs. [1](#page-4-1), [2,](#page-5-0) [3](#page-5-1), [4\)](#page-5-2).

The ripple ratio δ_B (magnitude of the magnetic field ripple) $\delta_B = (B_{\text{max}} - B_{\text{min}})/(B_{\text{max}} + B_{\text{min}})$ for IR-T1 with 16 coils is calculated as $\delta_R \simeq 0.6$. For TorSopra, $\delta_R = 0.5$, for JET, $\delta_B = 0.08$, for ASDEX, $\delta_B = 0.6$ and for JT060u $\delta_B = 1$ [[17](#page-6-14)].

Losses due to particle and energy transport can create many limitations in the design of the reactor magnet. Of course the number of toroidal coils can afect the dissipation of energy. The amplitude of the ripples is clearly lower when the number of toroidal coils is higher. For example, in JET tokamak, by reducing the number of coils from 32 to 16, the ripples level increased from 1 to 10% [[18](#page-6-15)[–24\]](#page-6-16).

Fig. 2 Radial profiles of density versus $x = r/a$ for IR-T1 tokamak parameters

Fig. 3 Plasma current of IR-T1 tokamak

Fig. 4 Toroidal magnetic field (B_t) of IR-T1 tokamak

The variation in transport coefficients on IR‑T1 tokamak

By using Eqs. (28) (28) and (24) (24) , (30) in Sect. [4](#page-3-0), for ripple and neoclassical transport, the coefficients have been evaluated numerically for IR-T1 tokamak parameters. The variations in the diffusion coefficient and ion heat conductivity with radius for IR-T1 parameters are plotted in Figs. [5](#page-5-3) and [6](#page-5-4), respectively.

As we see in Figs. [5](#page-5-3) and [6](#page-5-4) in the IR-T1 tokamak conditions, particle diffusion coefficient and heat conductivity do not differ

Fig. 5 Comparison of diffusion coefficient due to neoclassical and ripple transport versus radius, *x*=*r*/*a* on IR-T1 tokamak

Fig. 6 Comparison of ion heat conductivity due to neoclassical and ripple transport versus radius, *x*=*r*/*a* on IR-T1 tokamak

greatly. On both graphs, the neoclassical coefficient is decreasing by radius but the ripple distribution is increasing.

Also comparison of the plots shows that the thermal conductivity coefficient increases by increasing the radius, but this increase is faster than the diffusion coefficient with a factor about 4.1.

Conclusion

In this work, we investigated transport coefficients (diffusivity and ion heat conductivity) considering the efects of ripples in the magnetic feld. In addition to the neoclassical difusion, we observed the ripple difusion and compared the transport coefficients for these two modes. The ripple ratio is also calculated numerically, $\delta_B \simeq 0.6$, for IR-T1 tokamak magnetic feld. The observations indicate that difusivity and ion heat conductivity decrease, as we move away from the plasma center in neoclassical mode. But in ripple mode, transport coefficients increase with the radius, and the rate of growth of the conductivity coefficient is greater than the diffusion coefficient.

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